Overview of the package BuyseTest

Brice Ozenne

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This vignette describes the main functionalities of the **BuyseTest** package, focusing on software (and not statistical) aspects, and assume that the reader is familiar with the GPC framework ¹.

The BuyseTest package implements the Generalized Pairwise Comparisons (GPC) as defined in Buyse (2010) for complete observations, and extended in Péron et al. (2018) to deal with right-censoring and Piffoux et al. (2024) to incorporate a restriction time. When considering a single endpoint, the GPC procedure can be summarized as follow. Denote the endpoint by Y in the treatment group and by X in the control group. Given a threshold of clinical relevance τ , the aim of GPC is to estimate the proportion in favor of treatment² $\mathbb{P}[Y \geq X + \tau]$ and the proportion in favor of control $\mathbb{P}[X \geq Y + \tau]$. Their difference $\mathbb{P}[Y \geq X + \tau] - \mathbb{P}[X \geq Y + \tau]$ leads to the net treatment benefit and their ratio $\frac{\mathbb{P}[Y \geq X + \tau]}{\mathbb{P}[X \geq Y + \tau]}$ to the win ratio. The software also evaluate the proportion of neutral pairs $\mathbb{P}[|X - Y| < \tau]$ and which can be included to obtain the probabilistic index $\mathbb{P}[Y \geq X + \tau] + 0.5\mathbb{P}[|X - Y| < \tau]$ or win odds $\frac{\mathbb{P}[Y \geq X + \tau] + 0.5\mathbb{P}[|X - Y| < \tau]}{\mathbb{P}[X \geq Y + \tau] + 0.5\mathbb{P}[|X - Y| < \tau]}$.

- the function BuyseTest performs the GPC procedure and is the main function of the package. The user can interact with its output via various methods:
 - summary to obtain an overview of the results, including the estimated net treatment benefit. The result table at the end of the output can be directly access using model.tables.
 - coef to extract the estimates.
 - confint or model.tables to extract estimates, confidence intervals, and p.values.
 - plot for a graphical display of the scoring of the pair per endpoint.
 - sensitivity to perform a sensitivity analysis on the choice of the threshold(s).
 - nobs to extract the number of observations and pairs.
 - getIid to extract the iid decomposition of the estimator.
 - getPairScore to extract the contribution of each pair to the net treatment benefit.
 - getSurvival to extract the estimates of the survival used for right-censored endpoints.
 - BuyseMultComp to adjust p-values and confidence intervals for multiple comparisons.
- the powerBuyseTest function performs simulation studies, e.g. to estimate the statistical power or assess the bias / type 1 error rate of a test for a specific design. The simBuyseTest function can facilitate the definition of the data generating mechanism.

¹if not, Buyse (2010) is a good place to start.

²in absence of ties this equals the Wilcoxon-Mann-Whitney parameter

• the BuyseTest.options function enables the user to access the default values used in the BuyseTest package. The function can also change the default values to better match the user needs.

Another vignette, "Wilcoxon test via GPC", details connexions between GPC and the Wilcoxon rank sum test. Before going further we need to load the **BuyseTest** package in the R session:

```
library(BuyseTest)
library(data.table)
```

To illustrate the functionalities of the package, we will used the **veteran** dataset from the **survival** package:

```
data(cancer, package = "survival")
veteran <- cbind(id = 1:NROW(veteran), veteran)
veteran$trt <- factor(veteran$trt,1:2,c("Pl","Exp"))
head(veteran)</pre>
```

```
id trt celltype time status karno diagtime age prior
     Pl squamous
                    72
                                            7
1
                             1
                                  60
                                               69
  2 Pl squamous 411
                                  70
                                               64
2
                             1
                                            5
                                                      10
3
  3 Pl squamous 228
                             1
                                  60
                                            3
                                               38
                                                       0
4
  4 Pl squamous
                  126
                                            9
                                               63
                             1
                                  60
                                                      10
  5 Pl squamous
                                  70
                                               65
5
                  118
                             1
                                           11
                                                      10
  6 Pl squamous
                                  20
                                               49
                    10
                             1
                                            5
                                                       0
```

See ?veteran for a presentation of the database.

<u>Note:</u> the **BuyseTest** package is under active development. Newer package versions may include additional functionalities and fix previous bugs. The version of the package that is being is:

```
utils::packageVersion("BuyseTest")
```

```
[1] '3.3.3'
```

For completness, the details of the R session used to generate this document are:

```
sessionInfo()
```

```
R version 4.3.3 (2024-02-29)

Platform: x86_64-pc-linux-gnu (64-bit)

Running under: Ubuntu 22.04.5 LTS

Matrix products: default

BLAS: /usr/lib/x86_64-linux-gnu/blas/libblas.so.3.10.0

LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.10.0

locale:

[1] LC_CTYPE=en_US.UTF-8 LC_NUMERIC=C LC_TIME=en_US.UTF-8

[4] LC_COLLATE=en_US.UTF-8 LC_MONETARY=en_US.UTF-8 LC_MESSAGES=en_US.UTF-8
```

[7] LC_PAPER=en_US.UTF-8 LC_NAME=C LC_ADDRESS=C

[10] LC_TELEPHONE=C LC_MEASUREMENT=en_US.UTF-8 LC_IDENTIFICATION=C

time zone: Europe/Copenhagen
tzcode source: system (glibc)

attached base packages:

[1] stats graphics grDevices utils datasets methods base

other attached packages:

[1] data.table_1.17.2 BuyseTest_3.3.3 Rcpp_1.0.14 prodlim_2025.04.28

[5] ggplot2_3.5.2 survival_3.5-8

loaded via a namespace (and not attached):

[1] Matrix_1.6-5 gtable_0.3.6 future.apply_1.11.3 dplyr_1.1.4 [5] compiler_4.3.3 tidyselect_1.2.1 MatrixModels_0.5-3 parallel_4.3.3

[9] globals_0.18.0 splines_4.3.3 scales_1.4.0 lattice_0.22-5

[13] R6_2.6.1 generics_0.1.3 future_1.49.0 tibble_3.2.1

[17] pillar_1.10.2 RColorBrewer_1.1-3 rlang_1.1.6 cli_3.6.5 [21] withr_3.0.2 magrittr_2.0.3 digest_0.6.37 grid_4.3.3

[21] withr_3.0.2 magrittr_2.0.3 digest_0.6.37 grid_4.3.3 [25] lifecycle_1.0.4 lava_1.8.1 vctrs_0.6.5 SparseM_1.81

[29] glue_1.8.0 farver_2.1.2 listenv_0.9.1 codetools_0.2-19

[33] stats4_4.3.3 colorspace_2.1-1 parallelly_1.44.0 tools_4.3.3

[37] pkgconfig_2.0.3

1 Performing generalized pairwise comparisons (GPC)

To perform generalized pairwise comparisons, the BuyseTest function needs:

• where the data are stored - argument data

• the name of the endpoints - argument endpoint

• the type of each endpoint - argument type

• the variable defining the two treatment groups - argument treatment

The BuyseTest function has many optional arguments. For example:

- the threshold of clinical relevance associated to each endpoint argument threshold
- the censoring associated to each endpoint (for time to event endpoints) argument status

There are two equivalent ways to define the GPC:

• using a separate argument for each element:

Generalized Pairwise Comparisons

```
Settings
```

Point estimation and calculation of the iid decomposition

```
Estimation of the estimator's distribution - method: moments of the U-statistic
```

- or via a formula interface. In the formula interface, endpoints are wrapped by parentheses, preceded by a character string indicated their type:
 - binary (b, bin, or binary)
 - continuous (c, cont, or continuous)
 - time to event (t, tte, or timetoevent)

For instance:

```
BT.f <- BuyseTest(trt ~ tte(time, threshold = 20, status = "status"),
data = veteran, trace = FALSE)
```

where we also set the argument trace to FALSE to execute silently the function. We can check that the two approaches are equivalent:

```
BT.f@call <- list(); BT@call <- list();
testthat::expect_equal(BT.f,BT)</pre>
```

1.1 Displaying the results

The results of the GPC can be displayed using the summary method:

```
summary(BT)
```

Generalized pairwise comparisons with 1 endpoint

```
: net treatment benefit (delta: endpoint specific, Delta: global)
- statistic
- null hypothesis : Delta == 0
- confidence level: 0.95
                 : H-projection of order 1 after atanh transformation
inference
- treatment groups: Exp (treatment) vs. Pl (control)
- censored pairs : probabilistic score based on the survival curves
- results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                                                            Delta
               20
                       100
                                  37.78
                                                 46.54
                                                             15.68
                                                                         0 -0.0877
   time
CI [2.5%; 97.5%] p.value
 [-0.2735;0.1045] 0.37162
```

It displays information about each endpoint, percentage of pairs classified as favorable, unfavorable, neutral, and uninformative, as well as the estimated net treatment benefit (column Delta), its confidence interval, and the corresponding p-value testing the absence of a group difference. To display the number of pairs instead of the percentage of pairs that are favorable/unfavorable/neutral/uniformative, one can set the argument percentage to FALSE. See help(S4BuyseTest-summary) for more details about the summary method, its input and output.

