

# Package ‘clr’

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**Type** Package

**Title** Curve Linear Regression via Dimension Reduction

**Version** 0.1.2

**Author** Amandine Pierrot

with contributions and/or help from Qiwei Yao, Haeran Cho, Yannig Goude and Tony Aldon.

**Maintainer** Amandine Pierrot <amandine.m.pierrot@gmail.com>

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**Description** A new methodology for linear regression with both curve response and curve regressors, which is described in Cho, Goude, Brossat and Yao (2013) <[doi:10.1080/01621459.2012.722900](https://doi.org/10.1080/01621459.2012.722900)> and (2015) <[doi:10.1007/978-3-319-18732-7\\_3](https://doi.org/10.1007/978-3-319-18732-7_3)>. The key idea behind this methodology is dimension reduction based on a singular value decomposition in a Hilbert space, which reduces the curve regression problem to several scalar linear regression problems.

**License** LGPL (>= 2.0)

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 6.1.1

**Depends** R (>= 2.10)

**Imports** magrittr, lubridate, dplyr, stats

**NeedsCompilation** no

**Repository** CRAN

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clr-package	<i>Curve Linear Regression</i>
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**Description**

clr provides functions for curve linear regression via dimension reduction.

**Details**

The package implements a new methodology for linear regression with both curve response and curve regressors, which is described in Cho et al. (2013) and Cho et al. (2015). The CLR model performs a data-driven dimension reduction, based on a singular value decomposition in a Hilbert Space, as well as a data transformation so that the relationship between the transformed data is linear and can be captured by simple regression models.

**Author(s)**

Amandine Pierrot <amandine.m.pierrot@gmail.com>  
with contributions and help from Qiwei Yao, Haeran Cho, Yannig Goude and Tony Aldon.

**References**

These provide details for the underlying clr methods.

Cho, H., Y. Goude, X. Brossat, and Q. Yao (2013) Modelling and Forecasting Daily Electricity Load Curves: A Hybrid Approach. *Journal of the American Statistical Association* 108: 7-21.

Cho, H., Y. Goude, X. Brossat, and Q. Yao (2015) Modelling and Forecasting Daily Electricity Load via Curve Linear Regression. In *Modeling and Stochastic Learning for Forecasting in High Dimension*, edited by Anestis Antoniadis and Xavier Brossat, 35-54, Springer.

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clr	<i>Curve Linear Regression via dimension reduction</i>
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**Description**

Fits a curve linear regression (CLR) model to data, using dimension reduction based on singular value decomposition.

**Usage**

```
clr(Y, X, clust = NULL, qx_estimation = list(method = "pctvar", param =
  0.999), ortho_Y = TRUE, qy_estimation = list(method = "pctvar", param
  = 0.999), d_estimation = list(method = "cor", param = 0.5))
```

**Arguments**

Y	An object of class <code>clrdata</code> or <code>matrix</code> , of the response curves (one curve a row).
X	An object of class <code>clrdata</code> or <code>matrix</code> , of the regressor curves (one curve a row).
clust	If needed, a list of row indices for each cluster, to obtain (approximately) homogeneous dependence structure inside each cluster.
qx_estimation	A list containing both values for 'method' (among 'ratio', 'ratioM', 'pctvar', 'fixed') and for 'param' (depending on the selected method), in order to choose how to estimate the dimension of X (in the sense that its Karhunen-Loève decomposition has qx terms only).
ortho_Y	If TRUE then Y is orthogonalized.
qy_estimation	Same as for qx_estimation, if ortho_Y is set to TRUE.
d_estimation	A list containing both values for 'method' (among 'ratio', 'pctvar', 'cor') and for 'param' (depending on the selected method), in order to choose how to estimate the correlation dimension.

**Value**

An object of class `clr`, which can be used to compute predictions. This `clr` object is a list of lists: one list by cluster of data, each list including:

residuals	The matrix of the residuals of <code>d_hat</code> simple linear regressions.
b_hat	The vector of the estimated coefficient of the <code>d_hat</code> simple straight line regressions.
eta	The matrix of the projections of X.
xi	The matrix of the projections of Y.
qx_hat	The estimated dimension of X.
qy_hat	The estimated dimension of Y.
d_hat	The estimated correlation dimension.
X_mean	The mean of the regressor curves.
X_sd	The standard deviation of the regressor curves.
Y_mean	The mean of the response curves.
ortho_Y	The value which was selected for <code>ortho_Y</code> .
GAMMA	The standardized transformation for X.
INV_DELTA	The standardized transformation for Y to predict if <code>ortho_Y</code> was set to TRUE.
phi	The eigenvectors for Y to predict if <code>ortho_Y</code> was set to FALSE.
idx	The indices of the rows selected from X and Y for the current cluster.

**See Also**

[clr-package](#), [clrdata](#) and [predict.clr](#).

**Examples**

```
library(clr)
data(gb_load)
data(clust_train)

clr_load <- clrdata(x = gb_load$ENGLAND_WALES_DEMAND,
                   order_by = gb_load$TIMESTAMP,
                   support_grid = 1:48)

## data cleaning: replace zeros with NA
clr_load[rowSums((clr_load == 0) * 1) > 0, ] <- NA
matplot(t(clr_load), ylab = 'Daily loads', type = 'l')

Y <- clr_load[2:nrow(clr_load), ]
X <- clr_load[1:(nrow(clr_load) - 1), ]

begin_pred <- which(substr(rownames(Y), 1, 4) == '2016')[1]
Y_train <- Y[1:(begin_pred - 1), ]
X_train <- X[1:(begin_pred - 1), ]

## Example without any cluster
model <- clr(Y = Y_train, X = X_train)

## Example with clusters
model <- clr(Y = Y_train, X = X_train, clust = clust_train)
```

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clrdata

*Create an object of clrdata*

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**Description**

clrdata is used to create a clrdata object from raw data inputs.

