

Package ‘KERE’

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Title Expectile Regression in Reproducing Kernel Hilbert Space

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Depends methods

Description An efficient algorithm inspired by majorization-minimization principle for solving the entire solution path of a flexible nonparametric expectile regression estimator constructed in a reproducing kernel Hilbert space.

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as.kernelMatrix	<i>Assing kernelMatrix class to matrix objects</i>
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Description

as.kernelMatrix in package **KERE** can be used to coerce the kernelMatrix class to matrix objects representing a kernel matrix. These matrices can then be used with the kernelMatrix interfaces which most of the functions in **KERE** support.

Usage

```
## S4 method for signature 'matrix'
as.kernelMatrix(x, center = FALSE)
```

Arguments

x	matrix to be assigned the kernelMatrix class
center	center the kernel matrix in feature space (default: FALSE)

Author(s)

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See Also

[kernelMatrix](#), [dots](#)

Examples

```
## Create toy data
x <- rbind(matrix(rnorm(10),,2),matrix(rnorm(10,mean=3),,2))
y <- matrix(c(rep(1,5),rep(-1,5)))

### Use as.kernelMatrix to label the cov. matrix as a kernel matrix
### which is eq. to using a linear kernel

K <- as.kernelMatrix(crossprod(t(x)))

K
```

cv.KERE

*Cross-validation for KERE***Description**

Does k-fold cross-validation for KERE, produces a plot, and returns a value for lambda.

Usage

```
## S3 method for class 'KERE'
cv(x, y, kern, lambda = NULL, nfolds = 5, foldid, omega = 0.5, ...)
```

Arguments

x	matrix of predictors, of dimension $N \times p$; each row is an observation vector.
y	response variable.
kern	the built-in kernel classes in KERE . The kern parameter can be set to any function, of class kernel, which computes the inner product in feature space between two vector arguments. KERE provides the most popular kernel functions which can be initialized by using the following functions: • rbfdot Radial Basis kernel function, • polydot Polynomial kernel function, • vanilladot Linear kernel function, • tanhdot Hyperbolic tangent kernel function, • laplacedot Laplacian kernel function, • besseldot Bessel kernel function, • anovadot ANOVA RBF kernel function, • splinedot the Spline kernel. Objects can be created by calling the rbfdot, polydot, tanhdot, vanilladot, anovadot, besseldot, laplacedot, splinedot functions etc. (see example.)
lambda	a user supplied lambda sequence. It is better to supply a decreasing sequence of lambda values, if not, the program will sort user-defined lambda sequence in decreasing order automatically.
nfolds	number of folds - default is 5. Although nfolds can be as large as the sample size (leave-one-out CV), it is not recommended for large datasets. Smallest value allowable is nfolds=3.
foldid	an optional vector of values between 1 and nfold identifying what fold each observation is in. If supplied, nfold can be missing.
omega	the parameter ω in the expectile regression model. The value must be in (0,1). Default is 0.5.
...	other arguments that can be passed to KERE.

Details

The function runs `KERE` `nfolds+1` times; the first to get the `lambda` sequence, and then the remainder to compute the fit with each of the folds omitted. The average error and standard deviation over the folds are computed.

Value

an object of class `cv.KERE` is returned, which is a list with the ingredients of the cross-validation fit.

<code>lambda</code>	the values of <code>lambda</code> used in the fits.
<code>cvm</code>	the mean cross-validated error - a vector of length <code>length(lambda)</code> .
<code>cvsd</code>	estimate of standard error of <code>cvm</code> .
<code>cvupper</code>	upper curve = <code>cvm+cvsd</code> .
<code>cvlo</code>	lower curve = <code>cvm-cvsd</code> .
<code>name</code>	a character string "Expectile Loss"
<code>lambda.min</code>	the optimal value of <code>lambda</code> that gives minimum cross validation error <code>cvm</code> .
<code>cvm.min</code>	the minimum cross validation error <code>cvm</code> .

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References

Y. Yang, T. Zhang, and H. Zou. "Flexible Expectile Regression in Reproducing Kernel Hilbert Space." ArXiv e-prints: stat.ME/1508.05987, August 2015.