The print method provides a more concise display of the results:

```
print(BT, percentage = FALSE)
```

```
endpoint threshold total favorable unfavorable neutral uninf Delta CI [2.5%; 97.5%] time 20 4692 1772.59 2183.89 735.52 0 -0.0877 [-0.2735;0.1045] p.value 0.37162
```

To access these values, we recommand using the model.tables method that outputs the information from the previous table in a data.frame format:

```
model.tables(BT, percentage = FALSE)
```

An even more concise output can be obtained via the confint method:

```
confint(BT)
```

```
estimate se lower.ci upper.ci null p.value time_t20 -0.08765836 0.09760901 -0.2735301 0.1045245 0 0.371617
```

or coef method:

```
coef(BT)
```

```
time_t20 -0.08765836
```

1.2 What about other summary statistics?

Results for other summary statistics are also accessible:

- argument statistic

- proportion in favor of treatment (favorable): $\mathbb{P}[Y \geq X + \tau]$
- proportion in favor of control (unfavorable): $\mathbb{P}[X \geq Y + \tau]$
- win ratio (winRatio): $\frac{\mathbb{P}[Y \ge X + \tau]}{\mathbb{P}[X \ge Y + \tau]}$

For instance, to display the estimated win ratio instead of the estimated net treatment benefit, use:

```
summary(BT, statistic = "winRatio")
```

Generalized pairwise comparisons with 1 endpoint

```
: win ratio (delta: endpoint specific, Delta: global)
- null hypothesis : Delta == 1
- confidence level: 0.95
- inference
                  : H-projection of order 1 after log transformation
- treatment groups: Exp (treatment) vs. Pl (control)
- censored pairs : probabilistic score based on the survival curves
- results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) Delta
                                   37.78
                                                  46.54
   time
                20
                        100
                                                             15.68
                                                                          0 0.8117
CI [2.5%; 97.5%] p.value
  [0.5134;1.2833] 0.37195
```

In presence of ties, the null distribution of the proportion in favor of treatment or control depends on the data generative mechanism and the threshold of clinical relevance. This is why, unless the argument null is provided by the user, the confint method will not produce any p.value:

```
confint(BT, statistic = "favorable")
```

```
estimate se lower.ci upper.ci null p.value time_t20 0.3777905 0.04902199 0.2874747 0.477467 NA NA
```

A permutation test may be used to empirically estimate a value for the null hypothesis:

```
BT.perm <- BuyseTest(trt ~ tte(time, threshold = 20, status = "status"),
data = veteran, trace = FALSE,
method.inference = "permutation", seed = 10)
confint(BT.perm, statistic = "favorable")
```

```
estimate se lower.ci upper.ci null p.value time_t20 0.3777905 0.04770182 NA NA 0.4205855 0.3636364
```

which, in this example, is around 0.42. It worth noting that testing an inadequate null hypothesis can have dramatic consequences on the p-value:

```
estimate se lower.ci upper.ci null p.value
time_t20 0.3777905 0.04902199 0.2874747 0.477467 0.42 0.39826735
time_t201 0.3777905 0.04902199 0.2874747 0.477467 0.50 0.01673643
```

Considering the proportion of neutral pairs in the summary statistics: - argument add.halfNeutral

- Wilcoxon-Mann-Whitney parameter or probabilistic index: $\mathbb{P}[Y \ge X + \tau] + 0.5\mathbb{P}[|Y X| < \tau]$.
- win odds: $\frac{\mathbb{P}[Y \geq X + \tau] + 0.5\mathbb{P}[|Y X| < \tau]}{\mathbb{P}[X \geq Y + \tau] + 0.5\mathbb{P}[|Y X| < \tau]}.$

have been recommended (e.g. Ajufo et al. (2023)) over the win ratio. These summary statistics can be output by specifying the argument add.halfNeutral to TRUE when calling BuyseTest:

```
BT.half <- BuyseTest(trt ~ tte(time, threshold = 20, status = "status"),

data = veteran, trace = FALSE, add.halfNeutral = TRUE)

confint(BT.half, statistic = "favorable")
```

```
estimate se lower.ci upper.ci null p.value time_t20 0.4561708 0.04880921 0.3632263 0.5522714 0.5 0.3716632
```

```
confint(BT.half, statistic = "winRatio")
```

```
estimate se lower.ci upper.ci null p.value time_t20 0.8388127 0.1650208 0.5704361 1.233454 1 0.3716211
```

Testing a net treatment benefit of 0, a win odds of 1, or a Wilcoxon-Mann-Whitney parameter of 0.5 corresponds to the same hypothesis and therefore the same p-value should be obtained. The (small) discrepancy in p-values observed in this example (0.371617 vs. 0.3716211 vs. 0.3716632) are due to small sample approximation. Such discrepancies will not arise when using non-parametric bootstrap or permutation tests using quantiles of the bootstrap or permutation distribution, e.g.:

```
estimate se lower.ci upper.ci null p.value netBenefit -0.08765836 0.10021632 -0.2720510 0.1033974 0.0 0.383 winRatio 0.83881270 0.17440155 0.5722640 1.2306429 1.0 0.383 favorable 0.45617082 0.05010816 0.3639745 0.5516987 0.5 0.383
```

1.3 Stratified GPC

GPC can be performed for subgroups of a categorical variable

- argument strata

For instance, the celltype may have huge influence on the survival time and the investigator would like to only compare patients that have the same celltype. In the formula interface this is achieved by adding this variable wrapped by parenthesis and preceded by the character string strata in the formula:

```
ffstrata <- trt \sim tte(time, threshold = 20, status = "status") + strata(celltype) BTstrata <- BuyseTest(ffstrata, data = veteran, trace = 0)
```

When doing a stratified analysis, the summary method displays strata-specific and global results³:

Generalized pairwise comparisons with 1 endpoint and 4 strata

```
: net treatment benefit (delta: endpoint specific, Delta: global)
- null hypothesis : Delta == 0
- confidence level: 0.95
                  : H-projection of order 1 after atanh transformation
- inference
- treatment groups: Exp (treatment) vs. Pl (control)
- strata weights : 26.38%, 34.63%, 18.47%, 20.52%
- uninformative pairs: no contribution
- results
endpoint
            strata total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                                                                 delta
                                                                                         Delta
                                                   45.77
                                                                         0.85 -0.0997 -0.0997
                     100.00
                                    36.06
                                                               17.33
    time
            global
          squamous
                      25.38
                                    14.33
                                                     8.77
                                                                2.28
                                                                         0.00 0.2193
         smallcell
                      45.69
                                    12.69
                                                    20.88
                                                               11.27
                                                                         0.85 -0.1792
                                                                         0.00 - 0.1034
             adeno
                      13.71
                                     4.74
                                                     6.15
                                                                2.81
             large
                      15.23
                                     4.30
                                                     9.97
                                                                0.96
                                                                         0.00 - 0.3722
```

The percentage of pairs in the total/favorable/unfavorable/neutral/uninf columns are relative to the overall number of pairs whereas the column delta presents the endpoint and strata-specific net treatment benefits (in the last 4 lines). The last column (Delta) displays the global (i.e. pooled over strata), conditional, net treatment benefit.

⚠ With the default way of pooling results across strata, the proportion of favorable pairs minus the proportion of unfavorable pairs (36.06%-45.77%=9.71%) does not equal the global net treatment benefit (9.97%). To retrieve this value of the Net Treatment Benefit, one should first extract the number of pairs per strata using the method nobs:

```
strata.obs <- as.data.frame(nobs(BTstrata, strata = TRUE))
strata.obs</pre>
```

```
Pl Exp pairs squamous 15 20 300
```

³the strata-specific results can be removed by setting the argument strata to "global" when calling summary.

```
smallcell 30 18 540
adeno 9 18 162
large 15 12 180
```

and use the method model.tables to extract the number of favorable and unfavorable pairs per strata:

```
strata total favorable unfavorable
2 squamous 300 169.40260 103.6104
3 smallcell 540 150.00000 246.7778
4 adeno 162 56.00000 72.7500
5 large 180 50.83333 117.8333
```

We retrieve the strata-specific net treatment benefits by comparing, in each strata, the number of favorable and unfavorable pairs relative to the number of pairs⁴:

```
delta <- (dfStrata$favorable - dfStrata$unfavorable)/strata.obs$pairs delta
```

```
[1] 0.2193074 -0.1792181 -0.1033951 -0.3722222
```

The global net treatment benefit is then the sum of the strata-specific net treatment benefits weighted by the strata weights:

```
weightCMH <- strata.obs$pairs/(strata.obs$Pl + strata.obs$Exp)
list(estimate = sum(delta * weightCMH/sum(weightCMH)),
    weight = 100*weightCMH/sum(weightCMH))</pre>
```

\$estimate

[1] -0.09967584

\$weight

[1] 26.38329 34.62807 18.46830 20.52034

The approach is true for the probabilistic index but not for the win ratio/odds: the ratio between the global proportions is taken, i.e., pooling is performed at the numerator and at the denominator instead of pooling fractions - see Dong et al. (2018), equation 1.

⁴Alernatively one could compute, from the summary, the difference between the percentage of favorable and unfavorable pairs relative to the percentage of pairs in the strata, e.g. $(14.33\% - 8.77\%)/25.38\% \approx 21.93\%$

The default weighting scheme is CMH, standing for Cochran-Mantel-Haenszel, which has been recommaned in the litterature (Dong et al., 2018). It is efficient under the assumption of a common multiplicative effect (across strata) on the odds ratio scale.

Other weighting schemes can be used.

- argument pool.strata.

