

Package ‘Delta’

July 21, 2025

Title Measure of Agreement Between Two Raters

Version 0.2.0.3

Author Antonio Rodriguez [aut, cre],
Pedro Femia [cph, ctb],
Antonio Martin [cph, ctb]

Maintainer Antonio Rodriguez <tonirodriguezcontesti@gmail.com>

Description Measure of agreement delta was originally by Martín & Femia (2004) <[DOI:10.1348/000711004849268](https://doi.org/10.1348/000711004849268)>. Since then has been considered as agreement measure for different fields, since their behavior is usually better than the usual kappa index by Cohen (1960) <[DOI:10.1177/001316446002000104](https://doi.org/10.1177/001316446002000104)>. The main issue with delta is that can not be computed by hand contrary to kappa. The current algorithm is based on the Version 5 of the delta windows program that can be found on <<https://www.ugr.es/~bioest/software/delta/cmd.php?seccion=downloads>>.

Depends R (>= 3.2.0)

Imports stats

License GPL-3

Encoding UTF-8

LazyData true

RoxygenNote 6.1.0

NeedsCompilation no

Repository CRAN

Date/Publication 2019-12-09 07:30:02 UTC

Contents

CheckInput	2
CheckInputData	3
CheckSampling	3
Delta	4
GetAsinDeltaParams	5

GetB	6
GetCovariance	6
GetDeltaParams	7
GetDeltaParamsVar	7
GetDeltaPi	8
GetDeltaProblemType	9
GetGoodness	9
GetKappa	10
GetKappaProblemType	11
GetM1	11
GetMx	12

Index	13
--------------	-----------

CheckInput	<i>Main Check Input function</i>
------------	----------------------------------

Description

This function perform multiple tasks. First of all, check the parameters specified by the user. Also assign default values to some parameters not defined by the user. Finally it generates error messages and halt the execution in case it is needed.

Usage

```
CheckInput(datatable, fixedrows = FALSE, gstandard = "No",
           maxits = 1000, tol = 1e-12, dplaces = 4, showall = FALSE)
```

Arguments

datatable	Matrix. Expected to be square matrix with at least 2 rows (columns), non negative values and at least an element different of zero.
fixedrows	Boolean. Indicate if sample rows are fixed beforehand. Default is TRUE.
gstandard	Text. Indicate if there are a Gold Standard by Rows or columns. Only first letter matter without Case sensitivity. Options are: "N" for None, "R" for in Rows and "C" for in Columns. Default is "N".
maxits	Whole number. Indicate the maximum number of iterations of the numeric method to calculate B. Expected to be $100 \leq \text{maxits} \leq 5000$. Default is 1000.
tol	Double number. Indicate the precision of the numeric method to calculate B. Expected to be $1e-6 \leq \text{tol} \leq 1e-15$. Default is $1e-12$.
dplaces	Whole number. Decimal placed to be shown in the result. Expected to be $1 \leq \text{dplaces} < 6$. Default 4.
showall	Boolean. Indicate if all output should be shown. If TRUE also shown hidden results. If FALSE shown only main output. By default is FALSE.

Examples

```
CheckInput(matrix(c(1,2,3,4),2,2),fixedrows=FALSE,gstandard="No",maxits=100,tol=1e-12,dplaces=4)
```

CheckInputData	<i>Check Input Matrix function</i>
----------------	------------------------------------

Description

This function checks that matrix introduced is as expected. Should be a matrix, squared, with a dimension greater or equal to two, without negative entries and at least an entry different of 0.

Usage

```
CheckInputData(datatable)
```

Arguments

datatable	Matrix. Expected to be square matrix with at least 2 rows (columns), non negative values and at least an element different of zero.
-----------	---

Examples

```
CheckInputData(matrix(c(1,2,3,4),2,2))
```

CheckSampling	<i>Check Sampling type function</i>
---------------	-------------------------------------

Description

This function checks that fixedrows and gstandard parameters are correct. Also return a value indicating if it is or not valid and what kind of output should be shown at the end of the execution.

Usage

```
CheckSampling(fixedrows, gstandard)
```

Arguments

fixedrows	Boolean. Indicate if sample rows are fixed beforehand. Default is TRUE.
gstandard	Text. Indicate if there are a Gold Standard by Rows or columns. Only first letter matter without Case sensitivity. Options are: "N" for None, "R" for in Rows and "C" for in Columns. Default is "N".

