# Package 'causalOT'

July 22, 2025

```
Type Package
Title Optimal Transport Weights for Causal Inference
Version 1.0.2
Date 2024-02-17
Author Eric Dunipace [aut, cre] (ORCID:
      <https://orcid.org/0000-0001-8909-213X>)
Maintainer Eric Dunipace <edunipace@mail.harvard.edu>
Description Uses optimal transport distances to find probabilistic
      matching estimators for causal inference.
      These methods are described in Dunipace, Eric (2021) <doi:10.48550/arXiv.2109.01991>.
      The package will build the weights, estimate treatment effects, and
      calculate confidence intervals via the methods described in the paper.
      The package also supports several other methods as described in the help
      files.
License GPL (== 3.0)
Imports CBPS, ggplot2, lbfgsb3c, loo, Matrix (>= 1.5-0), matrixStats,
      methods, osqp, R6 (\geq= 2.4.1), Rcpp (\geq= 1.0.3), rlang, sandwich,
      torch, utils
LinkingTo BH (>= 1.66.0), Rcpp (>= 0.12.0), RcppEigen (>= 0.3.3.3.0),
      torch
Suggests data.table (>= 1.12.8), testthat (>= 2.1.0), knitr,
      reticulate, rkeops (>= 2.2.2), rmarkdown, V8, withr
Additional_repositories https://ericdunipace.github.io/drat/
Biarch true
Depends R (>= 3.5.0)
Encoding UTF-8
RoxygenNote 7.3.1
LazyData true
VignetteBuilder knitr
```

2 Contents

Collate 'DataSimClass.R' 'dataHolder.R' 'weightsClass.R' 'ESS.R'
'OT.R' 'PSIS.R' 'RcppExports.R' 'balanceFunctions.R'
'barycentricProjection.R' 'calc_weight.R' 'causalOT-package.R'
'cost_functions.R' 'scmClass.R' 'gridSearch.R' 'cotClass.R'
'cotOOP.R' 'cot_opts.R' 'likelihoodClass.R' 'mean_balance.R'
'summary.R' 'supportedMethods.R' 'treatment_effect.R' 'utils.R'
'zzz.R'

NeedsCompilation yes

Repository CRAN

**Date/Publication** 2024-02-18 22:50:08 UTC

# **Contents**

Index

	48
vcov.causalEffect	46
supported_methods	46
summary.causalWeights	44
scmOptions	44
sbwOptions	43
PSIS	41
print.dataHolder	40
predict.bp	
pph	38
plot.causalWeights	
ot_distance	33
OTProblem	29
Measure	26
mean_balance	26
LaLonde	23
Hainmueller	21
estimate_effect	20
ESS	19
entBWOptions	18
df2dataHolder	17
DataSim	15
dataHolder	14
CRASH3	12
cotOptions	9
coef.causalEffect	8
causalWeights-class	7
calc_weight	5
barycentric_projection	3

barycentric\_projection

Barycentric Projection outcome estimation

# Description

Barycentric Projection outcome estimation

# Usage

```
barycentric_projection(
  formula,
  data,
  weights,
  separate.samples.on = "z",
  penalty = NULL,
  cost_function = NULL,
  p = 2,
  debias = FALSE,
  cost.online = "auto",
  diameter = NULL,
  niter = 1000L,
  tol = 1e-07,
  ...
)
```

#### **Arguments**

formula A formula object specifying the outcome and covariates.

data A data.frame of the data to use in the model.

weights Either a vector of weights, one for each observations, or an object of class

causalWeights.

separate.samples.on

The variable in the data denoting the treatment indicator. How to separate sam-

ples for the optimal transport calculation

penalty The penalty parameter to use in the optimal transport calculation. By default it

is  $1/\log(n)$ .

cost\_function A user supplied cost function. If supplied, must take arguments x1, x2, and p.

p The power to raise the cost function. Default is 2.0. For user supplied cost

functions, the cost will not be raised by this power unless the user so specifies.

debias Should debiased barycentric projections be used? See details.

cost.online Should an online cost algorithm be used? Default is "auto", which selects an on-

line cost algorithm when the sample size in each group specified by separate.samples.on,

 $n_0$  and  $n_1$ , is such that  $n_0 \cdot n_1 \ge 5000^2$  Must be one of "auto", "online", or "ten-

sorized". The last of these is the offline option.

diameter The diameter of the covariate space, if known.

niter The maximum number of iterations to run the optimal transport problems

tol The tolerance for convergence of the optimal transport problems

... Not used at this time.

#### **Details**

The barycentric projection uses the dual potentials from the optimal transport distance between the two samples to calculate projections from one sample into another. For example, in the sample of controls, we may wish to know their outcome had they been treated. In general, we then seek to minimize

$$\operatorname{argmin}_{\eta} \sum_{ij} cost(\eta_i, y_j) \pi_{ij}$$

where  $\pi_{ij}$  is the primal solution from the optimal transport problem.

These values can also be de-biased using the solutions from running an optimal transport problem of one sample against itself. Details are listed in Pooladian et al. (2022) https://arxiv.org/abs/2202.08919.

#### Value

An object of class "bp" which is a list with slots:

- potentials The dual potentials from calculating the optimal transport distance
- penalty The value of the penalty parameter used in calculating the optimal transport distance
- cost\_function The cost function used to calculate the distances between units.
- cost\_alg A character vector denoting if an L<sub>1</sub> distance, a squared euclidean distance, or other distance metric was used.
- p The power to which the cost matrix was raised if not using a user supplied cost function.
- · debias Whether barycentric projections should be debiased.
- tensorized TRUE/FALSE denoting wether to use offline cost matrices.
- data An object of class dataHolder with the data used to calculate the optimal transport distance.
- y\_a The outcome vector in the first sample.
- y\_b The outcome vector in the second sample.
- x\_a The covariate matrix in the first sample.
- x\_b The covariate matrix in the second sample.
- a The empirical measure in the first sample.
- b The empirical measure in the second sample.
- terms The terms object from the formula.

calc\_weight 5

# **Examples**

```
if(torch::torch_is_installed()) {
set.seed(23483)
n <- 2<sup>5</sup>
pp <- 6
overlap <- "low"</pre>
design <- "A"
estimate <- "ATT"
power <- 2
data <- causalOT::Hainmueller$new(n = n, p = pp,</pre>
design = design, overlap = overlap)
data$gen_data()
weights <- causalOT::calc_weight(x = data,</pre>
  z = NULL, y = NULL,
  estimand = estimate,
  method = "NNM")
 df <- data.frame(y = data$get_y(), z = data$get_z(), data$get_x())</pre>
 fit <- causalOT::barycentric_projection(y ~ ., data = df,</pre>
    weight = weights,
    separate.samples.on = "z",
    niter = 2)
 inherits(fit, "bp")
 }
```

calc\_weight

Estimate causal weights

# Description

Estimate causal weights

# Usage

```
calc_weight(
    x,
    z,
    estimand = c("ATC", "ATT", "ATE"),
    method = supported_methods(),
    options = NULL,
    weights = NULL,
    ...
)
```

6 calc\_weight

#### **Arguments**

X	A numeric matrix of covariates. You can also pass an object of class dataHolder or DataSim, which will make argument z not necessary,
Z	A binary treatment indicator.
estimand	The estimand of interest. One of "ATT", "ATC", or "ATE".
method	The method to estimate the causal weights. Must be one of the methods returned by supported_methods().
options	The options for the solver. Specific options depend on the solver you will be using and you can use the solver specific options functions as detailed below
weights	The sample weights. Should be NULL or have a weight for each observation in the data. Normalized to sum to one.
	Not used at this time.

#### **Details**

We detail some of the particulars of the function arguments below.

# **Causal Optimal Transport (COT):**

This is the main method of the package. This method relies on various solvers depending on the particular options chosen. Please see cotOptions() for more details.