When considering additive effect, one should instead weight proportionally to the number of pairs:

```
BTstrata2 <- BuyseTest(ffstrata, data = veteran, trace = 0, pool.strata = "buyse")
summary(BTstrata2, type.display = keep.colStrata)
```

Generalized pairwise comparisons with 1 endpoint and 4 strata

```
: net treatment benefit (delta: endpoint specific, Delta: global)
- statistic
- null hypothesis : Delta == 0
- confidence level: 0.95
                  : H-projection of order 1 after atanh transformation
- inference
- treatment groups: Exp (treatment) vs. Pl (control)
- strata weights : 25.38%, 45.69%, 13.71%, 15.23%
- uninformative pairs: no contribution
- results
            strata total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
endpoint
                                                                                delta
                                                                                        Delta
                                                                         0.85 -0.0971 -0.0971
    time
            global
                     100.00
                                   36.06
                                                   45.77
                                                               17.33
          squamous
                      25.38
                                    14.33
                                                    8.77
                                                               2.28
                                                                         0.00 0.2193
         smallcell
                                    12.69
                                                   20.88
                                                                         0.85 -0.1792
                      45.69
                                                               11.27
                                                                         0.00 -0.1034
                      13.71
                                     4.74
                                                    6.15
                                                                2.81
             adeno
             large
                      15.23
                                     4.30
                                                    9.97
                                                               0.96
                                                                         0.00 - 0.3722
```

The strata-specifc net treatment benefits are unchanged: the weighting scheme only affects the evaluation of the overall net treatment benefit. With this weighting scheme it now equals the difference between the overall proportion of favorable vs. unfavorable pairs (36.06%-45.77%). While extractors will by default output global estimates (i.e. after pooling the results over strata)

```
confint(BTstrata2)
```

```
estimate se lower.ci upper.ci null p.value time t20 -0.09706901 0.0977929 -0.2829348 0.09582321 0 0.323961
```

one can specify the argument strata to extract strata-specific estimates:

```
confint(BTstrata, strata = TRUE)
```

```
estimate se lower.ci upper.ci null p.value time_t20.squamous 0.2193074 0.1911515 -0.1690137 0.5486919 0 0.2669352 time_t20.smallcell -0.1792181 0.1540933 -0.4567640 0.1301230 0 0.2551275 time_t20.adeno -0.1033951 0.2465197 -0.5314450 0.3667172 0 0.6771002 time_t20.large -0.3722222 0.2190018 -0.7110335 0.1068610 0 0.1240457
```

The pooled estimator presented in this section has a conditional interpretation, as they summarize comparisons made between observations from the same strata. They will generally differ from the marginal (i.e. non-adjusted) Net Treatment Benefit and tend to be more extreme (i.e. away from 0) in presence of group difference.

1.4 Standardization

When the interest lies in a marginal effect but one wish to adjust on baseline covariates to obtain more precise estimate, one should *not* restrict the comparisons between pairs of observations from the same strata. Instead one should estimate a Net Treatment Nenefit for each possible combinations of strata and pool the results (Buyse et al. (2025), chapter 9). This is what is being done when setting the argument pool.strata to "standardization":

```
BTstd <- BuyseTest(ffstrata, data = veteran, trace = 0, pool.strata = "standardization")
model.tables(BTstd)[,c("strata","total","delta","Delta","lower.ci","upper.ci","p.value")]
```

	strata	total	delta	Delta	lower.ci	upper.ci	p.value
1	global	100.000000	-0.11874500	-0.118745	-0.2857534	0.0552638	0.1805479
2	squamous	6.393862	0.21930736	NA	NA	NA	NA
3	smallcell.squamous	12.787724	0.35699653	NA	NA	NA	NA
4	adeno.squamous	3.836317	0.41018519	NA	NA	NA	NA
5	large.squamous	6.393862	0.03622106	NA	NA	NA	NA
6	squamous.smallcell	5.754476	-0.50654161	NA	NA	NA	NA
7	smallcell	11.508951	-0.17921811	NA	NA	NA	NA
8	adeno.smallcell	3.452685	-0.25308642	NA	NA	NA	NA
9	large.smallcell	5.754476	-0.80740741	NA	NA	NA	NA
10	squamous.adeno	5.754476	-0.41165224	NA	NA	NA	NA
11	smallcell.adeno	11.508951	-0.02906379	NA	NA	NA	NA
12	adeno	3.452685	-0.10339506	NA	NA	NA	NA
13	large.adeno	5.754476	-0.76311728	NA	NA	NA	NA
14	squamous.large	3.836317	-0.04494949	NA	NA	NA	NA
15	smallcell.large	7.672634	0.25946502	NA	NA	NA	NA
16	adeno.large	2.301790	0.21296296	NA	NA	NA	NA
17	large	3.836317	-0.37222222	NA	NA	NA	NA

Here strata equal to squamous means that the comparison betwen the active and control group was made using only patients whose lung cancer cell type were squamous. We retrive the same results as when setting pool.strata to "buyse" or "CMH". However now additional strata have been added like "smallcell.squamous" where control patients whose lung cancer cell type were smallcell are being compared to active patients whose lung cancer cell type were squamous. Indeed:

```
endpoint threshold Delta
time 20 0.357
```

leads, up to rounding, to the same result.

<u>Note:</u> it is possible to extract the strata-specific estimate (e.g. coef(BTstd, strata = TRUE)) but the software does not keep track of the strata-specific uncertainty via the H-decomposition and thus not able to output confidence intervals. A resampling method could be used if those are of interest:

```
BTstd.boot <- BuyseTest(ffstrata, data = veteran, trace = 0, pool.strata = "standardization", method.inference = "bootstrap", n.resampling = 100, seed = 10) confint(BTstd.boot, strata = TRUE)[1:6,]
```

Estimated p-value of 1 - consider increasing the number of boostrap samples

```
estimate
                                               se
                                                     lower.ci
                                                                upper.ci null
                                                                                 p.value
time_t20.squamous
                             0.21930736 0.2080541 -0.20675900
                                                               0.5739010
                                                                            0 0.31000000
time_t20.smallcell.squamous
                            0.35699653 0.1687546 0.05407602
                                                               0.6725760
                                                                            0 0.00990099
                             0.41018519 0.1934063 0.02191406
time_t20.adeno.squamous
                                                               0.7106061
                                                                            0 0.02000000
time_t20.large.squamous
                             0.03622106 0.2205302 -0.36689103
                                                                            0 1.00000000
                                                               0.4289194
time_t20.squamous.smallcell -0.50654161 0.1702545 -0.80210648 -0.1179729
                                                                            0 0.00990099
                            -0.17921811 0.1738337 -0.49175000 0.1397222
time_t20.smallcell
                                                                            0 0.3000000
```

Here n.resampling was set to a low value only to save computation time but this may lead to unreliable confidence intervals/p-values: larger values are recommended (e.g. 10000).

1.5 Using multiple endpoints

More than one endpoint can be considered by indicating a vector of endpoints, types, and thresholds. In the formula interface, the different endpoints must be separated with a "+" on the right hand side of the formula:

```
ff2 <- trt ~ tte(time, threshold = 20, status = "status") + cont(karno, threshold = 0)
BT.H <- BuyseTest(ff2, data = veteran, trace = 0)
summary(BT.H)</pre>
```

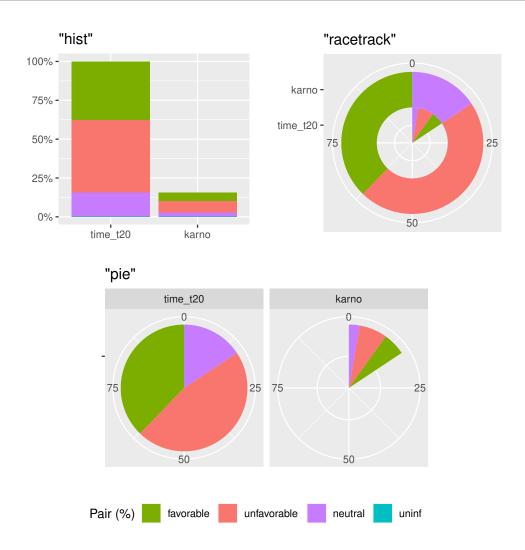
Generalized pairwise comparisons with 2 prioritized endpoints

```
: net treatment benefit (delta: endpoint specific, Delta: global)
- statistic
- null hypothesis : Delta == 0
- confidence level: 0.95
- inference
                  : H-projection of order 1 after atanh transformation
- treatment groups: Exp (treatment) vs. Pl (control)
- censored pairs : probabilistic score based on the survival curves
- neutral pairs
                  : re-analyzed using lower priority endpoints
- results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                                                               delta
                                                                                       Delta
    time
                20
                     100.00
                                   37.78
                                                   46.54
                                                              15.68
                                                                           0 -0.0877 -0.0877
  karno
                      15.68
                                    5.78
                                                    7.11
                                                               2.78
                                                                           0 -0.0133 -0.1009
CI [2.5%; 97.5%] p.value
 [-0.2735;0.1045] 0.37162
 [-0.2901;0.0959] 0.31478
```

The hierarchy of the endpoint is defined from left (most important endpoint, here time) to right (least important endpoint, here karno). In the summary output, the confidence intervals and p.values are computed for the column Delta, i.e. here -8.77% is the net treatment benefit for the first endpoint (line 1) and -10.09% is the net treatment benefit for the first and second endpoint (line 2). In other words, the last confidence interval and p-value is the one for the analysis over all endpoints (generally the one to report).