Examples

```
CheckSampling(TRUE,"rows")
CheckSampling(TRUE,"Columns")
```

Delta	<i>Delta coefficient function</i>
-------	-----------------------------------

Description

This function provides an analysis of the matrix provided, returning all the parameters estimations and SE calculations that have sense with the fixedrows and gstandard provided.

Usage

```
Delta(datatable, fixedrows = FALSE, gstandard = "No", maxits = 1000,
      tol = 1e-12, dplaces = 4, showall = FALSE)
```

```
## S3 method for class 'Delta'
print(x, ...)
```

```
## S3 method for class 'Delta'
summary(object, ...)
```

Arguments

datatable	Matrix. Expected to be square matrix with at least 2 rows (columns), non negative values and at least an element different of zero.
fixedrows	Boolean. Indicate if sample rows are fixed beforehand. Default is TRUE.
gstandard	Text. Indicate if there are a Gold Standard by Rows or columns. Only first letter matter without Case sensitivity. Options are: "N" for None, "R" for in Rows and "C" for in Columns. Default is "N".
maxits	Whole number. Indicate the maximum number of iterations of the numeric method to calculate B. Expected to be $100 \leq \text{maxits} \leq 5000$. Default is 1000.
tol	Double number. Indicate the precision of the numeric method to calculate B. Expected to be $1e-6 \leq \text{tol} \leq 1e-15$. Default is $1e-12$.
dplaces	Whole number. Decimal placed to be shown in the result. Expected to be $1 \leq \text{dplaces} < 6$. Default 4.
showall	Boolean. Indicate if all output should be shown. If TRUE also shown hidden results. If FALSE shown only main output. By default is FALSE.
x	List produced by Delta
...	Other print options
object	List produced by Delta

Details

This function study the matrix provided by the user. This function modify the matrix deleting missing rows and columns and if it is needed for the estimation, adding 0.5 to each cell.

Also calculate Cohen's Kappa coefficient and the goodness of fit for the Delta model.

Value

NULL
NULL

Examples

```
Delta(matrix(c(1,2,3,4),2,2))  
Delta(matrix(c(65,5,10,20),2,2),fixedrows=TRUE,gstandard="Row")
```

GetAsinDeltaParams	<i>Calculate Asintotic Delta related parameters function</i>
--------------------	--

Description

This function perform all needed calculations to get all Delta related parameters, for a 2x2 matrix.
All calculations are asintotics.

Usage

```
GetAsinDeltaParams(mx, fixedrows = TRUE)  
  
## S3 method for class 'GetAsinDeltaParams'  
print(x, ...)
```

Arguments

- mx Matrix. Agreement contingency table to perform calculations
- fixedrows Boolean. Indicate if sample rows are fixed beforehand.
- x List produced by GetAsinDeltaParams
- ... Other print options

Value

NULL

Examples

```
GetAsinDeltaParams(matrix(c(60,10,10,20),2,2),TRUE)
```

GetB	<i>Calculate B function</i>
------	-----------------------------

Description

This function solve numerically the non lineal inequation of the Delta system. Also return the s(i) values of the equation.

Usage

```
GetB(mx, tol = 1e-12, maxits = 1000)
```

Arguments

mx	Matrix. Modified matrix to have a solution. Usually GetMx\$M1 for k>2 and GetMx\$M2 in case of k = 2.
tol	Double number. Indicate the precision of the numeric method to calculate B. Expected to be $1e-6 \leq \text{tol} \leq 1e-15$. Default is 1e-12.
maxits	Whole number. Indicate the maximum number of iterations of the numeric method to calculate B. Expected to be $100 \leq \text{maxits} \leq 5000$. Default is 1000.

Examples

```
GetB(mx = matrix(c(1,0,0,0,2,0,0,0,3),3,3),tol = 1e-12, maxits = 1000)
GetB(mx = matrix(c(1,2,0,3,4,0,0,0,1),3,3),tol = 1e-12, maxits = 1000)
```

GetCovariance	<i>Calculate Covariance function</i>
---------------	--------------------------------------

Description

This function calculate covariance for combinations Cov(Delta,Delta), Cov(Delta,Pi) and Cov(Pi,Pi).