#### **Energy Balancing Weights (EnergyBW):**

This is equivalent to COT with an infinite penalty parameter, options(lambda = Inf). Uses the same solver and options as COT, cotOptions().

#### **Nearest Neighbor Matching with replacement (NNM):**

This is equivalent to COT with a penalty parameter = 0, options(lambda = 0). Uses the same solver and options as COT, cotOptions().

#### **Synthetic Control Method (SCM):**

The SCM method is equivalent to an OT problem from a different angle. See scmOptions().

#### **Entropy Balancing Weights (EntropyBW):**

This method balances chosen functions of the covariates specified in the data argument, x. See entBWOptions() for more details. Hainmueller (2012).

# **Stable Balancing Weights (SBW):**

Entropy Balancing Weights with a different penalty parameter, proposed by Zuizarreta (2012). See <a href="mailto:sbw0ptions">sbw0ptions</a>() for more details

# **Covariate Balancing Propensity Score (CBPS):**

The CBPS method of Imai and Ratkovic. Options argument is passed to the function CBPS().

# **Logistic Regression or Probit Regression:**

The main methods historically for implementing inverse probability weights. Options are passed directly to the glm function from R.

causalWeights-class 7

#### Value

An object of class causalWeights

#### See Also

```
estimate_effect()
```

#### **Examples**

```
set.seed(23483)
n <- 2<sup>5</sup>
p <- 6
#### get data ####
data <- Hainmuellernew(n = n, p = p)
data$gen_data()
x <- data$get_x()</pre>
z <- data$get_z()</pre>
if (torch::torch_is_installed()) {
# estimate weights
weights <- calc_weight(x = x,
                                   z = z,
                                   estimand = "ATE",
                                   method = "COT",
                                   options = list(lambda = 0))
#we can also use the dataSim object directly
weightsDS <- calc_weight(x = data,</pre>
                                   z = NULL,
                                   estimand = "ATE",
                                   method = "COT",
                                   options = list(lambda = 0))
all.equal(weights@w0, weightsDS@w0)
all.equal(weights@w1, weightsDS@w1)
}
```

causalWeights-class causalWeights class

# **Description**

causalWeights class

#### **Details**

This object is returned by the calc\_weight function in this package. The slots can be accessed as any S4 object. There is no publicly accessible constructor function.

8 coef.causalEffect

#### **Slots**

```
w0 A slot with the weights for the control group with n_0 entries. Weights sum to 1.
w1 The weights for the treated group with n_1 entries. Weights sum to 1.
```

estimand A character denoting the estimand targeted by the weights. One of "ATT", "ATC", or "ATE".

info A slot to store a variety of info for inference. Currently under development.

method A character denoting the method used to estimate the weights.

penalty A list or the selected penalty parameters, if relevant.

data The dataHolder object containing the original data.

call The call used to construct the weights.

coef.causalEffect

Extract treatment effect estimate

# Description

Extract treatment effect estimate

#### Usage

```
## S3 method for class 'causalEffect'
coef(object, ...)
```

# **Arguments**

object An object of class causalEffect
... Not used

#### Value

A number corresponding to the estimated treatment effect

# **Examples**

```
# set-up data
set.seed(1234)
data <- Hainmueller$new()
data$gen_data()

# calculate quantities
weight <- calc_weight(data, method = "Logistic", estimand = "ATE")
tx_eff <- estimate_effect(causalWeights = weight)

all.equal(coef(tx_eff), c(estimate = tx_eff@estimate))</pre>
```

cotOptions 9

cotOptions

Options available for the COT method

# **Description**

Options available for the COT method

# Usage

```
cotOptions(
  lambda = NULL,
  delta = NULL,
  opt.direction = c("dual", "primal"),
  debias = TRUE,
  p = 2,
  cost.function = NULL,
  cost.online = "auto",
  diameter = NULL,
 balance.formula = NULL,
  quick.balance.function = TRUE,
  grid.length = 7L,
  torch.optimizer = torch::optim_rmsprop,
  torch.scheduler = torch::lr_multiplicative,
  niter = 2000,
 nboot = 100L,
  lambda.bootstrap = 0.05,
  tol = 1e-04,
  device = NULL,
  dtype = NULL,
)
```

# **Arguments**

lambda	The penalty parameter for the entropy penalized optimal transport. Default is NULL. Can be a single number or a set of numbers to try.
delta	The bound for balancing functions if they are being used. Only available for biased entropy penalized optimal transport. Can be a single number or a set of numbers to try.
opt.direction	Should the optimizer solve the primal or dual problems. Should be one of "dual" or "primal" with a default of "dual" since it is typically faster.
debias	Should debiased optimal transport be used? TRUE or FALSE.
p	The power of the cost function to use for the cost.
cost.function	A function to calculate the pairwise costs. Should take arguments $x1$ , $x2$ , and $p$ . Default is NULL.

10 cotOptions

cost.online Should an online cost algorithm be used? One of "auto", "online", or "ten-

sorized". "tensorized" is the offline option.

diameter The diameter of the covariate space, if known. Default is NULL.

balance.formula

Formula for the balancing functions.

quick.balance.function

TRUE or FALSE denoting whether balance function constraints should be selected via a linear program (TRUE) or just checked for feasibility (FALSE).

Default is TRUE.

grid.length The number of penalty parameters to explore in a grid search if none are pro-

vided in arguments lambda or delta.

torch.optimizer

The torch optimizer to use for methods using debiased entropy penalized optimal transport. If debiased is FALSE or opt.direction is "primal", will default to torch::optim\_lbfgs(). Otherwise torch::optim\_rmsprop() is

used.

torch.scheduler

The scheduler for the optimizer. Defaults to torch::lr\_multiplicative().

niter The number of iterations to run the solver

nboot The number of iterations for the bootstrap to select the final penalty parameters.

lambda.bootstrap

The penalty parameter to use for the bootstrap hyperparameter selection of lambda.

tol The tolerance for convergence

device An object of class torch\_device denoting which device the data will be located

on. Default is NULL which will try to use a gpu if available.

dtype An object of class torch\_dtype that determines data type of the data, i.e. dou-

ble, float, integer. Default is NULL which will try to select for you.

... Arguments passed to the solvers. See details

#### Value

A list of class cotOptions with the following slots

- lambdaThe penalty parameter for the optimal transport distance
- deltaThe constraint for the balancing functions
- opt.direction Whether to solve the primal or dual optimization problems
- debiasTRUE or FALSE if debiased optimal transport distances are used
- balance. formula The formula giving how to generate the balancing functions.
- quick.balance.function TRUE or FALSE whether quick balance functions will be run.
- grid.length The number of parameters to check in a grid search of best parameters
- p The power of the cost function
- cost.online Whether online costs are used
- cost.function The user supplied cost function if supplied.

cotOptions 11

- diameter The diameter of the covariate space.
- torch.optimizer The torch optimizer used for Sinkhorn Divergences
- torch. scheduler The scheduler for the torch optimizer
- solver.options The arguments to be passeed to the torch.optimizer
- scheduler.options The arguments to be passeed to the torch.scheduler
- osqp.options Arguments passed to the osqp function if quick balance functions are used.
- niter The number of iterations to run the solver
- nboot The number of bootstrap samples
- lambda.bootstrap The penalty parameter to use for the bootstrap hyperparameter selection.
- tol The tolerance for convergence.
- device An object of class torch\_device.
- dtype An object of class torch\_dtype.

#### Solvers and distances

The function is setup to direct the COT optimizer to run two basic methods: debiased entropy penalized optimal transport (Sinkhorn Divergences) or entropy penalized optimal transport (Sinkhorn Distances).

