

Package ‘brxx’

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Type Package

Title Bayesian Test Reliability Estimation

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Description When samples contain missing data, are small, or are suspected of bias, estimation of scale reliability may not be trustworthy. A recommended solution for this common problem has been Bayesian model estimation. Bayesian methods rely on user specified information from historical data or researcher intuition to more accurately estimate the parameters. This package provides a user friendly interface for estimating test reliability. Here, reliability is modeled as a beta distributed random variable with shape parameters $\alpha = \text{true score variance}$ and $\beta = \text{error variance}$ (Tanzer & Harlow, 2020) <doi:10.1080/00273171.2020.1854082>.

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bcor	<i>bcor: Bayesian Estimation of The Correlation Matrix</i>
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Description

This function estimates coefficient omega internal consistency reliability.

Usage

```
bcor(data, iter, burn, seed, CI, S0, nu0, mu0)
```

Arguments

data	N by P data matrix.
iter	Number of iterations for the Gibbs sampler.
burn	Number of samples to burn in.
seed	Seed for the Gibbs sampler
CI	Credible interval quantile, as a decimal (ie, for 95 percent, 0.95).
S0	Prior variance covariance matrix.
nu0	Prior degrees of freedom for inverse Wishart prior distribution.
mu0	Prior means for each column.

Value

Returns median posterior estimates of the correlation matrix.

Examples

```
set.seed(999)
your_data=mvnrm(n=15,mu=c(0,0),Sigma=matrix(c(4,3,3,9),nrow=2,ncol=2))
Mu0=c(0,0)
Sigma0=matrix(c(1,0.6,0.6,4),nrow=2,ncol=2)
Nu0=1
bcor(data=your_data,iter=5000,burn=2500,seed=999,CI=0.95,
      mu0=Mu0,S0=Sigma0,nu0=Nu0)
```

bcov

*bcov: Bayesian Estimation of the Variance Covariance Matrix***Description**

This function estimates the variance covariance matrix for a

Usage

```
bcov(data, iter, burn, seed, CI, S0, nu0, mu0)
```

Arguments

data	N by P data matrix.
iter	Number of iterations for the Gibbs sampler.
burn	Number of samples to burn in.
seed	Seed for the Gibbs sampler
CI	Credible interval quantile, as a decimal (ie, for 95 percent, 0.95).
S0	Prior variance covariance matrix.
nu0	Prior degrees of freedom for inverse Wishart prior distribution.
mu0	Prior means for each column.

Value

Returns median posterior estimates of the variance covariance matrix.

Examples

```
## Not run:
set.seed(999)
your_data=mvnrm(n=15,mu=c(0,0),Sigma=matrix(c(4,3,3,9),nrow=2,ncol=2))
Mu0=c(0,0)
Sigma0=matrix(c(1,0.6,0.6,4),nrow=2,ncol=2)
Nu0=3-1
bcov(data=your_data,iter=5000,burn=2500,seed=999,CI=0.95,
      mu0=Mu0,S0=Sigma0,nu0=Nu0)
## End(Not run)
```

bomega

*bomega: Bayesian Estimation of Coefficient Omega***Description**

This function estimates coefficient omega internal consistency reliability.

Usage

```
bomega(K, mod, alpha, beta, CI)
```

Arguments

K	The number of test items.
mod	A measurement model estimated as a bsem object by blavaan.
alpha	Prior true score variance.
beta	Prior error variance.
CI	Credible interval quantile, as a decimal (ie, for 95 percent, 0.95).

Value

Returns estimated median and quantile based credible limits for omega.

Examples

```
your_data=data.frame(mvrnorm(n=20,mu=c(0,0,0,0,0),
Sigma=matrix(c(4,2,2,2,2,
                2,4,2,2,2,
                2,2,4,2,2,
                2,2,2,4,2,
                2,2,2,2,4),
                nrow=5, ncol=5)))
colnames(your_data)=c("x1","x2","x3","x4","x5")
mod='tau=~x1+x2+x3+x4+x5'
fit=bsem(mod,data=your_data)
bomega(K=5,mod=fit,alpha=3.51,beta=1.75,CI=0.95)
```

bomega_general	<i>bomega_general: Bayesian Estimation of Coefficient Omega, General Form</i>
----------------	---

Description

This function estimates coefficient omega internal consistency reliability.