Examples

```
N <- 200
X1 <- runif(N)
X2 <- 2*runif(N)
X3 <- 3*runif(N)
SNR <- 10 # signal-to-noise ratio
Y <- X1*1.5 + 2 * (X2*.5) + X1*X3
sigma <- sqrt(var(Y)/SNR)
Y <- Y + X2*rnorm(N,0,sigma)
X <- cbind(X1,X2,X3)

# set gaussian kernel
kern <- rbfdot(sigma=0.1)

# define lambda sequence
lambda <- exp(seq(log(0.5),log(0.01),len=10))

cv.KERE(x=X, y=Y, kern, lambda = lambda, nfolds = 5, omega = 0.5)
```

Description

The kernel generating functions provided in KERE.

The Gaussian RBF kernel $k(x, x') = \exp(-\sigma \|x - x'\|^2)$

The Polynomial kernel $k(x, x') = (scale < x, x' > + offset)^{degree}$

The Linear kernel $k(x, x') = < x, x' >$

The Hyperbolic tangent kernel $k(x, x') = \tanh(scale < x, x' > + offset)$

The Laplacian kernel $k(x, x') = \exp(-\sigma \|x - x'\|)$

The Bessel kernel $k(x, x') = (-Bessel_{(\nu+1)}^n \sigma \|x - x'\|^2)$

The ANOVA RBF kernel $k(x, x') = \sum_{1 \leq i_1 \dots < i_D \leq N} \prod_{d=1}^D k(x_{id}, x'_{id})$ where $k(x, x')$ is a Gaussian RBF kernel.

The Spline kernel $\prod_{d=1}^D 1 + x_i x_j + x_i x_j \min(x_i, x_j) - \frac{x_i + x_j}{2} \min(x_i, x_j)^2 + \frac{\min(x_i, x_j)^3}{3} \setminus$

Usage

```
rbfdot(sigma = 1)
```

```
polydot(degree = 1, scale = 1, offset = 1)
```

```
tanhdot(scale = 1, offset = 1)
```

```
vanilladot()
```

```
laplacedot(sigma = 1)
```

```
besseldot(sigma = 1, order = 1, degree = 1)
```

```
anovadot(sigma = 1, degree = 1)
```

```
splinedot()
```

Arguments

sigma	The inverse kernel width used by the Gaussian the Laplacian, the Bessel and the ANOVA kernel
degree	The degree of the polynomial, bessel or ANOVA kernel function. This has to be an positive integer.
scale	The scaling parameter of the polynomial and tangent kernel is a convenient way of normalizing patterns without the need to modify the data itself
offset	The offset used in a polynomial or hyperbolic tangent kernel
order	The order of the Bessel function to be used as a kernel

Details

The kernel generating functions are used to initialize a kernel function which calculates the dot (inner) product between two feature vectors in a Hilbert Space. These functions can be passed as a kernel argument on almost all functions in **KERE** (e.g., `ksvm`, `kpca` etc).

Although using one of the existing kernel functions as a kernel argument in various functions in **KERE** has the advantage that optimized code is used to calculate various kernel expressions, any other function implementing a dot product of class `kernel` can also be used as a kernel argument. This allows the user to use, test and develop special kernels for a given data set or algorithm.

Value

Return an S4 object of class `kernel` which extends the function class. The resulting function implements the given kernel calculating the inner (dot) product between two vectors.

`kpar` a list containing the kernel parameters (hyperparameters) used.

The kernel parameters can be accessed by the `kpar` function.

Note

If the offset in the Polynomial kernel is set to 0, we obtain homogeneous polynomial kernels, for positive values, we have inhomogeneous kernels. Note that for negative values the kernel does not satisfy Mercer's condition and thus the optimizers may fail.

In the Hyperbolic tangent kernel if the offset is negative the likelihood of obtaining a kernel matrix that is not positive definite is much higher (since then even some diagonal elements may be negative), hence if this kernel has to be used, the offset should always be positive. Note, however, that this is no guarantee that the kernel will be positive.

Author(s)

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See Also

[kernelMatrix](#), [kernelMult](#), [kernelPol](#)

Examples

```
rbfkernel <- rbfdot(sigma = 0.1)
rbfkernel

kpar(rbfkernel)

## create two vectors
x <- rnorm(10)
y <- rnorm(10)

## calculate dot product
```

```
rbfkernel(x,y)
```

KERE

Fits the regularization paths for the kernel expectile regression.

Description

Fits a regularization path for the kernel expectile regression at a sequence of regularization parameters `lambda`.