#### **Sinkhorn Distances:**

The optimal transport problem solved is  $min_w OT_{\lambda}(w, b)$  where

$$OT_{\lambda}(w,b) = \sum_{ij} C(x_i, x_j) P_{ij} + \lambda \sum_{ij} P_{ij} \log(P_{ij}),$$

such that the rows of the matrix  $P_{ij}$  sum to w and the columns sum to b. In this case C(,) is the cost between units i and j.

#### **Sinkhorn Divergences:**

The Sinkhorn Divergence solves

$$min_w OT_{\lambda}(w,b) - 0.5OT_{\lambda}(w,w) - 0.5 * OT_{\lambda}(b,b).$$

The solver for this function uses the torch package in R and by default will use the optim\_rmsprop solver. Your desired torch optimizer can be passed via torch.optimizer with a scheduler passed via torch.scheduler. GPU support is available as detailed in the torch package. Additional arguments in . . . are passed as extra arguments to the torch optimizer and schedulers as appropriate.

#### **Function balancing**

There may be certain functions of the covariates that we wish to balance within some tolerance,  $\delta$ . For these functions B, we will desire

$$\frac{\sum_{i:Z_i=0} w_i B(x_i) - \sum_{j:Z_j=1} B(x_j) / n_1}{\sigma} \le \delta$$

, where in this case we are targeting balance with the treatment group for the ATT.  $\sigma$  is the pooled standard deviation prior to balancing.

12 CRASH3

#### **Cost functions**

The cost function specifies pairwise distances. If argument cost. function is NULL, the function will default to using  $L_p^p$  distances with a default p=2 supplied by the argument p. So for p = 2, the cost between units  $x_i$  and  $x_j$  will be

$$C(x_i, x_j) = \frac{1}{2} ||x_i - x_j||_2^2.$$

If cost. function is provided, it should be a function that takes arguments x1, x2, and p: function(x1, x2, p){...}.

# **Examples**

```
if ( torch::torch_is_installed()) {
  opts1 <- cotOptions(lambda = 1e3, torch.optimizer = torch::optim_rmsprop)
  opts2 <- cotOptions(lambda = NULL)
  opts3 <- cotOptions(lambda = seq(0.1, 100, length.out = 7))
}</pre>
```

CRASH3

CRASH3 data example

#### **Description**

CRASH3 data example

CRASH3 data example

#### **Details**

Returns the CRASH3 data. Note that  $gen\_data()$  will initialize the fixed data for x and y, but z is generated from Binom(0.5).

# Value

An R6 object of class DataSim

# Super class

```
causalOT::DataSim -> CRASH3
```

#### **Public fields**

site\_id The site of the observation in terms of the original RCT.

CRASH3

# Methods

```
Public methods:
  • CRASH3$gen_data()
  • CRASH3$gen_x()
  • CRASH3$gen_y()
  • CRASH3$gen_z()
  • CRASH3$new()
  • CRASH3$clone()
Method gen_data(): The site ID for the observations
Draws new treatment indicators. x and y data are fixed.
 Usage:
 CRASH3$gen_data()
Method gen_x(): Sets up the covariate data. This data is fixed.
 Usage:
 CRASH3$gen_x()
Method gen_y(): Sets up the outcome data. This data is fixed.
 Usage:
 CRASH3$gen_y()
Method gen_z(): Sets up the treatment indicator. Drawn as Z \sim Binom(0.5)
 Usage:
 CRASH3$gen_z()
Method new(): Initializes the CRASH3 object.
 Usage:
 CRASH3$new(n = NULL, p = NULL, param = list(), design = NA_character_, ...)
 Arguments:
 n Not used. Maintained for symmetry with other DataSim objects.
 p Not used. Maintained for symmetry with other DataSim objects.
 param Not used. Maintained for symmetry with other DataSim objects.
 design Not used
 ... Not used.
 Examples:
 crash <- CRASH3$new()</pre>
 crash$gen_data()
 crash$get_n()
 crash$site_id
Method clone(): The objects of this class are cloneable with this method.
 Usage:
 CRASH3$clone(deep = FALSE)
 Arguments:
```

deep Whether to make a deep clone.

14 dataHolder

#### **Examples**

```
## ------
## Method `CRASH3$new`
## ------
crash <- CRASH3$new()
crash$gen_data()
crash$get_n()
crash$site_id</pre>
```

dataHolder

dataHolder

# **Description**

dataHolder

# Usage

```
dataHolder(x, z, y = NA_real_, weights = NA_real_)
```

# **Arguments**

X	the covariate data. Can be a matrix, an object of class dataHolder or a DataSim object. The latter two object types won't need arguments z or y.
z	the treatment indicator
У	the outcome data
weights	the empirical distribution of the sample

#### **Details**

Creates an object used internally by the causalOT package for data management.

#### Value

Returns an object of class dataHolder with slots

- x matrix. A matrix of confounders.
- z integer. The treatment indicator,  $z_i \in \{0, 1\}$ .
- y numeric. The outcome data.
- n0 integer. The number of observations where z==0
- n1 integer. The number of observations where z==1
- weights numeric. The empirical distribution of the full sample.

DataSim 15

#### **Examples**

```
x <- matrix(0, 100, 10)
z <- stats::rbinom(100, 1, 0.5)
# don't need to provide outcome
# function will assume each observation gets equal mass
dataHolder(x = x, z = z)</pre>
```

DataSim

R6 Data Generating Parent Class

# Description

R6 Data Generating Parent Class

R6 Data Generating Parent Class

#### **Details**

Can be used to make your own data simulation class. Should have the same slots listed in this class at a minimum, but you can add your own, of course. An easy way to do this is to make your class inherit from this one. See the example.

#### Value

An R6 object

# Methods

#### **Public methods:**

- DataSim\$get\_x()
- DataSim\$get\_y()
- DataSim\$get\_z()
- DataSim\$get\_n()
- DataSim\$get\_x1()
- DataSim\$get\_x0()
- DataSim\$get\_p()
- DataSim\$get\_tau()
- DataSim\$gen\_data()
- DataSim\$clone()

**Method** get\_x(): Gets the covariate data

Usage:

DataSim\$get\_x()

**Method** get\_y(): Gets the outcome vector

DataSim

```
Usage:
 DataSim$get_y()
Method get_z(): Gets the treatment indicator
 Usage:
 DataSim$get_z()
Method get_n(): Gets the number of observations
 Usage:
 DataSim$get_n()
Method get_x1(): Gets the covariate data for the treated individuals
 Usage:
 DataSim$get_x1()
Method get_x0(): Gets the covaraiate data for the control individuals
 Usage:
 DataSim$get_x0()
Method get_p(): Gets the dimensionality covariate data
 Usage:
 DataSim$get_p()
Method get_tau(): Gets the individual treatment effects
 Usage:
 DataSim$get_tau()
Method gen_data(): Generates the data. Default is an empty function
 Usage:
 DataSim$gen_data()
Method clone(): The objects of this class are cloneable with this method.
 Usage:
 DataSim$clone(deep = FALSE)
 deep Whether to make a deep clone.
```

# **Examples**

```
MyClass <- R6::R6Class("MyClass",
inherit = DataSim,
public = list(),
private = list())</pre>
```

df2dataHolder 17

df2dataHolder

df2dataHolder

#### **Description**

Function to turn a data.frame into a dataHolder object.

# Usage

```
df2dataHolder(
   treatment.formula,
  outcome.formula = NA_character_,
  data,
  weights = NA_real_
)
```

# **Arguments**

#### **Details**

This will take the formulas specified and transform that data.frame into a dataHolder object that is used internally by the causalOT package. Take care if you do not specify an outcome formula that you do not include the outcome in the data.frame. If you are not careful, the function may include the outcome as a covariate, which is not kosher in causal inference during the design phase.

If both outcome.formula and treatment.formula are specified, it will assume you are in the design phase, and create a combined covariate matrix to balance on the assumed treatment and outcome models.

If you are in the outcome phase of estimation, you can just provide a dummy formula for the treatment.formula like " $z \sim 0$ " just so the function can identify the treatment indicator appropriately in the data creation phase.