Usage

```
bomega_general(lambda, psi, alpha, beta, CI)
```

Arguments

lambda	vector of item loadings.
psi	vector of item variances.
alpha	Prior true score variance.
beta	Prior error variance.
CI	Credible interval quantile, as a decimal (ie, for 95 percent, 0.95).

Value

Returns estimated median and quantile based credible limits for omega.

Examples

```
lambda=c(0.7,0.5,0.6,0.7)
psi=c(0.2,0.4,0.3)
alpha=3.51
beta=1.75
bomega_general(lambda=lambda,psi=psi,alpha=alpha,beta=beta,CI=0.95)
```

brxx_Cor	<i>brxx_Cor: Bayesian Estimation of Reliability from Correlation</i>
----------	--

Description

This function estimates reliability from a correlation

Usage

```
brxx_Cor(x, y, alpha, beta, iter, burn, seed, CI, S0, nu0, mu0, items)
```

Arguments

x	First variable.
y	Second variable.
alpha	Prior true score variance (covariance between tests)
beta	Prior error variance (product of standard deviations minus covariance)
iter	Number of iterations for the Gibbs sampler.
burn	Number of samples to burn in.
seed	Seed for the Gibbs sampler
CI	Credible interval quantile, as a decimal (ie, for 95 percent, 0.95).
S0	Prior variance covariance matrix.
nu0	Prior degrees of freedom for inverse Wishart prior distribution.
mu0	Prior means for each column.
items	Number of test items.

Value

Returns median posterior estimates of the variance covariance matrix.

Examples

```
set.seed(999)
your_data=mvnrm(n=15,mu=c(0,0),Sigma=matrix(c(4,5,5,9),nrow=2,ncol=2))
x=your_data[,1]
y=your_data[,2]
Mu0=c(0,0)
Sigma0=matrix(c(1,0.6,0.6,4),nrow=2,ncol=2)
Nu0=3-1
brxx_Cor(x=x,y=y,iter=5000,burn=2500,seed=999,CI=0.95,
mu0=Mu0,S0=Sigma0,nu0=Nu0,items=10)
```

brxx_Cor_general

brxx_Cor_general: Bayesian Estimation of Reliability from Correlation, General Form

Description

This function estimates reliability from correlation given the correlation estimate.

Usage

```
brxx_Cor_general(cor, alpha, beta, CI, items)
```

Arguments

cor	Correlation estimate.
alpha	Prior true score variance.
beta	Prior error variance.
CI	Credible interval quantile, as a decimal (ie, for 95 percent, 0.95).
items	Number of test items.

Value

Returns estimated median and quantile based credible limits for reliability.

Examples

```
brxx_Cor_general(cor=0.85,alpha=3.51,beta=1.75,CI=0.95,items=10)
```

brxx_general	<i>brxx_general: Bayesian Estimation of Reliability from Variance Estimates</i>
--------------	---

Description

This function estimates reliability from given true and error variance estimates.

Usage

```
brxx_general(a, b, alpha, beta, CI, items)
```

Arguments

a	True score variance estimate.
b	Error variance estimate.
alpha	Prior true score variance.
beta	Prior error variance.
CI	Credible interval quantile, as a decimal (ie, for 95 percent, 0.95).
items	Number of test items.

Value

Returns estimated median and quantile based credible limits for reliability.

Examples

```

a=18.7
b=3.3
alpha=3.51
beta=1.75
brxx_general(a=a,b=b,alpha=alpha,beta=beta,CI=0.95,items=10)

```

brxx_ICC

*brxx_ICC: Bayesian Estimation of Reliability from ICC***Description**

This function estimates reliability from intraclass correlation coefficient

Usage

```
brxx_ICC(mod, alpha, beta, CI, items)
```

Arguments

mod	A mixed effects model object estimated by blmer.
alpha	Prior true score variance (subject variance)
beta	Prior error variance (residual variance)
CI	Credible interval quantile, as a decimal (ie, for 95 percent, 0.95).
items	Number of test items.