A graphical representation of the GPC procedure can be obtained by the plot method. It will display the percentage of favorable, unfavorable, neutral, and uninformative pairs per endpoint. Three (equivalent) graphical display are possible, the first one ("hist") being the recommanded one:

```
plot(BT.H, type = "hist")
plot(BT.H, type = "pie")
plot(BT.H, type = "racetrack")
```



It is also possible to perform the comparisons on all pairs for all endpoints by setting the argument hierarchical to FALSE:

```
BT.nH <- BuyseTest(ff2, hierarchical = FALSE, data = veteran, trace = 0)
summary(BT.nH)</pre>
```

Generalized pairwise comparisons with 2 endpoints

```
- statistic
                  : net treatment benefit (delta: endpoint specific, Delta: global)
- null hypothesis : Delta == 0
- confidence level: 0.95
- inference
                  : H-projection of order 1 after atanh transformation
- treatment groups: Exp (treatment) vs. Pl (control)
- censored pairs : probabilistic score based on the survival curves
- results
endpoint threshold weight total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                          37.78
    time
                20
                      0.5
                               100
                                                          46.54
                                                                     15.68
                                                                                  0 - 0.0877
  karno
                      0.5
                               100
                                          41.82
                                                          44.95
                                                                     13.24
                                                                                  0 -0.0313
 Delta CI [2.5%; 97.5%] p.value
-0.0438 [-0.1388;0.0519] 0.36977
-0.0595 [-0.2267;0.1111] 0.49514
```

In that case the score of a pair is the weighted sum of the score relative to each endpoint. By default, the weights are all set to the same value but this behavior can be changed by setting the argument weight when calling BuyseTest, e.g.:

```
endpoint threshold weight total favorable unfavorable neutral uninf
                                                                              delta
                        0.8
                              100 37.77905
                                               46.54489 15.67606
1
               2e+01
                                                                      0 -0.08765836
     time
               1e-12
                        0.2
                              100 41.81586
                                               44.94885 13.23529
3
                                                                      0 -0.03132992
     karno
                lower.ci
                           upper.ci
                                      p.value
        Delta
1 -0.07012668 -0.2203714 0.08336855 0.3707289
3 -0.07639267 -0.2503756 0.10237001 0.4026905
```

This has been referred as the O'Brien test in the litterature (Verbeeck et al. (2019), section 3.2). Alternatively, one may be interested in the endpoint specific results. This can be performed by applying the BuyseTest function separately to each endpoint, e.g.:

```
	ext{confint(BuyseTest(trt} \sim 	ext{cont(karno, threshold = 0), data = veteran, trace = 0))}
```

```
estimate se lower.ci upper.ci null p.value karno -0.03132992 0.09787113 -0.2197111 0.1593037 0 0.7490407
```

or setting the argument cumulative to FALSE when calling the confint function:

```
confint(BT.nHw, cumulative = FALSE)
```

```
estimate se lower.ci upper.ci null p.value
time_t20 -0.08765836 0.09760901 -0.2735301 0.1045245 0 0.3716170
karno -0.03132992 0.09787113 -0.2197111 0.1593037 0 0.7490407
```

Note: the apparent discrepency in p-value between the hierarchical and non-hierarchical GPC at the first priority (0.3762 vs 0.3698 vs 0-3707) is due to the use of a transformation that makes the p-value dependent on the estimate. Otherwise the p-value would be the same at the first priority, e.g.:

```
confint(BT.nHw, transform = FALSE)
```

```
        estimate
        se
        lower.ci
        upper.ci
        null
        p.value

        time_t20
        -0.07012668
        0.07808721
        -0.2231748
        0.08292143
        0
        0.3691557

        karno
        -0.07639267
        0.09093303
        -0.2546181
        0.10183280
        0
        0.4008534
```

1.6 Statistical inference

Uncertainty about the estimates can be quantified using:

- argument method.inference

• **permutation test** ("permutation"). Assuming exchangeability under the null hypothesis, this approach gives valid p-values (regardless to the sample size) for testing the absence of a difference between the groups.

```
BT.perm <- BuyseTest(trt ~ tte(time, threshold = 20, status = "status"),
data = veteran, trace = 0, method.inference = "permutation",
seed = 10)
summary(BT.perm)
```

Generalized pairwise comparisons with 1 endpoint

```
- statistic
                  : net treatment benefit (delta: endpoint specific, Delta: global)
- null hypothesis : Delta == 0
- confidence level: 0.95
- inference
                  : permutation test with 1000 samples
                   p-value computed using the permutation distribution
- treatment groups: Exp (treatment) vs. Pl (control)
- censored pairs : probabilistic score based on the survival curves
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) Delta p.value
                                   37.78
                                                  46.54
                                                                          0 -0.0877 0.35265
   time
                20
                        100
                                                             15.68
```

• bootstrap resampling ("bootstrap"). In large enough samples, this approach gives valid p-values and confidence intervals.

Generalized pairwise comparisons with 1 endpoint

```
- statistic
                  : net treatment benefit (delta: endpoint specific, Delta: global)
- null hypothesis : Delta == 0
- confidence level: 0.95
- inference
                  : bootstrap resampling with 1000 samples
                    CI computed using the percentile method; p-value by test inversion
- treatment groups: Exp (treatment) vs. Pl (control)
- censored pairs : probabilistic score based on the survival curves
- results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                   37.78
                                                  46.54
                                                             15.68
               20
                        100
                                                                          0 -0.0877
CI [2.5%; 97.5%] p.value
 [-0.2721;0.1034]
                 0.383
```

• asymptotic distribution ("u-statistic"). In large enough samples, this approach gives valid p-values and confidence intervals (Ozenne et al., 2021).

```
BT.ustat <- BuyseTest(trt ~ tte(time, threshold = 20, status = "status"),

data = veteran, trace = 0, method.inference = "u-statistic")
summary(BT.ustat)
```

Generalized pairwise comparisons with 1 endpoint

```
: net treatment benefit (delta: endpoint specific, Delta: global)
- statistic
- null hypothesis : Delta == 0
- confidence level: 0.95
                  : H-projection of order 1 after atanh transformation
- inference
- treatment groups: Exp (treatment) vs. Pl (control)
- censored pairs : probabilistic score based on the survival curves
- results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                                                              Delta
                20
                        100
                                   37.78
                                                  46.54
                                                             15.68
                                                                          0 -0.0877
CI [2.5%; 97.5%] p.value
 [-0.2735;0.1045] 0.37162
```

The first two approaches require simulating a large number of samples and applying the GPC to each of these samples. The seed argument is used to generate a seed for each sample. The number of samples is set using the arugment n.resampling and it should large enough to limit the Monte Carlo error when estimating the p-value. Typically should be at least 10000 to get, roughtly, 2-digit precision, as examplified below:

```
set.seed(10)
sapply(1:10, function(i){mean(rbinom(1e4, size = 1, prob = 0.05))})
```

[1] 0.0511 0.0491 0.0489 0.0454 0.0516 0.0522 0.0468 0.0483 0.0491 0.0508

Indeed, here we get a reasonnable approximation of 0.05 (if we round and only keep 2 digits). Note that to get 3 digits precision we would need more samples. The last method does not rely on resampling but on the computation of the influence function of the estimator. Fortunately, when using the Gehan's scoring rule, this does not really involve any extra-calculations and this is therefore very fast to perform. When using the Peron's scoring rule, more serious extra-calculations are involved so the computation time is expected to increase by a factor 5 to 10 compared to the point estimate alone (i.e. method.inference equal to "none").

It is possible to relax the exchangeability assumption using a studentized permutation. A studentized bootstrap is also possible to improve on the better small samples properties of the bootstrap confidence intervals. Both rely on the asymptotic approach to estimate standard errors and are more numerically intensive.

1.7 What if smaller is better?

By default BuyseTest will always assume that higher values of an endpoint are favorable. This behavior can be changed by specifying operator = "<0" for an endpoint:

```
ffop <- trt ~ tte(time, status = "status", threshold = 20, operator = "<0")
BTinv <- BuyseTest(ffop, data = veteran, trace = 0)
summary(BTinv)</pre>
```

Generalized pairwise comparisons with 1 endpoint

```
: net treatment benefit (delta: endpoint specific, Delta: global)
- statistic
- null hypothesis : Delta == 0
- confidence level: 0.95
                 : H-projection of order 1 after atanh transformation
- inference
- treatment groups: Exp (treatment) vs. Pl (control)
- censored pairs : probabilistic score based on the survival curves
- results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) Delta
                                                                         0 0.0877
                                  46.54
                                                 37.78
               20 100
                                                            15.68
CI [2.5%; 97.5%] p.value
 [-0.1045;0.2735] 0.37162
```

Internally BuyseTest will compute the favorable and unfavorable score as usual and then switch them around if the operator equals "<0".

1.8 Stopping comparison for neutral pairs

In presence of neutral pairs, BuyseTest will, by default, continue the comparison on the endpoints with lower priority. For instance let consider a dataset with one observation in each treatment arm:

```
Id treatment tumor size
1: 1 Yes Yes 15
2: 2 No Yes 20
```

If we use the GPC with tumor as the first endpoint and size as the second endpoint:

Generalized pairwise comparisons with 2 prioritized endpoints

```
: net treatment benefit (delta: endpoint specific, Delta: global)
- treatment groups: Yes (treatment) vs. No (control)
                  : re-analyzed using lower priority endpoints
- neutral pairs
- results
endpoint total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) delta Delta
  tumor
              100
                             0
                                             0
                                                      100
                                                                 0
                                                                       0
                                             0
                                                                 0
    size
              100
                           100
                                                        0
                                                                       1
                                                                              1
```

the outcome of the comparison is neutral for the first priority, but favorable for the second. Setting the argument neutral.as.uninf to FALSE will stop the comparison when a pair is classified as neutral:

```
BT.pair2 <- BuyseTest(treatment ~ bin(tumor) + cont(size, operator = "<0"), data = dt.sim, trace = 0, method.inference = "none", neutral.as.uninf = FALSE) summary(BT.pair2)
```

Generalized pairwise comparisons with 2 prioritized endpoints

```
: net treatment benefit (delta: endpoint specific, Delta: global)
- treatment groups: Yes (treatment) vs. No (control)
- neutral pairs : ignored at lower priority endpoints
- results
endpoint total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) delta Delta
              100
                             0
                                                      100
                                                                 0
  tumor
                                             0
                                                                        0
                0
                             0
                                             0
                                                        0
                                                                 0
                                                                       0
                                                                              0
    size
```

So in this case no pair is analyzed at second priority.