#### Value

Returns an object of class dataHolder()

18 entBWOptions

#### **Examples**

```
set.seed(20348)
n <- 15
d <- 3
x <- matrix(stats::rnorm(n*d), n, d)
z <- rbinom(n, 1, prob = 0.5)
y <- rnorm(n)
weights <- rep(1/n,n)
df <- data.frame(x, z, y)
dh <- df2dataHolder(
   treatment.formula = "z ~ .",
   outcome.formula = "y ~ ." ,
   data = df,
   weights = weights)</pre>
```

entBWOptions

Options for the Entropy Balancing Weights

# Description

Options for the Entropy Balancing Weights

#### Usage

```
entBWOptions(delta = NULL, grid.length = 20L, nboot = 1000L, ...)
```

# **Arguments**

A number or vector of tolerances for the balancing functions. Default is NULL which will use a grid search

grid.length The number of values to try in the grid search

The number of bootstrap samples to run during the grid search.

Arguments passed on to lbfgsb3c()

#### Value

A list of class entBWOptions with slots

- delta Delta values to try
- grid.length The number of parameters to try
- nboot Number of bootstrap samples
- solver.options A list of options passed to 'lbfgsb3c()

ESS 19

#### **Function balancing**

This method will balance functions of the covariates within some tolerance,  $\delta$ . For these functions B, we will desire

 $\frac{\sum_{i:Z_i=0} w_i B(x_i) - \sum_{j:Z_j=1} B(x_j) / n_1}{\sigma} \le \delta$ 

, where in this case we are targeting balance with the treatment group for the ATT.  $\sigma$  is the pooled standard deviation prior to balancing.

# **Examples**

```
opts <- entBWOptions(delta = 0.1)
```

**ESS** 

Effective Sample Size

# Description

Effective Sample Size

# Usage

```
ESS(x)
## S4 method for signature 'numeric'
ESS(x)
## S4 method for signature 'causalWeights'
ESS(x)
```

#### **Arguments**

Х

Either a vector of weights summing to 1 or an object of class causalWeights

# **Details**

Calculates the effective sample size as described by Kish (1965). However, this calculation has some problems and the PSIS() function should be used instead.

#### Value

Either a number denoting the effective sample size or if x is of class causalWeights, then returns a list of both values in the treatment and control groups.

# Methods (by class)

- ESS(numeric): default ESS method for numeric vectors
- ESS(causalWeights): ESS method for objects of class causalWeights

20 estimate\_effect

#### See Also

```
PSIS()
```

#### **Examples**

```
x <- rep(1/100,100)
ESS(x)</pre>
```

estimate\_effect

Estimate treatment effects

# **Description**

Estimate treatment effects

# Usage

```
estimate_effect(
  causalWeights,
  x = NULL,
  y = NULL,
  model.function,
  estimate.separately = TRUE,
  augment.estimate = FALSE,
  normalize.weights = TRUE,
  ...
)
```

#### **Arguments**

An object of class causalWeights causalWeights A dataHolder, matrix, data.frame, or object of class DataSim. See calc\_weight for more details how to input the data. If NULL, will use the info in the causalWeights argument. The outcome vector. У model.function The modeling function to use, if desired. Must take arguments "formula", "data", and "weights". Other arguments passed via . . ., the dots. estimate.separately Should the outcome model be estimated separately in each treatment group? TRUE or FALSE. augment.estimate Should an augmented, doubly robust estimator be used? normalize.weights Should the weights in the causalWeights argument be normalized to sum to one prior to effect estimation? Pass additional arguments to the outcome modeling functions.

Hainmueller 21

# Value

an object of class causalEffect

# **Examples**

Hainmueller

Hainmueller data example

# **Description**

Hainmueller data example

Hainmueller data example

# **Details**

Generates the data as described in Hainmueller (2012).

# Value

An R6 object of class DataSim

# Super class

```
causalOT::DataSim -> Hainmueller
```

#### Methods

# **Public methods:**

- Hainmueller\$gen\_data()
- Hainmueller\$gen\_x()
- Hainmueller\$gen\_y()

22 Hainmueller

```
• Hainmueller$gen_z()
  • Hainmueller$new()
  • Hainmueller$get_design()
  • Hainmueller$get_pscore()
  • Hainmueller$clone()
Method gen_data(): Generates the data
 Usage:
 Hainmueller$gen_data()
Method gen_x(): Generates the covaraiate data
 Usage:
 Hainmueller$gen_x()
Method gen_y(): Generates the outcome data
 Usage:
 Hainmueller$gen_y()
Method gen_z(): Generates the treatment indicator
 Usage:
 Hainmueller$gen_z()
Method new(): Generates the Hainmueller R6 class
 Usage:
 Hainmueller$new(
   n = 100,
   p = 6,
   param = list(),
   design = "A",
   overlap = "low",
 )
 Arguments:
 n The number of observations
 p The dimensions of the covariates. Fixed to 6.
 param The data generating parameters fed as a list.
 design One of "A" or "B". See details.
 overlap One of "high", "low", or "medium". See details.
 ... Extra arguments. Currently unused.
 Details:
   Design:
   Design "A" is the setting where the outcome is generated from a linear model, Y(0) = Y(1) =
   X_1+X_2+X_3-X_4+X_5+X_6+\eta and design "B" is where the outcome is generated from
   the non-linear model Y(0) = Y(1) = (X_1 + X_2 + X_5)^2 + \eta.
```

LaLonde 23

Overlap:

The treatment indicator is generated from  $Z=1(X_1+2X_2-2X_3-X_4-0.5X_5+X_6+\nu>0)$ , where  $\nu$  depends on the overlap selected. If overlap is "high", then  $\nu\sim N(0,100)$ . If overlap is "low", then  $\nu\sim N(0,30)$ . Finally, if overlap is "medium", then  $\nu$  is drawn from a  $\chi^2$  with 5 degrees of freedom that is scaled and centered to have mean 0.5 and variance 67.6.

```
Returns: An object of class DataSim.
```

```
Examples:
```

```
data <- Hainmueller$new(n = 100, p = 6, design = "A", overlap = "low")
data$gen_data()
print(data$get_x()[1:2,])</pre>
```

Method get\_design(): Returns the chosen design parameters

Usage:

Hainmueller\$get\_design()

Method get\_pscore(): Returns the true propensity score

Usage:

Hainmueller\$get\_pscore()

Method clone(): The objects of this class are cloneable with this method.

Usage:

Hainmueller\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

#### **Examples**

```
## ------
## Method `Hainmueller$new`
## ------
data <- Hainmueller$new(n = 100, p = 6, design = "A", overlap = "low")
data$gen_data()
print(data$get_x()[1:2,])</pre>
```

LaLonde

LaLonde data example

#### **Description**

LaLonde data example

LaLonde data example

24 LaLonde

#### **Details**

Returns the LaLonde data as used by Dehjia and Wahba. Note the data is fixed and gen\_data() will just initialize the fixed data.

#### Value

```
An R6 object of class DataSim
```

# Super class

```
causalOT::DataSim -> LaLonde
```

# Methods

#### **Public methods:**

```
• LaLonde$gen_data()
```

- LaLonde\$get\_tau()
- LaLonde\$gen\_x()
- LaLonde\$gen\_y()
- LaLonde\$gen\_z()
- LaLonde\$new()
- LaLonde\$get\_design()
- LaLonde\$clone()

```
Method gen_data(): Sets up the data
```

```
Usage:
```

LaLonde\$gen\_data()

Method get\_tau(): Returns the experimental treatment effect, \$1794

```
Usage:
```

LaLonde\$get\_tau()

**Method** gen\_x(): Sets up the covariate data

Usage:

LaLonde\$gen\_x()

**Method** gen\_y(): Sets up the outcome data

Usage:

LaLonde\$gen\_y()

Method gen\_z(): Sets up the treatment indicator

Usage:

LaLonde\$gen\_z()

Method new(): Initializes the LaLonde object.