Usage

```
KERE(x, y, kern, lambda = NULL, eps = 1e-08, maxit = 1e4,
      omega = 0.5, gamma = 1e-06, option = c("fast", "normal"))
```

Arguments

<code>x</code>	matrix of predictors, of dimension $N \times p$; each row is an observation vector.
<code>y</code>	response variable.
<code>kern</code>	the built-in kernel classes in KERE. The <code>kern</code> parameter can be set to any function, of class <code>kernel</code>, which computes the inner product in feature space between two vector arguments. KERE provides the most popular kernel functions which can be initialized by using the following functions: • <code>rbfdot</code> Radial Basis kernel function, • <code>polydot</code> Polynomial kernel function, • <code>vanilladot</code> Linear kernel function, • <code>tanhdot</code> Hyperbolic tangent kernel function, • <code>laplacedot</code> Laplacian kernel function, • <code>besseldot</code> Bessel kernel function, • <code>anovadot</code> ANOVA RBF kernel function, • <code>splinedot</code> the Spline kernel. Objects can be created by calling the <code>rbfdot</code>, <code>polydot</code>, <code>tanhdot</code>, <code>vanilladot</code>, <code>anovadot</code>, <code>besseldot</code>, <code>laplacedot</code>, <code>splinedot</code> functions etc. (see example.)
<code>lambda</code>	a user supplied <code>lambda</code> sequence. It is better to supply a decreasing sequence of <code>lambda</code> values, if not, the program will sort user-defined <code>lambda</code> sequence in decreasing order automatically.
<code>eps</code>	convergence threshold for majorization minimization algorithm. Each majorization descent loop continues until the relative change in any coefficient $\ \alpha(\text{new}) - \alpha(\text{old})\ _2^2 / \ \alpha(\text{old})\ _2^2$ is less than <code>eps</code> . Defaults value is $1e-8$.
<code>maxit</code>	maximum number of loop iterations allowed at fixed <code>lambda</code> value. Default is $1e4$. If models do not converge, consider increasing <code>maxit</code> .
<code>omega</code>	the parameter ω in the expectile regression model. The value must be in $(0,1)$. Default is 0.5 .

gamma	a scalar number. If it is specified, the number will be added to each diagonal element of the kernel matrix as perturbation. The default is 1e-06.
option	users can choose which method to use to update the inverse matrix in the MM algorithm. "fast" uses a trick described in Yang, Zhang and Zou (2015) to update estimates for each lambda. "normal" uses a naive way for the computation.

Details

Note that the objective function in KERE is

$$Loss(y - \alpha_0 - K * \alpha) + \lambda * \alpha^T * K * \alpha,$$

where the α_0 is the intercept, α is the solution vector, and K is the kernel matrix with $K_{ij} = K(x_i, x_j)$. Users can specify the kernel function to use, options include Radial Basis kernel, Polynomial kernel, Linear kernel, Hyperbolic tangent kernel, Laplacian kernel, Bessel kernel, ANOVA RBF kernel, the Spline kernel. Users can also tweak the penalty by choosing different *lambda*.

For computing speed reason, if models are not converging or running slow, consider increasing *eps* before increasing *maxit*.

Value

An object with S3 class [KERE](#).

call	the call that produced this object.
alpha	a <code>nrow(x)*length(lambda)</code> matrix of coefficients. Each column is a solution vector corresponding to a lambda value in the lambda sequence.
lambda	the actual sequence of lambda values used.
npass	total number of loop iterations corresponding to each lambda value.
jerr	error flag, for warnings and errors, 0 if no error.

Author(s)

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References

Y. Yang, T. Zhang, and H. Zou. "Flexible Expectile Regression in Reproducing Kernel Hilbert Space." ArXiv e-prints: stat.ME/1508.05987, August 2015.

Examples

```
# create data
N <- 200
X1 <- runif(N)
X2 <- 2*runif(N)
X3 <- 3*runif(N)
SNR <- 10 # signal-to-noise ratio
Y <- X1**1.5 + 2 * (X2**.5) + X1*X3
```

```

sigma <- sqrt(var(Y)/SNR)
Y <- Y + X2*rnorm(N,0,sigma)
X <- cbind(X1,X2,X3)

# set gaussian kernel
kern <- rbfdot(sigma=0.1)

# define lambda sequence
lambda <- exp(seq(log(0.5),log(0.01),len=10))

# run KERE
m1 <- KERE(x=X, y=Y, kern=kern, lambda = lambda, omega = 0.5)

# plot the solution paths
plot(m1)