1.9 Is multiple testing a concern with GPC?

Yes, as with any other statistical method. Having a pre-defined statistical plan (i.e. written before looking at the data) specifying the hierarchy of endpoints, their threshold of clinical relevance is recommanded. When planning multiple GPC, summarize the results can be done via one of two principles:

• intersection union principle: one rejects the (global) null hypothesis if there is evidence for an effect in all the GPC analyses. This is typically a sensitivity analysis: checking that the results are not too sensitive to the choice of an hyperparameter. No multiplicity adjustment is needed other than considering the largest p-value among all tests. For instance, when checking whether the estimated net treatment benefit is similar across a range of threshold of clincial relevance, we would obtain a p-value of 0.76

```
BTse <- sensitivity(BT.ustat, threshold = seq(0,500, length.out=10),
trace = FALSE)
BTse
```

```
time
                estimate
                                 se
                                       lower.ci
                                                  upper.ci null
                                                                   p.value
     0.00000 -0.08752774 0.10041203 -0.27851884 0.11012263
1
                                                               0 0.3858177
2
    55.5556 -0.08095829 0.08957699 -0.25229456 0.09530004
                                                               0 0.3682107
  111.11111 -0.03170177 0.07463991 -0.17629003 0.11422560
3
                                                               0 0.6712414
              0.01896964 0.06452954 -0.10713643 0.14447503
4
   166.66667
                                                               0 0.7688360
              0.03315614 0.05523512 -0.07506821 0.14060850
5
  222.22222
                                                               0 0.5486177
             0.04217485 0.04654025 -0.04914025 0.13279075
6
  277.77778
                                                               0 0.3653982
7
             0.04112991 0.03946828 -0.03631838 0.11808708
                                                               0 0.2979105
  333.33333
  388.88889
              0.04075638 0.03300933 -0.02402114 0.10519310
                                                               0 0.2174545
8
  444.4444
              0.04097871 0.03027888 -0.01844156 0.10011054
                                                               0 0.1764199
10 500.00000
             0.03517173 0.02769280 -0.01915553 0.08929191
                                                               0 0.2044340
```

• union intersection principle: one rejects the (global) null hypothesis if there is evidence for an effect for at least on of the GPC analyses. This is a typical exploratory analysis where one look for the most promising outcome. Adjustment for multiplicity is needed. Since estimates from GPC procedure are typically highly correlated, one can improve on bonferroni adjustment using a max-test adjustment. This is what is performed via the <code>BuyseMultComp</code> function:

```
BuyseMultComp(BT.H, endpoint = 1:2)
```

karno

0.3508339

Here we look at whether there is a benefit in survival alone (first priority time_t20) or a benefit over both endpoint (second priority karno). Setting the argument cumulative to FALSE when considering nonhierarchical GPC analyses enables to efficiently adjust endpoint-specific GPC for multiple comparisons:

```
BuyseMultComp(BT.nH, cumulative = FALSE, endpoint = 1:2)
```

- Univariate tests:

```
estimate se lower.ci upper.ci null p.value lower.band upper.band time_t20 -0.08765836 0.09760901 -0.2735301 0.1045245 0 0.3716170 -0.2953329 0.1279261 karno -0.03132992 0.09787113 -0.2197111 0.1593037 0 0.7490407 -0.2420777 0.1822409 adj.p.value time_t20 0.5597555 karno 0.9236602
```

One can also consider the global endpoint of two different GPC analyses:

```
BuyseMultComp(list(hierarchical = BT.H, Obrien = BT.nH), cluster = "id")
```

```
- Univariate tests:
```

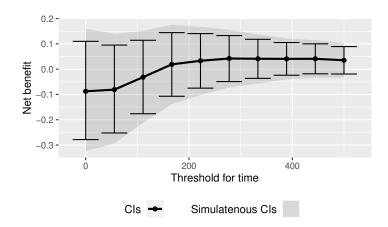
```
estimate
                                 se
                                      lower.ci
                                                  upper.ci null
                                                                  p.value lower.band
hierarchical -0.10092285 0.09971277 -0.2901336 0.09588144
                                                              0 0.3147770 -0.3014645
             -0.05949414 0.08700807 -0.2266953 0.11111326
                                                              0 0.4951361 -0.2368800
Obrien
             upper.band adj.p.value
hierarchical 0.1081696
                          0.3831444
Obrien
              0.1217304
                          0.5851872
```

Finally the **sensitivity** method can also be used to adjust for multiple comparisons over multiple thresholds:

```
time
             estimate
                      lower.ci
                               upper.ci
                                        p.value lower.band upper.band adj.p.value
1
     0.00000 \ -0.08752774 \ -0.27851884 \ 0.11012263 \ 0.3858177 \ -0.32447773 
                                                          0.1597587
                                                                    0.7745625
2
   55.55556 -0.08095829 -0.25229456 0.09530004 0.3682107 -0.29398532
                                                          0.1397311
                                                                    0.7528122
  111.11111 -0.03170177 -0.17629003 0.11422560 0.6712414 -0.21221507
3
                                                          0.1509036
                                                                    0.9810274
           0.01896964 \ -0.10713643 \ 0.14447503 \ 0.7688360 \ -0.13890539
4
  166.66667
                                                          0.1759043
                                                                    0.9969926
  222.2222 0.03315614 -0.07506821 0.14060850 0.5486177 -0.10248262
5
                                                          0.1675845
                                                                    0.9257172
  6
                                                          0.1556050
                                                                    0.7492675
  7
                                                          0.1375213
                                                                   0.6545176
  388.88889 0.04075638 -0.02402114 0.10519310 0.2174545 -0.04052732
8
                                                          0.1215042
                                                                    0.5203739
  444.4444 0.04097871 -0.01844156 0.10011054 0.1764199 -0.03358825
                                                          0.1150920
                                                                    0.4429140
0.1030201
                                                                    0.4967546
```

Here by setting the argument band to TRUE (and adj.p.value to TRUE), we obtain confidence intervals (and p-values) adjusted for multiple comparisons. Said otherwise, the columns lower.ci and upper.ci provide a (pointwise) confidence interval with 95% coverage for a given threshold while the columns lower.band and upper.band provide a (simutaneous) confidence interval with 95% coverage across all given thresholds. The difference can be visualized using the autoplot method:

```
library(ggplot2)
autoplot(BTse.ustat)
```



Simultaneous and pointwise confidence intervals are here of similar width due to the very high correlation between estimates across thresholds:

```
BTse.cor <- cor(lava::iid(BTse.ustat))
range(BTse.cor[lower.tri(BTse.cor)])
```

[1] 0.3716902 0.9848999

Note that with multiple endpoints, the thresholds can be specified using a list:

```
BTse.H <- sensitivity(BT.H, trace = FALSE,
threshold = list(time = seq(0,500,length = 10), karno = c(0,40,80)))
head(BTse.H)
```

```
upper.ci null
       time karno
                     estimate
                                       se
                                            lower.ci
                                                                        p.value
                0 -0.08754474 0.10044847 -0.2786016 0.11017738
    0.00000
                                                                    0 0.3858987
  55.55556
                0 -0.11177487 0.09915501 -0.2995661 0.08435417
                                                                   0 0.2636263
3 111.11111
                0 -0.08618872 0.09822940 -0.2732475 0.10715096
                                                                    0 0.3826244
4 166.66667
                0 -0.05180121 0.09818252 -0.2400240 0.14017526
                                                                   0 0.5984319
 222.22222
                0 -0.03668720 0.09810141 -0.2253052 0.15458146
                                                                    0 0.7086747
6 277.77778
                0 -0.02906324 0.09773146 -0.2172647 0.16122161
                                                                    0 0.7663054
```

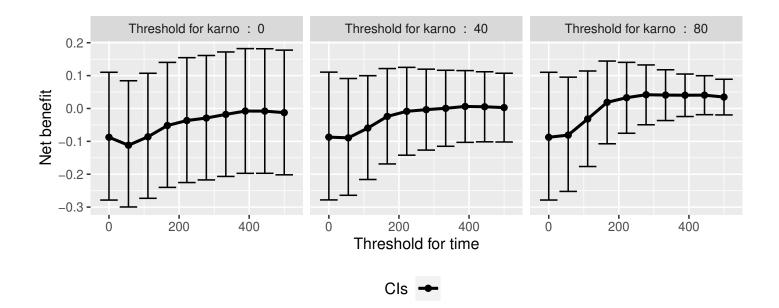
or a matrix:

```
grid <- expand.grid(list("time_t20" = seq(0,500,length = 10), "karno" = c(0,40,80)))
cbind(head(grid)," " = " ... ",tail(grid))
BTse.H2 <- sensitivity(BT.H, threshold = grid, trace = FALSE)
range(BTse.H-BTse.H2)</pre>
```

```
time_t20 karno
                             time_t20 karno
    0.00000
                 0
                             222.2222
                                          80
1
2
  55.55556
                 0
                             277.7778
                                          80
3 111.11111
                 0
                             333.3333
                                          80
4 166.66667
                 0
                             388.8889
                                          80
 222.22222
                 0
                             444.4444
                                          80
6 277.77778
                             500.0000
                                          80
[1] 0 0
```

The latter should be used when the same endpoint is used at different priorities (each column correspond to the threshold that should be used at a priority). As before we can display the results using the autoplot function:

```
autoplot(BTse.H, col = NA)
## alternative display:
## autoplot(BTse.H, position = position_dodge(width = 15))
```



The autoplot function can only be used when 1 or 2 thresholds are varied at the same time.

2 Getting additional inside: looking at the pair level

So far we have looked at the overall score and probabilities. But it is also possible to extract the score relative to each pair, as well as to "manually" compute this score. This can give further inside on what the software is actually doing and what is the contribution of each individual on the evaluation of the treatment.