Usage

```
GetCovariance(mx, Delta, Pi, B)
```

Arguments

mx	Matrix. Modified matrix to have a solution. Usually GetMx\$M1 for k>2 and GetMx\$M2 in case of k = 2.
Delta	Vector. Each element indicate the probability of recognize an element i.
Pi	Vector. Each element indicate the probability of classify at random an element in category i.
B	Double. Numerical solution to the equation given by the model.

Examples

```
GetCovariance(mx = matrix(c(1.5,0.5,0.5,0.5,2.5,0.5,0.5,0.5,3.5),3,3),
  Delta = c(0.4,0.5714286,0.666667),
  Pi = c(0.3333,0.333333,0.33333),B = 4.5)
GetCovariance(mx = matrix(c(60,0,3,2,50,1,3,2,79),3,3),
  Delta = c( 0.8945724, 0.9522836, 0.8962094),
  Pi = c( 0.2703707, 0.1939561, 0.5356732), B = 17.94867)
```

GetDeltaParams

*Calculate Delta related parameters function***Description**

This function perform all needed calculations to get all Delta related parameters. For do the exact calculations some variables previously calculated are needed.

Usage

```
GetDeltaParams(mx, Delta, Pi, k)
```

Arguments

mx	Matrix. Agreement contingency table to perform calculations
Delta	Vector. Each element indicate the probability of recognize an element i.
Pi	Vector. Each element indicate the probability of classify at random an element in category i.
k	Integer. Dimension of the problem.

Examples

```
GetDeltaParams(mx = matrix(c(60,0,3,2,50,1,3,2,79),3,3),
  Delta = c( 0.8945724, 0.9522836, 0.8962094),
  Pi = c( 0.2703707, 0.1939561, 0.5356732), k = 3)
```

GetDeltaParamsVar

*Calculate Delta related parameters variance function***Description**

This function perform all needed calculations to get all Delta related parameters variance. For do the exact calculations some variables previously calculated are needed.

Usage

```
GetDeltaParamsVar(mx, fixedrows = FALSE, Delta, Pi, k, Cov, E)
```

Arguments

mx	Matrix. Agreement contingency table to perform calculations
fixedrows	Boolean. Indicate if sample rows are fixed beforehand.
Delta	Vector. Each element indicate the probability of recognize an element i.
Pi	Vector. Each element indicate the probability of classify at random an element in category i.
k	Integer. Dimension of the problem.
Cov	Matrix. Covariance matrix of Delta.
E	Double. Value calculated for Cov matrix derivation.

Examples

```
GetDeltaParamsVar(mx = matrix(c(60,0,3,2,50,1,3,2,79),3,3),
fixedrows = FALSE,Delta = c( 0.8945724, 0.9522836, 0.8962094),
  Pi = c( 0.2703707, 0.1939561, 0.5356732), k = 3,
  Cov = matrix(c(0.002736490, 0.000004188, -0.001074704,
0.000004188, 0.001141059, -0.000181746,
-0.001074704, -0.000181746, 0.004912131),3,3),
  E = c(0.03159824, 0.01304313, -0.88650011))
```

GetDeltaPi

*Calculate Delta and Pi parameters function***Description**

This function provide an estimation of Pi and Delta for each category. To do so, it is needed to solve the non-linear equation of B, given by the function GetB.

Usage

```
GetDeltaPi(mx, dtp, tol = 1e-12, maxits = 1000, original.mx = TRUE)
```

Arguments

mx	Matrix. Modified matrix to have a solution. Usually GetMx\$M1 for $k > 2$ and GetMx\$M2 in case of $k = 2$.
dtp	String. Type of delta problem.
tol	Double number. Indicate the precision of the numeric method to calculate B. Expected to be $1e-6 \leq \text{tol} \leq 1e-15$. Default is $1e-12$.
maxits	Whole number. Indicate the maximum number of iterations of the numeric method to calculate B. Expected to be $100 \leq \text{maxits} \leq 5000$. Default is 1000.
original.mx	Boolean. Indicate if the dtp parameter correspond to the current mx parameter. By default TRUE.

Details

In some type of problems, the solution is on the borderline, and in those situation we may have not solutions at all, only one or infinity of them.