Usage:

LaLonde 25

```
LaLonde$new(n = NULL, p = NULL, param = list(), design = "NSW", ...)
       Arguments:
       n Not used. Maintained for symmetry with other DataSim objects.
       p Not used. Maintained for symmetry with other DataSim objects.
       param Not used. Maintained for symmetry with other DataSim objects.
       design One of "NSW" or "Full". "NSW" uses the original experimental data from the job
           training program while option "Full" uses the treated individuals from LaLonde's study and
           compares them to individuals from the Current Population Survey as controls.
       ... Not used.
       Examples:
       nsw <- LaLonde$new(design = "NSW")</pre>
       nsw$gen_data()
       nsw$get_n()
       obs.study <- LaLonde$new(design = "Full")</pre>
       obs.study$gen_data()
       obs.study$get_n()
     Method get_design(): Returns the chosen design parameters
       Usage:
       LaLonde$get_design()
     Method clone(): The objects of this class are cloneable with this method.
       Usage:
       LaLonde$clone(deep = FALSE)
       Arguments:
       deep Whether to make a deep clone.
Examples
```

```
## Method `LaLonde$new`
nsw <- LaLonde$new(design = "NSW")</pre>
nsw$gen_data()
nsw$get_n()
obs.study <- LaLonde$new(design = "Full")</pre>
obs.study$gen_data()
obs.study$get_n()
```

26 Measure

	1 7	1	
mean	na	ı an	ce

Standardized absolute mean difference calculations

# Description

This function will calculate the difference in means between treatment groups standardized by the pooled standard-deviation of the respective covariates.

# Usage

```
mean\_balance(x = NULL, z = NULL, weights = NULL, ...)
```

# **Arguments**

X	Either a matrix, an object of class dataHolder, or an object of class DataSim
Z	A integer vector denoting the treatments of each observations. Can be null if x is a DataSim object or already of class dataHolder.
weights	An object of class causalWeights.
	Not used at this time.

#### Value

A vector of mean balances

# **Examples**

```
n <- 100
p <- 6
x <- matrix(stats::rnorm(n * p), n, p)
z <- stats::rbinom(n, 1, 0.5)
weights <- calc_weight(x = x, z = z, estimand = "ATT", method = "Logistic")
mb <- mean_balance(x = x, z = z, weights = weights)
print(mb)</pre>
```

Measure

An R6 Class for setting up measures

# **Description**

An R6 Class for setting up measures

Measure 27

#### Usage

```
Measure(
    x,
    weights = NULL,
    probability.measure = TRUE,
    adapt = c("none", "weights", "x"),
    balance.functions = NA_real_,
    target.values = NA_real_,
    dtype = NULL,
    device = NULL
)
```

#### **Arguments**

x The data points

weights The empirical measure. If NULL, assigns equal weight to each observation

probability.measure

Is the empirical measure a probability measure? Default is TRUE.

adapt Should we try to adapt the data ("x"), the weights ("weights"), or neither ("none").

Default is "none".

balance.functions

A matrix of functions of the covariates to target for mean balance. If NULL and

target.values are provided, will use the data in x.

target.values The targets for the balance functions. Should be the same length as columns in

balance. functions.

dtype The torch\_tensor dtype or NULL.

device The device to have the data on. Should be result of torch::torch\_device()

or NULL.

#### Value

Returns a Measure object

# **Public fields**

```
balance_functions the functions of the data that we want to adjust towards the targets balance_target the values the balance_functions are targeting adapt. What aspect of the data will be adapted. One of "none", "weights", or "x". device the torch::torch_device of the data. dtype the torch::torch_dtype of the data.

n the rows of the covariates, x.

d the columns of the covariates, x.

probability_measure is the measure a probability measure?
```

28 Measure

# **Active bindings**

```
grad gets or sets gradient
init_weights returns the initial value of the weights
init_data returns the initial value of the data
requires_grad checks or turns on/off gradient
weights gets or sets weights
x Gets or sets the data
```

#### Methods

#### **Public methods:**

- Measure\$detach()
- Measure\$get\_weight\_parameters()
- Measure\$clone()

**Method** detach(): generates a deep clone of the object without gradients.

```
Usage:
Measure$detach()
```

**Method** get\_weight\_parameters(): Makes a copy of the weights parameters.

```
Usage:
```

```
Measure$get_weight_parameters()
```

**Method** clone(): The objects of this class are cloneable with this method.

```
Usage:
Measure$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

# **Examples**

```
if(torch::torch_is_installed()) {
m <- Measure(x = matrix(0, 10, 2), adapt = "none")
print(m)
m$x
m$x <- matrix(1,10,2) # must have same dimensions
m$x
m$weights
m$weights <- 1:10/sum(1:10)
m$weights

# with gradients
m <- Measure(x = matrix(0, 10, 2), adapt = "weights")
m$requires_grad # TRUE
m$requires_grad <- "none" # turns off
m$requires_grad # FALSE</pre>
```

```
m$requires_grad <- "x"
m$requires_grad # TRUE
m <- Measure(matrix(0, 10, 2), adapt = "none")
m$grad # NULL
m <- Measure(matrix(0, 10, 2), adapt = "weights")
loss <- sum(m$weights * 1:10)
loss$backward()
m$grad
# note the weights gradient is on the log softmax scale
#and the first parameter is fixed for identifiability
m$grad <- rep(1,9)
m$grad
}</pre>
```

OTProblem

Object Oriented OT Problem

# **Description**

Object Oriented OT Problem

#### Usage

```
OTProblem(measure_1, measure_2, ...)
```

#### **Arguments**

```
measure_1 An object of class Measure
measure_2 An object of class Measure
... Not used at this time
```

#### Value

An R6 object of class "OTProblem"

# **Public fields**

```
device the torch::torch_device() of the data.

dtype the torch::torch_dtype of the data.

selected_delta the delta value selected after choose_hyperparameters

selected_lambda the lambda value selected after choose_hyperparameters
```

#### **Active bindings**

loss prints the current value of the objective. Only available after the OTProblem\$solve() method has been run

penalty Returns a list of the lambda and delta penalities that will be iterated through. To set these values, use the OTProblem\$setup\_arguments() function.

# Methods

```
Public methods:
  • OTProblem$add()
  • OTProblem$subtract()
  • OTProblem$multiply()
  • OTProblem$divide()
  • OTProblem$setup_arguments()
  • OTProblem$solve()
  • OTProblem$choose_hyperparameters()
  • OTProblem$info()
  • OTProblem$clone()
Method add(): adds o2 to the OTProblem
 Usage:
 OTProblem$add(o2)
 Arguments:
 o2 A number or object of class OTProblem
Method subtract(): subtracts o2 from OTProblem
 Usage:
 OTProblem$subtract(o2)
 Arguments:
 o2 A number or object of class OTProblem
Method multiply(): multiplies OTProblem by o2
 Usage:
 OTProblem$multiply(o2)
 Arguments:
 o2 A number or an object of class OTProblem
Method divide(): divides OTProblem by o2
 Usage:
 OTProblem$divide(o2)
 Arguments:
 o2 A number or object of class OTProblem
Method setup_arguments():
 Usage:
 OTProblem$setup_arguments(
       lambda,
       delta,
```

grid.length = 7L, cost.function = NULL,