2.1 Extracting the contribution of each pair to the statistic

The net treatment benefit or the win ratio statistics can be expressed as a sum of a score over all pairs of patients. The argument keep.pairScore enables to export the score relative to each pair in the output of BuyseTest:

The method **getPairScore** can then be used to extract the contribution of each pair. For instance the following code extracts the contribution for the first endpoint:

```
getPairScore(BT.keep, endpoint = 1)
```

```
Key: <index.Exp, index.Pl>
       index.Pl index.Exp favorable unfavorable neutral uninf weight
                1
                           70
                                         1
                                                       0
                                                                 0
                                                                         0
   1:
                                                                                  1
                2
                                         1
                                                       0
                                                                 0
                                                                                  1
   2:
                           70
                                                                         0
   3:
                3
                           70
                                        1
                                                       0
                                                                 0
                                                                         0
                                                                                  1
                4
   4:
                           70
                                         1
                                                       0
                                                                 0
                                                                         0
                                                                                  1
                5
                           70
                                         1
                                                       0
                                                                 0
                                                                                  1
4688:
                                        0
                                                                 0
              65
                          137
                                                       1
                                                                         0
                                                                                  1
                                        0
                                                                                  1
4689:
               66
                          137
                                                       1
                                                                 0
                                                                         0
4690:
               67
                          137
                                        0
                                                       1
                                                                 0
                                                                         0
                                                                                  1
4691:
               68
                          137
                                        0
                                                                 0
                                                                         0
                                                                                  1
                                                       1
4692:
               69
                          137
                                        0
                                                       1
                                                                 0
                                                                         0
                                                                                  1
```

Each line corresponds to different comparison between a pair from the control arm and the treatment arm. The column strata store to which strata the pair belongs (first, second, ...). The columns favorable, unfavorable, neutral, uninformative contains the result of the comparison, e.g. the first pair was classified as favorable while the last was classified as favorable with a weight of 1. The second and third columns indicates the rows in the original dataset corresponding to the pair:

```
veteran[c(70,1),]
```

```
id trt celltype time status karno diagtime age prior 70 70 Exp squamous 999 1 90 12 54 10 1 1 Pl squamous 72 1 60 7 69 0
```

For the first pair, the event was observed for both observations and since 999 > 72 + 20 the pair is rated favorable. Substracting the average probability of the pair being favorable minus the average probability of the pair being unfavorable:

```
getPairScore(BT.keep, endpoint = 1)[, mean(favorable) - mean(unfavorable)]
```

[1] -0.08765836

gives the net treatment benefit in favor of the treatment for the first endpoint:

```
BT.keep
```

```
endpoint threshold delta Delta
time 20 -0.0877 -0.0877
karno -0.0133 -0.1009
```

More examples and explanation can be found in the documentation of the method getPairScore.

2.2 Extracting the survival probabilities

When using scoring.rule equals "Peron", survival probabilities at event time, and event times +/threshold in the control and treatment arms are used to score the pair. Setting keep.survival to TRUE
and precompute to FALSE in BuyseTest.options enables to export the survival probabilities in the output
of BuyseTest:

```
BuyseTest.options(keep.survival = TRUE, precompute = FALSE)

BT.keep2 <- BuyseTest(trt ~ tte(time, threshold = 20, status = "status") + cont(karno),

data = veteran, keep.pairScore = TRUE, scoring.rule = "Peron",

trace = 0, method.inference = "none")
```

The method getSurvival can then be used to extract these survival probabilities. For instance the following code extracts the survival for the first endpoint:

```
outSurv <- getSurvival(BT.keep2, endpoint = 1, strata = 1)
str(outSurv)</pre>
```

```
List of 5

$ survTimeC: num [1:69, 1:13] 72 411 228 126 118 10 82 110 314 100 ...
..- attr(*, "dimnames")=List of 2
....$: NULL
....$: chr [1:13] "time" "survivalC-threshold" "survivalC_0" "survivalC+threshold" ...
$ survTimeT: num [1:68, 1:13] 999 112 87 231 242 991 111 1 587 389 ...
..- attr(*, "dimnames")=List of 2
....$: NULL
....$: chr [1:13] "time" "survivalC-threshold" "survivalC_0" "survivalC+threshold" ...
$ survJumpC: num [1:57, 1:6] 3 4 7 8 10 11 12 13 16 18 ...
..- attr(*, "dimnames")=List of 2
....$: NULL
....$: chr [1:6] "time" "survival" "dSurvival" "index.survival" ...
```

```
$ survJumpT: num [1:51, 1:6] 1 2 7 8 13 15 18 19 20 21 ...
..- attr(*, "dimnames")=List of 2
....$ : NULL
....$ : chr [1:6] "time" "survival" "dSurvival" "index.survival" ...
$ lastSurv : num [1:2] 0 0
```

2.2.1 Computation of the score with only one censored event

Let's look at pair 91:

```
getPairScore(BT.keep2, endpoint = 1, rm.withinStrata = FALSE)[91]
```

In the dataset this corresponds to:

```
veteran[c(22,71),]
```

```
id trt celltype time status karno diagtime age prior 22 22 Pl smallcell 97 0 60 5 67 0 71 71 Exp squamous 112 1 80 6 60 0
```

The observation from the control group is censored at 97 while the observation from the treatment group has an event at 112. Since the threshold is 20, and (112-20)<97, we know that the pair is not in favor of the treatment. The formula for probability in favor of the control is $\frac{S_c(97)}{S_c(112+20)}$. The survival at the event time in the censoring group is stored in survTimeC. Since observation 22 is the 22th observation in the control group:

```
iSurv <- outSurv$survTimeC[22,]
iSurv</pre>
```

```
time
                                 survivalC-threshold
                                                                    survivalC_0
               97.000000
                                           0.5615232
                                                                      0.5171924
      survivalC+threshold
                                 survivalT-threshold
                                                                    survivalT_0
                0.4235463
                                           0.4558824
                                                                      0.3643277
      survivalT+threshold index.survivalC-threshold
                                                              index.survivalC_0
                                                                     28.0000000
                0.2827500
                                          25.0000000
index.survivalC+threshold index.survivalT-threshold
                                                              index.survivalT_0
                                          27.0000000
                                                                     32.0000000
               33.0000000
index.survivalT+threshold
               35.0000000
```

Since we are interested in the survival in the control arm exactly at the event time:

```
Sc97 <- iSurv["survivalC_0"]
Sc97
```

survivalC_0 0.5171924

The survival at the event time in the treatment group is stored in survTimeC. Since observation 71 is the 2nd observation in the treatment group:

```
iSurv <- outSurv$survTimeT[2,] ## survival at time 112+20
iSurv</pre>
```

survivalC_0	survivalC-threshold	time	
0.4549201	0.5319693	112.0000000	
survivalT_0	survivalT-threshold	survivalC+threshold	
0.2827500	0.3801681	0.3594915	
index.survivalC_0	$\verb"index.survivalC-threshold"$	survivalT+threshold	
32.0000000	27.0000000	0.2827500	
index.survivalT_0	$\verb"index.survivalT-threshold"$	<pre>index.survivalC+threshold</pre>	
35.0000000	31.0000000	37.0000000	
		index.survivalT+threshold	
		35.0000000	

Since we are interested in the survival in the control arm at the event time plus threshold:

```
Sc132 <- iSurv["survivalC+threshold"]
Sc132
```

```
survivalC+threshold 0.3594915
```

The probability in favor of the control is then:

```
Sc132/Sc97
```

```
survivalC+threshold
0.6950827
```

2.2.2 Computation of the score with two censored events

When both observations are censored, the formula for computing the probability in favor of treatment or control involves an integral. This integral can be computed using the function calcIntegralSurv_cpp that takes as argument a matrix containing the survival and the jumps in survival, e.g.:

```
head(outSurv$survJumpT)
```

time survival dSurvival index.survival index.dsurvival1 index.dsurvival2 [1,] 1 0.7681159 -0.02941176 12 [2,] 2 2 0.7536232 -0.01470588 13 1 [3,] 7 0.7388463 -0.02941176 14 2 3 [4,]8 0.7388463 -0.02941176 14 3 4 [5,] 13 0.7092924 -0.01470588 16 4 5 [6,]15 0.6945155 -0.02941176 17

and the starting time of the integration time. For instance, let's look at pair 148:

```
getPairScore(BT.keep2, endpoint = 1, rm.withinStrata = FALSE)[148]
```

Key: <index.Exp, index.Pl>
 index.Pl index.Exp indexWithinStrata.Pl indexWithinStrata.Exp favorable unfavorable
1: 10 72 10 3 0.5058685 0.3770426
 neutral uninf weight
1: 0.1170889 0 1

which corresponds to the observations:

```
veteran[c(10,72),]
```

id trt celltype time status karno diagtime age prior
10 10 Pl squamous 100 0 70 6 70 0
72 72 Exp squamous 87 0 80 3 48 0

The probability in favor of the treatment (p_F) and control (p_{UF}) can be computed as:

$$p_{F} = -\frac{1}{S_{T}(x)S_{C}(y)} \int_{t>y} S_{T}(t+\tau)dS_{C}(t)$$

$$p_{UF} = -\frac{1}{S_{T}(x)S_{C}(y)} \int_{t>x} S_{C}(t+\tau)dS_{T}(t)$$

where x = 87 and y = 100. To ease the call of calcIntegralScore_cpp we create a warper:

and then call it to compute the probabilities:

```
favorable unfavorable lowerBound 0.5058685 0.3770426 upperBound 0.5058685 0.3770426
```