```

kernel-class	<i>Class "kernel" "rbfkernel" "polykernel", "tanhkernel", "vanillakernel"</i>
--------------	---

Description

The built-in kernel classes in **KERE**

Objects from the Class

Objects can be created by calls of the form `new("rbfkernel")`, `new{"polykernel"}`, `new{"tanhkernel"}`, `new{"vanillakernel"}`, `new{"anovakernel"}`, `new{"besselkernel"}`, `new{"laplacekernel"}`, `new{"splinekernel"}` or by calling the `rbfdot`, `polydot`, `tanhdot`, `vanilladot`, `anovadot`, `besseldot`, `laplacedot`, `splinedot` functions etc..

Slots

.Data: Object of class "function" containing the kernel function
kpar: Object of class "list" containing the kernel parameters

Extends

Class "kernel", directly. Class "function", by class "kernel".

Methods

kernelMatrix signature(kernel = "rbfkernel", x = "matrix"): computes the kernel matrix
kernelMult signature(kernel = "rbfkernel", x = "matrix"): computes the quadratic kernel expression
kernelPol signature(kernel = "rbfkernel", x = "matrix"): computes the kernel expansion
kernelFast signature(kernel = "rbfkernel", x = "matrix"), ,a: computes parts or the full kernel matrix, mainly used in kernel algorithms where columns of the kernel matrix are computed per invocation

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See Also

[dots](#)

Examples

```
rbfkernel <- rbfdot(sigma = 0.1)
rbfkernel
is(rbfkernel)
kpar(rbfkernel)
```

kernelMatrix	<i>Kernel Matrix functions</i>
--------------	--------------------------------

Description

kernelMatrix calculates the kernel matrix $K_{ij} = k(x_i, x_j)$ or $K_{ij} = k(x_i, y_j)$.
 kernelPol computes the quadratic kernel expression $H = z_i z_j k(x_i, x_j)$, $H = z_i k_j k(x_i, y_j)$.
 kernelMult calculates the kernel expansion $f(x_i) = \sum_{j=1}^m z_j k(x_i, x_j)$
 kernelFast computes the kernel matrix, identical to kernelMatrix, except that it also requires the squared norm of the first argument as additional input, useful in iterative kernel matrix calculations.

Usage

```
## S4 method for signature 'kernel'
kernelMatrix(kernel, x, y = NULL)

## S4 method for signature 'kernel'
kernelPol(kernel, x, y = NULL, z, k = NULL)

## S4 method for signature 'kernel'
kernelMult(kernel, x, y = NULL, z, blocksize = 256)

## S4 method for signature 'kernel'
kernelFast(kernel, x, y, a)
```

Arguments

kernel	the kernel function to be used to calculate the kernel matrix. This has to be a function of class kernel, i.e. which can be generated either one of the build in kernel generating functions (e.g., rbfdot etc.) or a user defined function of class kernel taking two vector arguments and returning a scalar.
--------	---

x	a data matrix to be used to calculate the kernel matrix.
y	second data matrix to calculate the kernel matrix.
z	a suitable vector or matrix
k	a suitable vector or matrix
a	the squared norm of x, e.g., <code>rowSums(x^2)</code>
blocksize	the kernel expansion computations are done block wise to avoid storing the kernel matrix into memory. blocksize defines the size of the computational blocks.

Details

Common functions used during kernel based computations.

The kernel parameter can be set to any function, of class kernel, which computes the inner product in feature space between two vector arguments. **KERE** provides the most popular kernel functions which can be initialized by using the following functions:

- `rbfdot` Radial Basis kernel function
- `polydot` Polynomial kernel function
- `vanilladot` Linear kernel function
- `tanhdot` Hyperbolic tangent kernel function
- `laplacedot` Laplacian kernel function
- `besseldot` Bessel kernel function
- `anovadot` ANOVA RBF kernel function
- `splinedot` the Spline kernel

(see example.)

`kernelFast` is mainly used in situations where columns of the kernel matrix are computed per invocation. In these cases, evaluating the norm of each row-entry over and over again would cause significant computational overhead.

Value

`kernelMatrix` returns a symmetric diagonal semi-definite matrix.

`kernelPol` returns a matrix.

`kernelMult` usually returns a one-column matrix.