```
p = 2,
        cost.online = "auto",
        debias = TRUE,
        diameter = NULL,
        ot_niter = 1000L,
        ot_tol = 0.001
      )
 Arguments:
 lambda The penalty parameters to try for the OT problems. If not provided, function will select
 delta The constraint paramters to try for the balance function problems, if any
 grid.length The number of hyperparameters to try if not provided
 cost.function The cost function for the data. Can be any function that takes arguments x1,
     x2, p. Defaults to the Euclidean distance
 p The power to raise the cost matrix by. Default is 2
 cost.online Should online costs be used? Default is "auto" but "tensorized" stores the cost
     matrix in memory while "online" will calculate it on the fly.
 debias Should debiased OT problems be used? Defaults to TRUE
 diameter Diameter of the cost function.
 ot_niter Number of iterations to run the OT problems
 ot_tol The tolerance for convergence of the OT problems
 Returns: NULL
 Examples:
  otsetup\_arguments(lambda = c(1000,10))
Method solve(): Solve the OTProblem at each parameter value. Must run setup arguments
first.
 Usage:
 OTProblem$solve(
        niter = 1000L,
        tol = 1e-05,
        optimizer = c("torch", "frank-wolfe"),
        torch_optim = torch::optim_lbfgs,
        torch_scheduler = torch::lr_reduce_on_plateau,
        torch_args = NULL,
        osqp_args = NULL,
        quick.balance.function = TRUE
      )
 Arguments:
 niter The nubmer of iterations to run solver at each combination of hyperparameter values
 tol The tolerance for convergence
 optimizer The optimizer to use. One of "torch" or "frank-wolfe"
 torch_optim The torch_optimizer to use. Default is torch::optim_lbfgs
```

```
torch_scheduler The torch::lr_scheduler to use. Default is torch::lr_reduce_on_plateau
 torch_args Arguments passed to the torch optimizer and scheduler
 osqp_args Arguments passed to osqp::osqpSettings() if appropriate
 quick.balance.function Should osqp::osqp() be used to select balance function constraints
     (delta) or not. Default true.
 Examples:
  ot$solve(niter = 1, torch_optim = torch::optim_rmsprop)
Method choose_hyperparameters(): Selects the hyperparameter values through a bootstrap
algorithm
 Usage:
 OTProblem$choose_hyperparameters(
        n_boot_lambda = 100L,
        n_{boot_{delta}} = 1000L,
        lambda_bootstrap = Inf
      )
 Arguments:
 n_boot_lambda The number of bootstrap iterations to run when selecting lambda
 n_boot_delta The number of bootstrap iterations to run when selecting delta
 lambda_bootstrap The penalty parameter to use when selecting lambda. Higher numbers run
     faster.
 Examples:
  ot$choose_hyperparameters(n_boot_lambda = 10,
                                                     n_{boot_delta} = 10,
                                                     lambda_bootstrap = Inf)
Method info(): Provides diagnostics after solve and choose_hyperparameter methods have
been run.
 Usage:
 OTProblem$info()
 Returns: a list with slots
   • loss the final loss values
   • iterations The number of iterations run for each combination of parameters
   • balance.function.differences The final differences in the balance functions
   • hyperparam.metrics A list of the bootstrap evaluation for delta and lambda values
 Examples:
  ot$info()
Method clone(): The objects of this class are cloneable with this method.
 Usage:
 OTProblem$clone(deep = FALSE)
 Arguments:
 deep Whether to make a deep clone.
```

ot\_distance 33

#### **Examples**

```
## -----
## Method `OTProblem(measure_1, measure_2)`
if (torch::torch_is_installed()) {
 # setup measures
 x \leftarrow matrix(1, 100, 10)
 m1 \leftarrow Measure(x = x)
 y <- matrix(2, 100, 10)
 m2 <- Measure(x = y, adapt = "weights")</pre>
 z \leftarrow matrix(3,102, 10)
 m3 \leftarrow Measure(x = z)
 # setup OT problems
 ot1 <- OTProblem(m1, m2)
 ot2 <- OTProblem(m3, m2)
 ot <-0.5 * ot1 + 0.5 * ot2
 print(ot)
## Method `OTProblem$setup_arguments`
 ot$setup_arguments(lambda = 1000)
## Method `OTProblem$solve`
 ot$solve(niter = 1, torch_optim = torch::optim_rmsprop)
## -----
## Method `OTProblem$choose_hyperparameters`
 ot$choose_hyperparameters(n_boot_lambda = 1,
                         n_{boot_delta} = 1,
                         lambda_bootstrap = Inf)
## -----
## Method `OTProblem$info`
ot$info()
```

ot\_distance

# **Description**

**Optimal Transport Distance** 

# Usage

```
ot_distance(
  x1,
 x2 = NULL,
 a = NULL
 b = NULL,
 penalty,
 p = 2,
  cost = NULL,
  debias = TRUE,
 online.cost = "auto",
  diameter = NULL,
 niter = 1000,
  tol = 1e-07
)
## S3 method for class 'causalWeights'
ot_distance(
 x1,
 x2 = NULL
 a = NULL
 b = NULL
 penalty,
  p = 2,
  cost = NULL,
  debias = TRUE,
 online.cost = "auto",
  diameter = NULL,
 niter = 1000,
  tol = 1e-07
## S3 method for class 'matrix'
ot_distance(
 x1,
 x2,
  a = NULL,
 b = NULL,
  penalty,
  p = 2,
  cost = NULL,
  debias = TRUE,
  online.cost = "auto",
  diameter = NULL,
```

ot\_distance 35

```
niter = 1000,
 tol = 1e-07
)
## S3 method for class 'array'
ot_distance(
 x1,
 x2,
 a = NULL
 b = NULL,
 penalty,
 p = 2,
 cost = NULL,
 debias = TRUE,
 online.cost = "auto",
 diameter = NULL,
 niter = 1000,
 tol = 1e-07
)
## S3 method for class 'torch_tensor'
ot_distance(
 x1,
 x2,
 a = NULL
 b = NULL,
 penalty,
 p = 2,
 cost = NULL,
 debias = TRUE,
 online.cost = "auto",
 diameter = NULL,
 niter = 1000,
  tol = 1e-07
)
```

# **Arguments**

x1	Either an object of class causalWeights or a matrix of the covariates in the first sample
x2	NULL or a matrix of the covariates in the second sample.
a	Empirical measure of the first sample. If NULL, assumes each observation gets equal mass. Ignored for objects of class causalWeights.
b	Empirical measure of the second sample. If NULL, assumes each observation gets equal mass. Ignored for objects of class causalWeights.
penalty	The penalty of the optimal transport distance to use. If missing or NULL, the function will try to guess a suitable value depending if debias is TRUE or FALSE.

36 plot.causalWeights

p	$L_p$ distance metric power
cost	Supply your own cost function. Should take arguments x1, x2, and p.
debias	TRUE or FALSE. Should the debiased optimal transport distances be used.
online.cost	How to calculate the distance matrix. One of "auto", "tensorized", or "online".
diameter	The diameter of the metric space, if known. Default is NULL.
niter	The maximum number of iterations for the Sinkhorn updates
tol	The tolerance for convergence

#### Value

For objects of class matrix, numeric value giving the optimal transport distance. For objects of class causalWeights, results are returned as a list for before ('pre') and after adjustment ('post').

# Methods (by class)

- ot\_distance(causalWeights): method for causalWeights class
- ot\_distance(matrix): method for matrices
- ot\_distance(array): method for arrays
- ot\_distance(torch\_tensor): method for torch\_tensors

# **Examples**

```
if ( torch::torch_is_installed()) {
    x <- matrix(stats::rnorm(10*5), 10, 5)
    z <- stats::rbinom(10, 1, 0.5)
    weights <- calc_weight(x = x, z = z, method = "Logistic", estimand = "ATT")
    ot1 <- ot_distance(x1 = weights, penalty = 100,
    p = 2, debias = TRUE, online.cost = "auto",
    diameter = NULL)
    ot2<- ot_distance(x1 = x[z==0, ], x2 = x[z == 1,],
    a= weights@w0/sum(weights@w0), b = weights@w1,
    penalty = 100, p = 2, debias = TRUE, online.cost = "auto", diameter = NULL)
    all.equal(ot1$post, ot2)
}</pre>
```

plot.causalWeights plot.causalWeights

#### Description

plot.causalWeights

plot.causalWeights 37

## Usage