Note: the lower bound is identical to the upper bound as we could estimate the full survival curve:

outSurv\$lastSurv

[1] 0 0

3 Dealing with missing values or/and right censoring

In presence of censoring or missing values, it is often not be possible to classify all pairs without a model for the censoring mechanism. The unclassified pairs, called uninformative, have a score of 0 which will typically bias the estimate of the net net treatment benefit towards 0 ⁵. Consider the following dataset:

```
id treatment eventtimeUncensored eventtime status toxicity eta_toxicity status1
               \mathsf{C}
                             0.2135567 0.2135567
                                                                      -0.07945702
1:
   1
                                                         1
                                                                 yes
                                                                                          1
               C
                             0.3422379 0.3422379
2:
    2
                                                                       1.18175155
                                                                                          1
                                                         1
                                                                 no
3:
    3
               C
                             1.3933222 1.3933222
                                                                       2.18614406
                                                                                          1
                                                         1
                                                                 no
    4
               \mathsf{C}
                             0.6737702 0.1961599
                                                         0
                                                                       0.40617493
4:
                                                                 no
                                                                                          1
               C
                             0.5642992 0.5642992
    5
5:
                                                         1
                                                                 yes -0.73835910
                                                                                          1
               C
                             1.1039218 0.1764950
6:
    6
                                                         0
                                                                      -1.95648670
                                                                                          1
                                                                 yes
```

where we have the uncensored event times (eventtimeUncensored) as well as the censored event times (eventtime). The percentage of censored observations is:

```
100*dt[,mean(status==0)]
```

[1] 44

We would like to be able to recover the net treatment benefit estimated with the uncensored event times:

```
BuyseTest(treatment ~ tte(eventtimeUncensored, status1, threshold = 0.5),
data = dt,
scoring.rule = "Gehan", method.inference = "none", trace = 0)
```

```
eventtimeUncensored 0.5 -0.271
```

using the censored survival times.

⁵While the power is typically reduced, the type 1 error will still be controlled if censoring is at random

The BuyseTest function handles missing values via two arguments:

- scoring.rule indicates how pairs involving missing data are compared.
 - the Gehan's scoring rule compares the observed values. If it is not possible to decide whether one observation has a better endpoint than the other (e.g. because both are right-censoring) then the paired is scored uninformative.
 - the Peron's scoring rule compares the probability of one observation having a better endpoint
 than the other given the observed values. This require a model for the censoring distribution.
 If the full survival curve can be identified then all pairs can be fully classified otherwise some
 of the pair will be partially uninformative.
 - the Efron's scoring rule same as the Peron's scoring rule except that the survival curve is extrapolated to 0 when its tail is unknown. Only relevant when using a (stratified) Kaplan-Meier estimator and no competing risks.
- correction.uninf indicates what to do with the uninformative scores. For instance setting this argument to TRUE will re-distribute this score to favorable/unfavorable/neutral scores.

The Peron's scoring rule is the default (and recommanded) approach. It uses a Kaplan Meier estimator stratified on treatment and GPC strata variable (if any) as survival model. When the last observation is censored, then part of the survival curve is unknown which can be necessary to score some of the pairs (especially in presence of a threshold of clinical relevance). One can:

- use a restriction time within the time interval where the survival curve can be estimated for each group.
- still use the default Peron's scoring rule: this will lead to uninformative pairs which can be reclassified based on a lower priority endpoint.
- use the Peron's scoring rule with another survival model, using parametric assumptions to inform about the unknown part of the survival curve. This can be achieved via the model.tte argument or using the Efron's scoring rule.
- use an add-hoc correction for the uninformative pairs (correction.uninf)

The first two solutions lead to a change of estimand, the first being much more clearly defined than the second. The last two solutions correspond to make statistical assumptions, the former assumptions being more explicit than with the later solution.

3.1 Gehan's scoring rule

In the example, Gehan's scoring rule:

leads to many uninformative pairs (about 60%) and an estimate much closer to 0 than the truth.

3.2 Peron's scoring rule

In the example, Peron's scoring rule:

```
endpoint threshold total favorable unfavorable neutral uninf Delta lower.ci

1 eventtime 0.5 100 11.1737 43.33707 44.12373 1.365504 -0.3216337 -0.4584262
upper.ci p.value

1 -0.1699543 5.385074e-05
```

leads to no uninformative pairs. Indeed the last observation in each group is an (uncensored) event:

```
dt[,.SD[which.max(eventtime)],by="treatment"]
```

so the full survival curve could be identified. As a result the estimate is very close to the truth.

<u>Note 1:</u> the censoring model can be specified by first fitting a survival model (prodlim or survreg) for the survival time:

```
library(prodlim) e.prodlim <- prodlim(Hist(eventtime, status) \sim treatment, data = dt)
```

Then passing the model to the BuyseTest via the model.tte argument:

When the dataset used to fit the survival model match the one used to run the GPC procedure, the overall uncertainty will be computed. Otherwise:

Uncertainty related to the estimation of the survival probabilities is ignored.

Consider adding an attribute "iidNuisance" to the argument 'model.tte' taking value TRUE to change endpoint threshold total favorable unfavorable neutral uninf Delta lower.ci

1 eventtime 0.5 100 11.1737 43.33707 44.12373 1.365504 -0.3216337 -0.4187087 upper.ci p.value

1 -0.2172912 6.570106e-09

the survival probabilities will assumed to be known with infinite precision and only the uncertainty of the GPC procedure will be considered. Add-hoc modification of the data can be used to obtain 'conservative' estimates when considering a single endpoint, e.g.:

Note 2: it is possible to use a parametric model via the survreg function:

Then passing the model to the BuyseTest via the model.tte argument:

```
endpoint threshold total favorable unfavorable neutral uninf Delta lower.ci

1 eventtime 0.5 100 11.65444 34.18937 54.14472 0.01147085 -0.2253494 -0.3476693
    upper.ci p.value

1 -0.09548719 0.0007624659
```

Internally the survival curve is discretized using 1000 points starting from survival = 1 to survival = 0.001 (this is why there is a non-0 but small percentage of uninformative pairs). This is performed internally by applying the BuyseTTEM method. Another discretisation can be obtained by calling BuyseTTEM with another value for the n.grid argument:

```
e.TTEM <- BuyseTTEM(e.survreg, treatment = "treatment", iid = TRUE, n.grid = 2500)
str(e.TTEM$peron$jumpSurvHaz[[1]][[1]])
```

```
$ time.jump : num    0 0.000307 0.000632 0.000964 0.001301 ...
$ survival : num    1 1 0.999 0.998 ...
and then passing to BuyseTest:
e.P4 <- BuyseTest(treatment ~ tte(eventtime, status, threshold = 0.5),</pre>
```

2500 obs. of 3 variables:

It is therefore possible to extend the approach to other model by defining an appropriate BuyseTTEM method. Looking at the code use for defining BuyseTTEM.survreg can be helpful.

3.3 Correction via re-weighting

\$ index.jump: logi NA NA NA NA NA NA ...

'data.frame':

The weights of the non-informative pairs is redistributed to the informative pairs. This is only a good strategy when there are no neutral pairs or there are no lower priority endpoints. This gives an estimate much closer to the true net treatment benefit:

Generalized pairwise comparisons with 1 endpoint

```
- statistic : net treatment benefit (delta: endpoint specific, Delta: global)
- treatment groups: T (treatment) vs. C (control)
```

```
censored pairs : deterministic score or uninformative
uninformative pairs: no contribution, their weight is passed to the informative pairs using IPCW
results
```

```
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) Delta eventtime 0.5 100 11.82 36.43 51.75 0 -0.2461
```

We can also see that no pair is finally classified as non informative. To get some inside about the correction we can look at the scores of the pairs:

```
iScore <- getPairScore(BT, endpoint = 1)
```

To get a synthetic view, we only look at the unique favorable/unfavorable/neutral/uniformative results:

```
favorable unfavorable neutral uninf favorableC unfavorableC neutralC uninfC
            0
                         0
                                                           0.000000 2.531646
                                  1
                                        0
                                             0.000000
1:
            0
                         1
                                        0
                                             0.000000
                                                           2.531646 0.000000
                                                                                    0
2:
3:
            0
                         0
                                  0
                                             0.000000
                                                           0.000000 0.000000
                                                                                    0
                                        1
                                  0
                                        0
                                             2.531646
                                                           0.000000 0.000000
                                                                                    0
            1
                         \cap
4:
```

We can see that the favorable/unfavorable/neutral pairs have seen their contribution multiplied by:

```
iScore[,1/mean(favorable + unfavorable + neutral)]
```

[1] 2.531646

i.e. the inverse probability of being informative.