Examples

```
GetDeltaPi(mx = matrix(c(1,0,0,0,2,0,0,0,3),3,3), dtp = "DN0", tol = 1e-12, maxits = 1000)
GetDeltaPi(mx = matrix(c(1.5,2.5,0.5,3.5,4.5,0.5,0.5,0.5,1.5),3,3), dtp = "DN2",
  tol = 1e-12, maxits = 1000, original.mx = FALSE)
```

GetDeltaProblemType	<i>Get Delta problem type function</i>
---------------------	--

Description

This function apply Test to identify where are the solution located. We have mainly 3 situations for $k > 2$ and 2 for $k = 2$. For $k > 2$ we have: DN2 = No estimators in the boundary. DN1 = Some estimator in the boundary and global agreement imaginary. DN0 = Any other case For $k = 2$ we have: DA0 = Some estimator in the boundary. DA1 = Any other case

Usage

```
GetDeltaProblemType(Mx)
```

Arguments

Mx	Matrix. Matrix reduced.
----	-------------------------

Examples

```
GetDeltaProblemType(matrix(c(1,2,0,3,4,0,0,0,1),3,3))
GetDeltaProblemType(matrix(c(1,0,0,0,2,0,0,0,3),3,3))
```

GetGoodness	<i>Calculate Goodness of fit function</i>
-------------	---

Description

This function provide an Chi-square test for the given matrix, Delta and Pi provided.

Usage

```
GetGoodness(mx, Pi, Delta)

## S3 method for class 'GetGoodness'
print(x, ...)
```

Arguments

mx	Matrix. Modified matrix to have a solution. Usually GetMx\$M1 for $k > 2$ and GetMx\$M2 in case of $k = 2$.
Pi	Vector. Each element indicate the probability of classify at random an element in category i.
Delta	Vector. Each element indicate the probability of recognize an element i.
x	List produced by GetGoodness
...	Other print options

Value

NULL

Examples

```
GetGoodness(mx = matrix(c(1,0,0,0,2,0,0,0,3),3,3), Delta = c(1,1,1), Pi = NULL)
GetGoodness(mx = matrix(c(1.5,2.5,0.5,3.5,4.5,0.5,0.5,0.5,1.5),3,3),
             Delta = c(-0.2662395, 0.2047577, 0.5664672),
             Pi = c(0.42564365, 0.49700867, 0.07734769))
GetGoodness(mx = matrix(c(60,0,3,2,50,1,3,2,79),3,3),
             Delta = c(0.8945724, 0.9522836, 0.8962094),
             Pi = c(0.2703707, 0.1939561, 0.5356732))
```

GetKappa

Calculate Cohen's Kappa coefficient function

Description

This function perform Cohen's Kappa coefficient calculations. The function provide the Kappa coefficient and SE.

Usage

```
GetKappa(mx)

## S3 method for class 'GetKappa'
print(x, ...)
```

Arguments

mx	Matrix. Agreement contingency table to perform calculations
x	List produced by GetKappa
...	Other print options

Value

NULL

Examples

```
GetKappa(matrix(c(50,10,10,20),2,2))
```

GetKappaProblemType	<i>Get Kappa problem type function</i>
---------------------	--

Description

This function apply Test to identify where kappa solutions are placed K0 = Full agreement (diagonal matrix) K1 = Any other case

Usage

```
GetKappaProblemType(Mx)
```

Arguments

Mx	Matrix. Matrix reduced.
----	-------------------------

Examples

```
GetKappaProblemType(matrix(c(1,2,0,3,4,0,0,0,1),3,3))
GetKappaProblemType(matrix(c(1,0,0,0,2,0,0,0,3),3,3))
```

GetM1	<i>Get reduced matrix (M1) function</i>
-------	---

Description

This function reduce matrix provided by the user deleting missing categories, those j where $\text{sum}(\text{datatable}[j,]) = \text{sum}(\text{datatable}[,j]) = 0$. Also provide a list of the categories deleted and provides the new size of the problem

Usage

```
GetM1(datatable)

## S3 method for class 'GetM1'
print(x, ...)
```

Arguments

datatable	Matrix. Expected to be square matrix with at least 2 rows (columns), non negative values and at least an element different of zero.
x	List produced by GetM1
...	Other print options

Value

NULL

Examples

```
GetM1(matrix(c(1,2,0,3,4,0,0,0,0),3,3))
```

GetMx	<i>Get matrix of the problem (Mx) function</i>
-------	--

Description

This function produce 3 new auxiliar matrix. Those matrix are always defined, but depending of the problem they will be used or not. All the auxiliar matrices are created to be able to solve the problem and avoid issues with solutions in the boundary or not completly defined.