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See Also

[rbfdot](#), [polydot](#), [tanhdot](#), [vanilladot](#)

Examples

```
## use the spam data
x <- matrix(rnorm(10*10),10,10)

## initialize kernel function
rbf <- rbfdot(sigma = 0.05)
rbf

## calculate kernel matrix
kernelMatrix(rbf, x)

y <- matrix(rnorm(10*1),10,1)

## calculate the quadratic kernel expression
kernelPol(rbf, x, ,y)

## calculate the kernel expansion
kernelMult(rbf, x, ,y)
```

plot.KERE

Plot coefficients from a "KERE" object

Description

Produces a coefficient profile plot of the coefficient paths for a fitted [KERE](#) object.

Usage

```
## S3 method for class 'KERE'
plot(x, ...)
```

Arguments

x fitted [KERE](#) model.

... other graphical parameters to plot.

Details

A coefficient profile plot is produced. The x-axis is $\log(\lambda)$. The y-axis is the value of fitted α 's.

Author(s)

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References

Y. Yang, T. Zhang, and H. Zou. "Flexible Expectile Regression in Reproducing Kernel Hilbert Space." ArXiv e-prints: stat.ME/1508.05987, August 2015.

Examples

```
# create data
N <- 200
X1 <- runif(N)
X2 <- 2*runif(N)
X3 <- 3*runif(N)
SNR <- 10 # signal-to-noise ratio
Y <- X1**1.5 + 2 * (X2**.5) + X1*X3
sigma <- sqrt(var(Y)/SNR)
Y <- Y + X2*rnorm(N,0,sigma)
X <- cbind(X1,X2,X3)

# set gaussian kernel
kern <- rbfdot(sigma=0.1)

# define lambda sequence
lambda <- exp(seq(log(0.5),log(0.01),len=10))

# run KERE
m1 <- KERE(x=X, y=Y, kern=kern, lambda = lambda, omega = 0.5)

# plot the solution paths
plot(m1)
```

predict.KERE	<i>make predictions from a "KERE" object.</i>
--------------	---

Description

Similar to other predict methods, this functions predicts fitted values and class labels from a fitted [KERE](#) object.

Usage

```
## S3 method for class 'KERE'
predict(object, kern, x, newx,...)
```

Arguments

object	fitted KERE model object.
kern	the built-in kernel classes in KERE . Objects can be created by calling the rbfdot, polydot, tanhdot, vanilladot, anovadot, besseldot, laplacedot, splinedot functions etc. (see example.)

<code>x</code>	the original design matrix for training KERE.
<code>newx</code>	matrix of new values for <code>x</code> at which predictions are to be made. NOTE: <code>newx</code> must be a matrix with each row as an observation. <code>predict</code> function does not accept a vector or other formats of <code>newx</code> .
<code>...</code>	other parameters to <code>predict</code> function.

Details

The fitted $\alpha_0 + K * \alpha$ at `newx` is returned as a size `nrow(newx)*length(lambda)` matrix for various `lambda` values where the KERE model was fitted.

Value

The fitted $\alpha_0 + K * \alpha$ is returned as a size `nrow(newx)*length(lambda)` matrix. The row represents the index for observations of `newx`. The column represents the index for the `lambda` sequence.

Author(s)

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References

Y. Yang, T. Zhang, and H. Zou. "Flexible Expectile Regression in Reproducing Kernel Hilbert Space." ArXiv e-prints: stat.ME/1508.05987, August 2015.

Examples

```
# create data
N <- 100
X1 <- runif(N)
X2 <- 2*runif(N)
X3 <- 3*runif(N)
SNR <- 10 # signal-to-noise ratio
Y <- X1**1.5 + 2 * (X2**1.5) + X1*X3
sigma <- sqrt(var(Y)/SNR)
Y <- Y + X2*rnorm(N,0,sigma)
X <- cbind(X1,X2,X3)

# set gaussian kernel
kern <- rbfdot(sigma=0.1)

# define lambda sequence
lambda <- exp(seq(log(0.5),log(0.01),len=10))

# run KERE
m1 <- KERE(x=X, y=Y, kern=kern, lambda = lambda, omega = 0.5)

# create newx for prediction
N1 <- 5
X1 <- runif(N1)
```

```
X2 <- 2*runif(N1)
X3 <- 3*runif(N1)
newx <- cbind(X1,X2,X3)

# make prediction
p1 <- predict.KERE(m1, kern, X, newx)
p1
```

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