Value

Returns estimated median and quantile based credible limits for ICC.

Examples

```

your_data_wide=mvnrm(20,c(0,0),matrix(c(1,0.8,0.8,1),nrow=2,ncol=2))
your_data_long=c(as.vector(your_data_wide[,1]),as.vector(your_data_wide[,2]))
time=c(rep(0,20),rep(1,20))
id=c(rep(1:20,2))
mod=blmer(your_data_long~time+(1|id))
brxx_ICC(mod=mod,alpha=3.51,beta=1.75,CI=0.95,items=10)

```

brxx_ICC_general	<i>brxx_ICC_general: Bayesian Estimation of Reliability from ICC, General Form</i>
------------------	--

Description

This function estimates reliability from intraclass correlation given correlation.

Usage

```
brxx_ICC_general(WS, Resid, alpha, beta, CI, items)
```

Arguments

WS	Within subjects variance estimate.
Resid	Residual variance estimate.
alpha	Prior true score variance.
beta	Prior error variance.
CI	Credible interval quantile, as a decimal (ie, for 95 percent, 0.95).
items	Number of test items.

Value

Returns estimated median and quantile based credible limits for reliability.

Examples

```
WS=20.4
Resid=3.6
alpha=3.51
beta=1.75
brxx_ICC_general(WS=WS,Resid=Resid,alpha=alpha,beta=beta,CI=0.95,items=5)
```

prep	<i>prep: Prepare Data File for Bayesian Analysis</i>
------	--

Description

This function prepares data for analysis using Stan factor analysis code.

Usage

```
prep(data, nfactors, Prior)
```

Arguments

data	N by P data matrix.
nfactors	Number of factors to extract.
Prior	Prior loading matrix.

Value

Returns a formatted data file for use with Stan MCMC sampler.

Examples

```
set.seed(999)
your_data=data.frame(mvrnorm(n=20,mu=c(0,0,0,0,0),
                             Sigma=matrix(c(4,2,2,2,2,
                                             2,4,2,2,2,
                                             2,2,4,2,2,
                                             2,2,2,4,2,
                                             2,2,2,2,4),
                                             nrow=5, ncol=5)))
colnames(your_data)=c("x1","x2","x3","x4","x5")
your_data_miss=matrix(ncol=5,nrow=20)
for (i in 1:20){
  for (p in 1:5){
    your_data_miss[i,p]=ifelse(runif(1,0,1)<0.2,NA,your_data[i,p])
  }
}
formatted_data=prep(your_data_miss,nfactors=3)
```

process

process: rotates and calculates reliability for Stan output

Description

This function processes Stan loading matrix data.

Usage

```
process>Loading_Matrix, Format, Rotate)
```

Arguments

Loading_Matrix	S by P*Q matrix of loading samples.
Format	list formatted data file provided for Stan
Rotate	If Q>1, rotation (for options, see GPArotation package)

Value

Returns rotated loadings, uniqueness, communality, and reliability.

Examples

```
## Not run:
your_data_s=standardize(your_data)
formatted_data=prep(your_data_s,nfactors=3)
out=sampling(model, data=formatted_data, iter=5000, seed=999)
res=as.matrix(out)
unpacked=unpack(Samples=res,Format=formatted_data)

processed=process>Loading_Matrix=unpacked$Loading_Matrix,
                  Format=formatted_data,
                  Rotate="oblimin")
## End(Not run)
```

scree

scree: Scree Plot with Pairwise Complete Cases

Description

This function provides a scree plot when data may be missing.

Usage

```
scree(data)
```

Arguments

data N by P data matrix.

Value

Returns eigenvalues and scree plot.