```
## S3 method for class 'causalWeights'
plot(
    x,
    r_eff = NULL,
    penalty,
    p = 2,
    cost = NULL,
    debias = TRUE,
    online.cost = "auto",
    diameter = NULL,
    niter = 1000,
    tol = 1e-07,
    ...
)
```

# Arguments

X	A causalWeights object
r_eff	The $r_{ m eff}$ to use for the PSIS_diag() function.
penalty	The penalty of the optimal transport distance to use. If missing or NULL, the function will try to guess a suitable value depending if debias is TRUE or FALSE.
p	$L_p$ distance metric power
cost	Supply your own cost function. Should take arguments x1, x2, and p.
debias	TRUE or FALSE. Should the debiased optimal transport distances be used.
online.cost	How to calculate the distance matrix. One of "auto", "tensorized", or "online".
diameter	The diameter of the metric space, if known. Default is NULL.
niter	The maximum number of iterations for the Sinkhorn updates
tol	The tolerance for convergence
•••	Not used at this time

## **Details**

The plot method first calls summary.causalWeights on the causalWeights object. Then plots the diagnostics from that summary object.

## Value

The plot method returns an invisible object of class summary\_causalWeights.

#### See Also

```
summary.causalWeights()
```

38 pph

pph

An external control trial of treatments for post-partum hemorrhage

## **Description**

A dataset evaluating treatments for post-partum hemorrhage. The data contain treatment groups receiving misoprostol vs potential controls from other locations that received only oxytocin. The data is stored as a numeric matrix.

## Usage

data(pph)

#### **Format**

A matrix with 802 rows and 17 variables

#### **Details**

The variables are as follows:

- cum\_blood\_20m. The outcome variable denoting cumulative blood loss in mL 20 minutes after the diagnosis of post-partum hemorrhage (650 2000).
- tx. The treatment indicator of whether an individual received misoprostol (1) or oxytocin (0).
- age. the mother's age in years (15-43).
- no\_educ. whether a woman had no education (1) or some education (0).
- num\_livebirth. the number of previous live births.
- cur\_married. whether a mother is currently married (1 = yes, 0 = no).
- gest\_age. the gestational age of the fetus in weeks (35 43).
- prev\_pphyes. whether the woman has had a previous post-partum hemorrahge.
- hb\_test. the woman's hemoglobin in mg/dL (7 15).
- induced\_laboryes. whether labor was induced (1 = yes, 0 = no).
- augmented\_laboryes. whether labor was augmented (1 = yes, 0 = no).
- early\_cordclampyes. whether the umbilical cord was clamped early (1 = yes, 0 = no).
- control\_cordtractionyes. whether cord traction was controlled (1 = yes, 0 = no).
- uterine\_massageyes. whether a uterine massage was given (1 = yes, 0 = no).
- placenta. whether placenta was delivered before treatment given (1 = yes, 0 = no).
- bloodlossattx. amount of blood lost when treatment given (500 mL 1800 mL)
- sitecode. Which site is the individual from? (1 = Cairo, Egypt, 2 = Turkey, 3 = Hocmon, Vietnam, 4 = Cuchi, Vietnam, and 5 Burkina Faso).

predict.bp 39

#### **Source**

Data from the following Harvard Dataverse:

• Winikoff, Beverly, 2019, "Two randomized controlled trials of misoprostol for the treatment of postpartum hemorrhage", https://doi.org/10.7910/DVN/ETHH4N, Harvard Dataverse, V1.

The data was originally analyzed in

• Blum, J. et al. Treatment of post-partum haemorrhage with sublingual misoprostol versus oxytocin in women receiving prophylactic oxytocin: a double-blind, randomised, non-inferiority trial. The Lancet 375, 217–223 (2010).

predict.bp

Predict method for barycentric projection models

# Description

Predict method for barycentric projection models

#### Usage

```
## $3 method for class 'bp'
predict(
   object,
   newdata = NULL,
   source.sample,
   cost_function = NULL,
   niter = 1000,
   tol = 1e-07,
   ...
)
```

#### **Arguments**

```
object An object of class "bp"

newdata a data.frame containing new observations

source.sample a vector giving the sample each observations arise from

cost_function a cost metric between observations

niter number of iterations to run the barycentric projection for powers > 2.

tol Tolerance on the optimization problem for projections with powers > 2.

... Dots passed to the lbfgs method in the torch package.
```

40 print.dataHolder

#### **Examples**

```
if(torch::torch_is_installed()) {
set.seed(23483)
n <- 2<sup>5</sup>
pp <- 6
overlap <- "low"</pre>
design <- "A"
estimate <- "ATT"
power <- 2
data <- causalOT::Hainmueller$new(n = n, p = pp,</pre>
design = design, overlap = overlap)
data$gen_data()
weights <- causalOT::calc_weight(x = data,</pre>
  z = NULL, y = NULL,
  estimand = estimate,
 method = "NNM")
 df <- data.frame(y = data$get_y(), z = data$get_z(), data$get_x())</pre>
 # undebiased
 fit <- causalOT::barycentric_projection(y ~ ., data = df,</pre>
    weight = weights,
    separate.samples.on = "z", niter = 2)
 #debiased
 fit_d <- causalOT::barycentric_projection(y ~ ., data = df,</pre>
    weight = weights,
    separate.samples.on = "z", debias = TRUE, niter = 2)
 # predictions, without new data
 undebiased_predictions <- predict(fit, source.sample = df$z)</pre>
 debiased_predictions <- predict(fit_d, source.sample = df$z)</pre>
 isTRUE(all.equal(unname(undebiased_predictions), df$y)) # FALSE
 isTRUE(all.equal(unname(debiased_predictions), df$y)) # TRUE
 }
```

print.dataHolder

print.dataHolder

#### Description

print.dataHolder

#### Usage

```
## S3 method for class 'dataHolder' print(x, ...)
```

PSIS 41

# Arguments

x dataHolder object

... Not used

**PSIS** 

Pareto-Smoothed Importance Sampling

## **Description**

Pareto-Smoothed Importance Sampling

# Usage

```
PSIS(x, r_eff = NULL, ...)
## S4 method for signature 'numeric'
PSIS(x, r_eff = NULL, ...)
## S4 method for signature 'causalWeights'
PSIS(x, r_eff = NULL, ...)
## S4 method for signature 'list'
PSIS(x, r_eff = NULL, ...)
PSIS_diag(x, ...)
## S4 method for signature 'numeric'
PSIS_diag(x, r_eff = NULL)
## S4 method for signature 'causalWeights'
PSIS_diag(x, r_eff = NULL)
## S4 method for signature 'causalPSIS'
PSIS_diag(x, ...)
## S4 method for signature 'list'
PSIS_diag(x, r_eff = NULL)
## S4 method for signature 'psis'
PSIS_diag(x, r_eff = NULL)
```

## Arguments

x For PSIS(), a vector of weights, an object of class causalWeights, or a list with slots "w0" and "w1". For PSIS\_diag, the results of a run of PSIS().

42 PSIS

r\_eff

A vector of relative effective sample size with one estimate per observation. If providing an object of class causalWeights, should be a list of vectors with one vector for each sample. See psis() from the loo package for more details. Updates to the loo package now make it so this parameter should be ignored.

... Arguments passed to the psis() function.

#### **Details**

Acts as a wrapper to the psis() function from the loo package. It is built to handle the data types found in this package. This method is preferred to the ESS() function in causalOT since the latter is prone to error (infinite variances) but will not give good any indication that the estimates are problematic.

## Value

For PSIS(), returns a list. See psis() from loo for a description of the outputs. Will give the log of the smoothed weights in slot log\_weights, and in the slot diagnostics, it will give the pareto\_k parameter (see the pareto-k-diagnostic page) and the n\_eff estimates. PSIS\_diag() returns the diagnostic slot from an object of class "psis".

# Methods (by class)

- PSIS(numeric): numeric weights
- PSIS(causalWeights): object of class causalWeights
- PSIS(list): list of weights
- PSIS\_diag(numeric): numeric weights
- PSIS\_diag(causalWeights): object of class causalWeights diagnostics
- PSIS\_diag(causalPSIS): diagnostics from the output of a previous call to PSIS
- PSIS\_diag(list): a list of objects
- PSIS\_diag(psis): output of PSIS function

#### See Also

ESS()

## **Examples**