3.4 Correction at the pair level

Another possible correction is to distribute the non-informative weight of a pair to the average favor-able/unfavorable/neutral probability observed on the sample:

Generalized pairwise comparisons with 1 endpoint

```
- statistic : net treatment benefit (delta: endpoint specific, Delta: global)
- treatment groups: T (treatment) vs. C (control)
- censored pairs : deterministic score or uninformative
- uninformative pairs: score equals the averaged score of all informative pairs
- results
- endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) Delta
eventtime 0.5 100 11.82 36.43 51.75 0 -0.2461
```

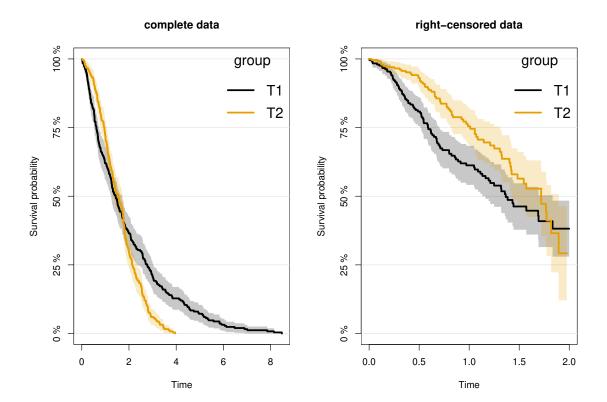
Looking at the scores of the pairs:

```
favorable unfavorable neutral uninf favorableC unfavorableC neutralC uninfC
                               1
                                     0.0000000
                                                     0.0000000 1.0000000
                       0
                                                                              0
1:
2:
           0
                       1
                               0
                                     0.0000000
                                                     1.0000000 0.0000000
                                                                              0
                                        0.1182278
           0
                       0
                                                     0.3643038 0.5174684
                                                                              0
3:
                               0
                                     1
                                        1.0000000
                                                     0.0000000 0.0000000
                                                                              0
4:
           1
                       0
                               0
                                     0
```

we can see that the corrected probability have not changed for the informative pairs, but for the non-informative they have been set to:

3.5 Note on the use of the corrections

As mentioned in Péron et al. (2021), the corrections (at the pair level or IPCW) are assumes that uninformative pairs would on average behave like informative pairs. This is typically the case under the proportional hazard assumption. However that may not be the case with other distributions, e.g.:



Here the net treatment benefit that we would have estimated with complete data:

```
BuyseTest.options(method.inference = "none")
e.ref <- BuyseTest(group ~ tte(time,status), data = df, trace = FALSE)
s.ref <- model.tables(e.ref, column = c("favorable","unfavorable","neutral","uninf","Delta"))
s.ref</pre>
```

```
favorable unfavorable neutral uninf Delta 1 50.2048 49.7952 0 0 0.004096
```

can be taken as a reference. Violation of the assumption will in this example have a substantial impact and lead to a worse estimate with the correction:

```
e.correction <- BuyseTest(group ~ tte(timeC,statusC), data = df, trace = FALSE, correction.
    uninf = TRUE)
s.correction <- model.tables(e.correction, column = c("favorable","unfavorable","neutral","
    uninf","Delta"))</pre>
```

Warning message:

```
In .BuyseTest(envir = envirBT, iid = outArgs$iid, method.inference = "none", :
   Some of the survival curves for endpoint(s) "timeC" are unknown beyond a survival of 0.25.
The correction of uninformative pairs assume that uninformative pairs would on average behave like
This can be a strong assumption and have substantial impact when the tail of the survival curve is
```

than without:

```
e.Peron <- BuyseTest(group ~ tte(timeC,statusC), data = df, trace = FALSE)
s.Peron <- model.tables(e.Peron, column = c("favorable","unfavorable","neutral","uninf","Delta
    "))
rbind("reference" = s.ref,
    "no correction" = s.Peron,
    "correction" = s.correction)</pre>
```

favorable unfavorable neutral uninf Delta reference 50.20480 49.79520 0 0.00000 0.00409600 no correction 49.09253 39.74775 0 11.15972 0.09344778 correction 55.25931 44.74069 0 0.00000 0.10518628

4 Simulating data using simBuyseTest

You can simulate data with the simBuyseTest function. For instance the following code simulates data for 5 individuals in the treatment arm and 5 individuals in the control arm:

```
set.seed(10)
simBuyseTest(n.T = 5, n.C = 5)
```

```
id treatment eventtime status toxicity
                                                    score
               C 0.60539304
1:
    1
                                  0
                                          yes -1.85374045
               C 0.31328027
2:
    2
                                  1
                                          yes -0.07794607
               C 0.03946623
3:
    3
                                  0
                                          yes 0.96856634
                                          yes 0.18492596
    4
               C 0.32147489
4:
                                  1
               C 1.57044952
    5
                                  0
                                          yes -1.37994358
5:
               T 0.29069131
     6
                                  0
                                              1.10177950
    7
               T 0.19522131
                                              0.75578151
7:
                                  0
                                          yes
               T 0.04640668
                                          yes -0.23823356
    8
                                  0
8:
               T 0.05277335
     9
                                  1
                                              0.98744470
9:
10: 10
               T 0.43062009
                                          yes 0.74139013
```

By default a categorical, continuous and time to event outcome are generated independently. You can modify their distribution via the arguments argsBin, argsCont, argsTTE. For instance the following code simulates two continuous variables with mean 5 in the treatment arm and 10 in the control arm all with variance 1:

```
id treatment eventtime status toxicity tumorSize
                                                           score
               C 0.1805891
                                 0
                                        yes 11.086551
                                                       8.564486
     1
 1:
     2
               C 0.1702538
 2:
                                 1
                                             9.237455 10.362087
               C 0.2621793
     3
                                 1
                                             9.171337 8.240913
 3:
               C 0.2959301
     4
                                 0
                                         no 10.834474 9.675456
 4:
     5
               C 0.4816549
                                             9.032348
                                                       9.348437
                                 1
               T 0.6446131
                                             5.089347
                                                        6.101780
 6:
     6
                                 1
                                         no
 7:
    7
               T 0.7372264
                                        yes 4.045056
                                                       5.755782
                                 1
               T 0.7213402
     8
                                 0
                                             4.804850
                                                        4.761766
 8:
                                        yes
 9:
     9
               T 0.1580651
                                 1
                                             5.925521
                                                        5.987445
                                        yes
10: 10
               T 0.2212117
                                 0
                                        yes 5.482979
                                                        5.741390
```

This functionality is based on the sim function of the lava package.

5 Power calculation using powerBuyseTest

The function powerBuyseTest can be used to perform power calculation, i.e., estimate the probability of rejecting a null hypothesis under a specific generative mechanism. The user therefore need to specify:

- the generative mechanism via a function argument sim
- the null hypothesis argument null
- the sample size(s) for the which the power should be computed argument sample.size

Consider the following generative mechanism where the outcome follows a Student's t-distribution in the treatment and control group, with same variance and degrees of freedom but different mean:

```
Y group
     0.02241932
                      0
  2: -1.07273566
      0.76072274
                      0
  4: -0.25812356
                      0
      0.97207866
                      0
      1.82349375
198:
199: -0.98560076
200:
      1.48143637
201: 3.69314316
                      1
202:
      0.96244416
                      1
```

We then define the null hypothesis:

```
null <- c("netBenefit" = 0)</pre>
```

Naming the value is important since that will indicate which statistic should be used (here the net treatment benefit). We can assess the power of a test based on the net treatment benefit using the following syntax:

```
summary(powerW)
```

Simulation study with Generalized pairwise comparison with 1000 samples $\,$

```
- net benefit statistic (null hypothesis Delta=0)
endpoint threshold n.T n.C mean.estimate sd.estimate mean.se rejection.rate
      Y
             1e-12
                    5
                                  0.2484
                                               0.359 0.3395
                        5
                                                                      0.069
                    10 10
                                  0.2471
                                              0.2551 0.2464
                                                                      0.137
                                              0.1746 0.1757
                    20 20
                                  0.2444
                                                                      0.221
                                              0.1436 0.1437
                    30 30
                                  0.243
                                                                      0.365
                    50 50
                                  0.2438
                                              0.1114 0.1113
                                                                      0.557
                   100 100
                                  0.2458
                                              0.0804 0.0787
                                                                      0.865
```

```
n.T : number of observations in the treatment group

n.C : number of observations in the control group

mean.estimate: average estimate over simulations

sd.estimate : standard deviation of the estimate over simulations

mean.se : average estimated standard error of the estimate over simulations

rejection : frequency of the rejection of the null hypothesis over simulations

(standard error: H-projection of order 1| p-value: after transformation)
```

It is also possibly to use an asymptotic approximation to derive a approximate sample size satisfying a specific type 1 and type 2 error rate:

This procedure is inspired from the procedure presented by Brunner et al. (2018) in section 3.8.2.2. In short, several 'large' datasets are generated and analyzed using GPC to approximate the statistic of interest (Δ) and its asymptotic variance (σ^2). The sample size needed to achieve the requested power $(1-\beta)$ and the requested type 1 error (α) is then deduce, give a dataset, according to the equation $N = \sigma^2 \frac{\left(u_{1-\alpha/2} + u_{1-\beta}\right)^2}{\Delta^2}$ where u_x denotes the x-quantile of the normal distribution. The estimated sample size is then the average calculated sample size across dataset. The argument max.sample.size specifies the number of observation per group in the 'large' dataset (here 1000 per group) and the second element of the argument n.rep specifies the number of datasets (here 10). The quality of the approximation, as well as the computation time, thus improves when increasing max.sample.size and n.rep[2]. The achieved power with the estimated sample size can be output as usual using the summary method:

```
summary(nW)
```

```
Sample size calculation with Generalized pairwise comparison for a power of 0.8 and type 1 error rate of 0.05
```

- estimated sample size (mean [min;max]): 89 [60;145] controls 89 [60;145] treated

- net benefit statistic (null hypothesis Delta=0)

endpoint threshold n.T n.C mean.estimate sd.estimate mean.se rejection.rate Y 1e-12 89 89 0.2452 0.0854 0.0834 0.806

n.T : number of observations in the treatment groupn.C : number of observations in the control group

mean.estimate: average estimate over simulations

sd.estimate : standard deviation of the estimate over simulations

mean.se : average estimated standard error of the estimate over simulations rejection : frequency of the rejection of the null hypothesis over simulations

(standard error: H-projection of order 1| p-value: after transformation)

6 Modifying default options

The BuyseTest.options method enable to get and set the default options of the BuyseTest function. For instance, the default option for trace is:

```
BuyseTest.options("trace")
```

\$trace

[1] 2

To change the default option to 0 (i.e. no output) use:

```
BuyseTest.options(trace = 0)
```

To change what the results output by the summary function use:

Generalized pairwise comparisons with 1 endpoint

To restore the original default options do:

```
BuyseTest.options(reinitialise = TRUE)
```

References

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