**Usage**

```
clrdata(x, order_by, support_grid)
```

**Arguments**

x	A vector containing the time series values
order_by	A corresponding vector of unique time-dates - must be of class 'POSIXct'
support_grid	A vector corresponding to the support grid of functional data

**Value**

An object of class `clrdata` with one function a row. As it inherits the `matrix` class, all `matrix` methods remain valid. If time-dates are missing in `x`, corresponding NA functions are added by `clrdata` so that time sequence is preserved between successive rows.

**Examples**

```
library(clr)
data(gb_load)

clr_load <- clrdata(x = gb_load$ENGLAND_WALES_DEMAND,
                   order_by = gb_load$TIMESTAMP,
                   support_grid = 1:48)

head(clr_load)
dim(clr_load)
summary(clr_load)

matplot(t(clr_load), ylab = 'Daily loads', type = 'l')
lines(colMeans(clr_load, na.rm = TRUE),
      col = 'black', lwd = 2)

clr_weather <- clrdata(x = gb_load$TEMPERATURE,
                      order_by = gb_load$TIMESTAMP,
                      support_grid = 1:48)

summary(clr_weather)
plot(1:48,
     colMeans(clr_weather, na.rm = TRUE),
     xlab = 'Instant', ylab = 'Mean of temperatures',
     type = 'l', col = 'cornflowerblue')
```

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clust\_test

*Electricity load example: clusters on test set*


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**Description**

A list with observations by cluster for prediction

**Usage**

```
clust_test
```

**Format**

A list of length 14:

14 clusters of loads, depending on both daily and seasonal classification, banking holidays being removed

**Author(s)**

Amandine Pierrot <amandine.m.pierrot@gmail.com>

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clust\_train

*Electricity load example: clusters on train set*

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**Description**

A list with observations by cluster for fitting

**Usage**

clust\_train

**Format**

A list of length 14:

14 clusters of loads, depending on both daily and seasonal classification, banking holidays being removed

**Author(s)**

Amandine Pierrot <amandine.m.pierrot@gmail.com>

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gb\_load

*Electricity load from Great Britain*

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**Description**

A dataset containing half-hourly electricity load from Great Britain from 2011 to 2016, together with observed temperatures. Temperatures are computed from weather stations all over the country. It is a weighted averaged temperature depending on population geographical distribution.

**Usage**

gb\_load

**Format**

A data frame with 105216 rows and 7 variables:

**SETTLEMENT\_DATE** date, the time zone being Europe/London

**SETTLEMENT\_PERIOD** time of the day

**TIMESTAMP** date-time, the time zone being Europe/London

**ENGLAND\_WALES\_DEMAND** British electric load, measured in MW, on average over the half hour

**TEMPERATURE** observed temperature in Celsius

**MV** percentage of missing values when averaging over weather stations, depending on the weight of the station

**DAY\_TYPE** type of the day of the week, from 1 for Sunday to 7 for Saturday, 8 being banking holidays

**Author(s)**

Amandine Pierrot <amandine.m.pierrot@gmail.com>

**Source**

National Grid

National Centers for Environmental Information

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predict.clr

*Prediction from fitted CLR model(s)*

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**Description**

Takes a fitted `clr` object produced by `clr()` and produces predictions given a new set of functions or the original values used for the model fit.

**Usage**

```
## S3 method for class 'clr'
predict(object, newX = NULL, newclust = NULL,
        newXmean = NULL, simplify = FALSE, ...)
```

**Arguments**

**object** A fitted `clr` object produced by `clr()`.

**newX** An object of class `clrdata` or a matrix with one function a row. If this is not provided then predictions corresponding to the original data are returned. If `newX` is provided then it should contain the same type of functions as the original ones (same dimension, same clusters eventually, ...).

newclust	A new list of indices to obtain (approximately) homogeneous dependence structure inside each cluster of functions.
newXmean	To complete when done
simplify	If TRUE, one matrix of predicted functions is returned instead of a list of matrices (one matrix by cluster). In the final matrix, rows are sorted by increasing row numbers.
...	Further arguments are ignored.

## Value

predicted functions

## Examples

```
library(clr)
data(gb_load)

clr_load <- clrdata(x = gb_load$ENGLAND_WALES_DEMAND,
                   order_by = gb_load$TIMESTAMP,
                   support_grid = 1:48)

# data cleaning: replace zeros with NA
clr_load[rowSums((clr_load == 0) * 1) > 0, ] <- NA

Y <- clr_load[2:nrow(clr_load), ]
X <- clr_load[1:(nrow(clr_load) - 1), ]

begin_pred <- which(substr(rownames(Y), 1, 4) == '2016')[1]
Y_train <- Y[1:(begin_pred - 1), ]
X_train <- X[1:(begin_pred - 1), ]
Y_test <- Y[begin_pred:nrow(Y), ]
X_test <- X[begin_pred:nrow(X), ]

## Example without any cluster
model <- clr(Y = Y_train, X = X_train)

pred_on_train <- predict(model)
head(pred_on_train[[1]])

pred_on_test <- predict(model, newX = X_test)
head(pred_on_test[[1]])

## Example with clusters
model <- clr(Y = Y_train, X = X_train, clust = clust_train)

pred_on_train <- predict(model)
str(pred_on_train)
head(pred_on_train[[1]])
```



```
pred_on_test <- predict(model, newX = X_test, newclust = clust_test,  
                        simplify = TRUE)  
str(pred_on_test)  
head(pred_on_test)  
  
# With dates as row names  
rownames(pred_on_test) <- rownames(Y_test)[as.numeric(rownames(pred_on_test))]
```

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