```
x <- runif(100)
w <- x/sum(x)

res <- PSIS(x = w, r_eff = 1)
PSIS_diag(res)</pre>
```

sbwOptions 43

sbw0	pti	ions

Options for the SBW method

#### Description

Options for the SBW method

## Usage

```
sbwOptions(delta = NULL, grid.length = 20L, nboot = 1000L, ...)
```

#### **Arguments**

A number or vector of tolerances for the balancing functions. Default is NULL which will use a grid search

grid.length The number of values to try in the grid search

The number of bootstrap samples to run during the grid search.

Arguments passed on to osqpSettings()

#### Value

A list of class sbwOptions with slots

- delta Delta values to try
- grid.length The number of parameters to try
- sumto1 Forced to be TRUE. Weights will always sum to 1.
- nboot Number of bootstrap samples
- solver.optionsA list with arguments passed to osqpSettings()

## **Function balancing**

This method will balance functions of the covariates within some tolerance,  $\delta$ . For these functions B, we will desire

$$\frac{\sum_{i:Z_i=0} w_i B(x_i) - \sum_{j:Z_j=1} B(x_j) / n_1}{\sigma} \le \delta$$

, where in this case we are targeting balance with the treatment group for the ATT.  $\sigma$  is the pooled standard deviation prior to balancing.

#### **Examples**

```
opts <- sbwOptions(delta = 0.1)</pre>
```

scmOptions

Options for the SCM Method

# Description

Options for the SCM Method

## Usage

```
scmOptions(...)
```

## **Arguments**

... Arguments passed to the osqpSettings() function which solves the problem.

## **Details**

Options for the solver used in the optimization of the Synthetic Control Method of Abadie and Gardeazabal (2003).

### Value

A list with arguments to pass to osqpSettings()

# **Examples**

```
opts <- scmOptions()</pre>
```

summary.causalWeights Summary diagnostics for causalWeights

# Description

Summary diagnostics for causalWeights print.summary\_causalWeights plot.summary\_causalWeights

## Usage

```
## S3 method for class 'causalWeights'
summary(
 object,
 r_{eff} = NULL,
 penalty,
 p = 2,
 cost = NULL,
 debias = TRUE,
 online.cost = "auto",
 diameter = NULL,
 niter = 1000,
  tol = 1e-07,
)
## S3 method for class 'summary_causalWeights'
print(x, ...)
## S3 method for class 'summary_causalWeights'
plot(x, ...)
```

#### **Arguments**

object	an object of class causalWeights
r_eff	The r_eff used in the PSIS calculation. See PSIS_diag()
penalty	The penalty parameter to use
р	The power of the Lp distance to use. Overridden by argument cost.
cost	A user supplied cost function. Should take arguments x1, x2, p.
debias	Should debiased optimal transport distances be used. TRUE or FALSE
online.cost	Should the cost be calculated online? One of "auto", "tensorized", or "online".
diameter	the diameter of the covariate space. Default is NULL.
niter	the number of iterations to run the optimal transport distances
tol	the tolerance for convergence for the optimal transport distances
	Not used
x	an object of class "summary_causalWeights"

#### Value

The summary method returns an object of class "summary\_causalWeights".

### **Functions**

- print(summary\_causalWeights): print method
- plot(summary\_causalWeights): plot method

46 vcov.causalEffect

#### **Examples**

 $supported\_methods$ 

Supported Methods

# **Description**

Supported Methods

## Usage

```
supported_methods()
```

#### Value

A character list with supported methods. Note "COT" is the same as "Wasserstein". We provide the second name for backwards compatibility.

## **Examples**

```
supported_methods()
```

vcov.causalEffect

Get the variance of a causalEffect

#### Description

Get the variance of a causalEffect

#### Usage

```
## S3 method for class 'causalEffect'
vcov(object, ...)
```

vcov.causalEffect 47

## **Arguments**

object An object of class causalEffect

... Passed on to the sandwich estimator if there is a model fit that supports one

#### Value

The variance of the treatment effect as a matrix

# **Examples**

```
# set-up data
set.seed(1234)
data <- Hainmueller$new()
data$gen_data()

# calculate quantities
weight <- calc_weight(data, estimand = "ATT", method = "Logistic")
tx_eff <- estimate_effect(causalWeights = weight)
vcov(tx_eff)</pre>
```

# **Index**

* datasets	osqpSettings(), 43, 44		
pph, 38	ot_distance, 33		
	OTProblem, 29		
barycentric_projection, 3			
	pareto-k-diagnostic,42		
$calc_weight, 5, 20$	plot.causalWeights, 36		
causalEffect, 8, 21, 47	plot.summary_causalWeights		
causalOT::DataSim, <i>12</i> , <i>21</i> , <i>24</i>	(summary.causalWeights), 44		
causalWeights, 3, 7, 19, 20, 26, 35, 37, 41,	pph, 38		
42, 45	predict.bp, 39		
causalWeights-class, 7	print.dataHolder,40		
CBPS(), 6	print.summary_causalWeights		
<pre>coef.causalEffect, 8</pre>	(summary.causalWeights), 44		
cotOptions, 9	PSIS, 41		
cotOptions(), 6	PSIS(), 19, 20		
CRASH3, 12	psis(), 42		
	PSIS, causalWeights-method (PSIS), 41		
dataHolder, 4, 6, 14, 26	PSIS, list-method (PSIS), 41		
dataHolder(), 17	PSIS, numeric-method (PSIS), 41		
DataSim, 6, 12, 14, 15, 21, 23, 24	PSIS_diag (PSIS), 41		
df2dataHolder, 17	PSIS_diag(), 37, 45		
	PSIS_diag, causalPSIS-method (PSIS), 41		
entBWOptions, 18	PSIS_diag, causalWeights-method (PSIS),		
entBWOptions(), 6	41		
ESS, 19	PSIS_diag,list-method(PSIS),41		
ESS(), 42	PSIS_diag, numeric-method (PSIS), 41		
ESS, causalWeights-method (ESS), 19	PSIS_diag, psis-method (PSIS), 41		
ESS, numeric-method (ESS), 19	1 313_d1dg, p313		
estimate_effect, 20	R6, 12, 15, 21, 24		
<pre>estimate_effect(), 7</pre>	10, 12, 13, 21, 27		
	sbwOptions, 43		
Hainmueller, 21	sbwOptions(), 6		
Lalanda 22	scmOptions, 44		
LaLonde, 23	scmOptions(), 6		
1bfgsb3c(), <i>18</i>	summary.causalWeights,44		
mean_balance, 26	summary.causalWeights(), 37		
Measure, 26, 29	supported_methods, 46		
Heasul 6, 20, 27	supported_methods(), 6		
osqp::osqp(), 32	Supported_methods(), o		
osqp::osqpSettings(), 32	<pre>torch::lr_multiplicative(), 10</pre>		

INDEX 49

```
torch::lr_reduce_on_plateau, 32
torch::lr_scheduler, 32
torch::optim_lbfgs, 31
torch::optim_lbfgs(), 10
torch::optim_rmsprop(), 10
torch::torch_device, 27
torch::torch_device(), 27, 29
torch::torch_dtype, 27, 29
vcov.causalEffect, 46
```