Examples

```
set.seed(999)
your_data=data.frame(mvrnorm(n=20,mu=c(0,0,0,0,0),
                               Sigma=matrix(c(4,2,2,2,2,
                                                2,4,2,2,2,
                                                2,2,4,2,2,
                                                2,2,2,4,2,
                                                2,2,2,2,4),
                                              nrow=5, ncol=5)))
colnames(your_data)=c("x1","x2","x3","x4","x5")
```

```

your_data_miss=matrix(ncol=5,nrow=20)
for (i in 1:20){
  for (p in 1:5){
    your_data_miss[i,p]=ifelse(runif(1,0,1)<0.2,NA,your_data[i,p])
  }
}
scree(your_data_miss)

```

standardize

standardize: Standardization of Data Matrix

Description

This function standardizes an N by P data matrix, as is strongly recommended before using any of the brxx reliability estimation functions

Usage

```
standardize(data)
```

Arguments

data N by P data matrix.

Value

Returns an item level standardized data matrix.

Examples

```

set.seed(999)
your_data=data.frame(mvrnorm(n=20,mu=c(0,0,0,0,0,0,0),
                               Sigma=matrix(c(4,2,2,2,2,2,2,
                                                2,4,2,2,2,2,2,
                                                2,2,4,2,2,2,2,
                                                2,2,2,4,2,2,2,
                                                2,2,2,2,4,2,2,
                                                2,2,2,2,2,4,2,
                                                2,2,2,2,2,2,4,2,
                                                2,2,2,2,2,2,2,4),
                               nrow=7, ncol=7)))

your_data_miss=matrix(ncol=5,nrow=20)
for (i in 1:20){
  for (p in 1:5){
    your_data_miss[i,p]=ifelse(runif(1,0,1)<0.2,NA,your_data[i,p])
  }
}
standardize(your_data_miss)

```

summarize	<i>summarize: Summarize Stan output as median, SD, and HPD quantiles</i>
-----------	--

Description

This function converts raw MCMC sample data into matrix formatted summaries

Usage

```
summarize(Samples, nrow, ncol, CI)
```

Arguments

Samples	S by theta matrix of sampled parameter estimates.
nrow	Number of rows of target summary matrix
ncol	Number of columns of target summary matrix
CI	Credible interval quantile, as a decimal (ie, for 95 percent, 0.95)

Value

Returns median, SD, and HPD CI limits

Examples

```
## Not run:
your_data_s=standardize(your_data)
formatted_data=prep(your_data_s,nfactors=3)
out=sampling(model, data=formatted_data, iter=5000, seed=999)
res=as.matrix(out)
unpacked=unpack(Samples=res,Format=formatted_data)
processed=process>Loading_Matrix=unpacked$Loading_Matrix,
               Format=formatted_data,
               Rotate="oblimin")

summarize(processed$Loadings,
           nrow=Formatted_data$P,
           ncol=Formatted_data$Q)$Table
summarize(processed$Communality,
           nrow=Formatted_data$P,
           ncol=1)$Table
summarize(processed$Uniqueness,
           nrow=Formatted_data$P,
           ncol=1)$Table
summarize(processed$G_Factor,
           nrow=Formatted_data$P,
           ncol=1)$Table
summarize(processed$Interfactor_Correlations,
```

```

        nrow=Formatted_data$Q,
        ncol=Formatted_data$Q)$Table
summarize(processed$Omega,
          nrow=1,
          ncol=1)$Table
summarize(unpacked$Tau_Matrix,
          nrow=Formatted_data$P,
          ncol=1)$Table
## End(Not run)

```

unpack

unpack: Unpack Stan output for factor analysis samples from Stan

Description

This function unpacks raw Stan samples output.

Usage

```
unpack(Samples, Format)
```

Arguments

Samples	S by theta matrix of sample parameter estimates.
Format	list formatted data file provided for Stan

Value

Returns four matrices:

- 1). S by Q latent score matrix, x.
- 2). S by Q*P loading matrix, lambda.
- 3). S by P mean matrix, tau.
- 4). S by P loading variance matrix, alpha.

Examples

```

## Not run:
your_data_s=standardize(your_data)
formatted_data=prep(your_data_s,nfactors=3)
out=sampling(model, data=formatted_data, iter=5000, seed=999)
res=as.matrix(out)

```

```

unpacked=unpack(Samples=res,Format=formatted_data)
## End(Not run)

```

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