Usage

```
GetMx(M1)
```

Arguments

M1 Matrix. Initial matrix without missing categories.

Details

The matrix are defined as follows - M2: Extended M1 with \$c_33\$ of 1 and increased by 0.5 - M3: M1 increased by 0.5 - M4: M1 increased by 1
In case of M1 is not 2x2, M2 and M3 are the same matrix.

Examples

```
GetMx(matrix(c(1,2,0,3,4,0,0,0,1),3,3))
```

Index

- * **Asintotic**
 - GetAsinDeltaParams, 5
- * **B**
 - GetB, 6
 - GetCovariance, 6
 - GetDeltaParams, 7
 - GetDeltaParamsVar, 7
- * **Cohen**
 - GetKappa, 10
- * **Covariance**
 - GetCovariance, 6
- * **Cov**
 - GetDeltaParams, 7
 - GetDeltaParamsVar, 7
- * **Delta**
 - Delta, 4
 - GetAsinDeltaParams, 5
 - GetB, 6
 - GetCovariance, 6
 - GetDeltaParams, 7
 - GetDeltaParamsVar, 7
 - GetDeltaPi, 8
 - GetGoodness, 9
- * **Goodness**
 - GetGoodness, 9
- * **Kappa**
 - GetKappa, 10
- * **M1**
 - GetM1, 11
 - GetMx, 12
- * **Mx**
 - GetDeltaProblemType, 9
 - GetKappaProblemType, 11
 - GetMx, 12
- * **Pi**
 - GetCovariance, 6
 - GetDeltaParams, 7
 - GetDeltaParamsVar, 7
 - GetGoodness, 9
- * **check**
 - CheckInput, 2
 - CheckInputData, 3
 - CheckSampling, 3
- * **datatable**
 - CheckInput, 2
 - CheckInputData, 3
 - Delta, 4
 - GetM1, 11
- * **dplaces**
 - CheckInput, 2
 - Delta, 4
- * **dtp**
 - GetDeltaPi, 8
- * **fixedrows**
 - CheckInput, 2
 - CheckSampling, 3
 - Delta, 4
 - GetAsinDeltaParams, 5
 - GetDeltaParams, 7
 - GetDeltaParamsVar, 7
- * **gstandard**
 - CheckInput, 2
 - CheckSampling, 3
 - Delta, 4
- * **k**
 - GetCovariance, 6
 - GetDeltaParams, 7
 - GetDeltaParamsVar, 7
- * **maxits**
 - CheckInput, 2
 - Delta, 4
 - GetB, 6
 - GetDeltaPi, 8
- * **mx**
 - GetAsinDeltaParams, 5
 - GetB, 6
 - GetCovariance, 6
 - GetDeltaParams, 7

- GetDeltaParamsVar, 7
- GetDeltaPi, 8
- GetGoodness, 9
- GetKappa, 10
- * **original.mx**
 - GetDeltaPi, 8
- * **tol**
 - CheckInput, 2
 - Delta, 4
 - GetB, 6
 - GetDeltaPi, 8
- CheckInput, 2
- CheckInputData, 3
- CheckSampling, 3
- Delta, 4
- GetAsinDeltaParams, 5
- GetB, 6
- GetCovariance, 6
- GetDeltaParams, 7
- GetDeltaParamsVar, 7
- GetDeltaPi, 8
- GetDeltaProblemType, 9
- GetGoodness, 9
- GetKappa, 10
- GetKappaProblemType, 11
- GetM1, 11
- GetMx, 12
- print.Delta (Delta), 4
- print.GetAsinDeltaParams
 - (GetAsinDeltaParams), 5
- print.GetGoodness (GetGoodness), 9
- print.GetKappa (GetKappa), 10
- print.GetM1 (GetM1), 11
- summary.Delta (Delta), 4