# Package 'distfreereg'

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distfreereg-package Distribution-Free Goodness-of-Fit Testing for Regression

# Description

Implements the distribution-free goodness-of-fit regression test for the mean structure of parametric models introduced in Khmaladze (2021) <doi:10.1007/s10463-021-00786-3>. The test is implemented for general functions with minimal distributional assumptions as well as common models (e.g., lm, glm) with the usual assumptions.

## Details

The DESCRIPTION file:

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Imports:	calculus, clue, lme4, methods
Suggests:	knitr, rmarkdown
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Date:	2025-07-01
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Maintainer:	Jesse Miller <mill9116@umn.edu></mill9116@umn.edu>
Description:	Implements the distribution-free goodness-of-fit regression test for the mean structure of parametric model
License:	GPL-3
Author:	Jesse Miller [aut, cre] (ORCID: <https: 0009-0005-9465-7461="" orcid.org="">)</https:>

Index of help topics:

asymptotics	Convenience function for exploring asymptotic
	behavior and sample size adequacy
coef.distfreereg	Extract estimated parameters from 'distfreereg'

distfreereg-package

compare	objects Compare the simulated statistic distribution with the observed statistic distribution used in distribution-free parametric regression testing
confint.distfreereg	Calculate confidence intervals with a 'distfreereg' object
distfreereg	Distribution-free parametric regression testing
distfreereg-package	Distribution-Free Goodness-of-Fit Testing for Regression
fitted.distfreereg	Extract fitted values from 'distfreereg' objects
formula.distfreereg	Extract formulas from 'distfreereg' objects
ks.test.compare	Formally compare observed and simulated statistics from a 'compare' object
plot.compare	Summary and diagnostic plots for 'compare' objects
plot.distfreereg	Summary and diagnostic plots for 'distfreereg' objects
predict.distfreereg	Generate predicted values from 'distfreereg' objects
print.compare	Printing 'compare' objects
print.distfreereg	Printing 'distfreereg' objects
rejection	Compute rejection rates of a distribution-free test from a 'compare' object
residuals.distfreereg	Extract residuals from 'distfreereg' objects
update.distfreereg	Update 'distfreereg' objects
vcov.distfreereg	Calculate parameter covariance matrices from 'distfreereg' objects

Further information is available in the following vignettes:

v1_introduction	An Introduction to the 'distfreereg' Package (source)
v2_compare	Comparing Distributions with the 'distfreereg' Package (source)
v3_plotting	Plotting with the 'distfreereg' Package (source)
v4_parameter-estimation	Parameter Estimation (source)
v5_advanced-options	Advanced Options for 'distfreereg' Package (source)

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asymptotics

## Description

This is a convenience function that calls compare using object to create the true and test model specifications.

## Usage

asymptotics(object, ...)

# Arguments

object	Object of class distfreereg.
	Additional arguments to pass to compare.

## Details

An important step in implementing distfreereg is determining the plausibility that the sample size of a data set is adequate to produce the desired asymptotic behavior of the simulated statistics. This can be done by calling compare with the appropriate argument values. Because of the importance of this step, this convenience function automates that call using a single argument, namely the object of class distfreereg in question.

# Value

Object of class compare.

# Warning

The fitted model in object is assumed to be the true model, not an estimation of the true model. Further, the simulation of values requires assuming a particular error distribution. See the "Warnings" section in compare's documentation for details.

# Author(s)

Jesse Miller

#### See Also

distfreereg, compare

coef.distfreereg *Extract estimated parameters from* distfreereg *objects* 

# Description

This is a **coef** method for objects of class distfreereg. It extracts the estimated parameters from a model in a distfreereg object.

## Usage

## S3 method for class 'distfreereg'
coef(object, ...)

#### Arguments

object	Object of class distfreereg.
	Additional parameters passed to or from other methods. Currently ignored.

## Value

Numeric vector of estimated model parameters.

## Author(s)

Jesse Miller

## See Also

distfreereg, vcov.distfreereg, confint.distfreereg

compare
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Compare the simulated statistic distribution with the observed statistic distribution used in distribution-free parametric regression testing

# Description

Simulate response data repeatedly with true\_mean as the mean and true\_covariance as the covariance structure, each time running distfreereg on the simulated data. The observed statistics and p-values are saved, as are the simulated statistics from the first replication.

See the Comparing Distributions with the distfreereg Package vignette for an introduction.

```
compare(true_mean, true_method = NULL, true_method_args = NULL, true_covariance,
true_X = NULL, true_data = NULL, theta = NULL, n = NULL, reps = 1e3,
prog = reps/10, simulate_args = NULL, err_dist_fun = NULL,
err_dist_args = NULL, keep = NULL, manual = NULL, update_args = NULL,
global_override = NULL, ...)
```

# Arguments

true_mean	Object specifying the mean structure of the true model. It is used to generate the true values of Y that are passed internally to distfreereg.
true_method	Character vector of length one; specifies the function (e.g., 1m) to use to create a model when true_mean is a formula.
true_method_arg	js
	Optional list; values are passed to the function specified by true_method.
true_covariance	
	Named list; specifies the covariance structures of the true error distribution in the format described in the documentation for the covariance argument of distfreereg. Required when true_mean is a function or nls object, or true_method is "nls".
true_X, true_dat	a
	Optional numeric matrix or data frame, respectively; specifies the covariate values for the true model. true_X is used when true_mean is a function that has an X or x argument, and the data argument is used when true_mean is a formula or model object.
theta	Numeric vector; used as the (true) parameter values for the model when true_mean is a function.
n	Optional integer; indicates how long each simulated data vector should be. Re- quired only when no covariate values are specified for either the true or test mean. Silently converted to integer if numeric.
reps	Integer; specifies number of replications. Silently converted to integer if numeric.
prog	Integer or Inf; if finite, a progress message is given when the current repetition is a multiple of prog. Default value is reps/10, unless reps is less than 10, in which case the default is 1. If Inf, no progress messages are given. Silently converted to integer if finite numeric.
simulate_args	Optional list; specifies additional named arguments to pass to simulate.
err_dist_fun	Character string; specifies the name of the function to be used to simulate errors when true_mean is a function or nls object, or true_method is "nls". See details.
err_dist_args	Optional list; specifies additional named arguments to pass to err_dist_fun.
keep	A vector of integers, or the character string "all". If not NULL, then the output of each replication's call to distfreereg is included in the output if its repetition number is included in keep. Using keep = "all" is equivalent to keep = 1: reps.

#### compare

manual	Optional function; applied to the distfreereg object created in each iteration, whose output is saved in the list manual in the output.
update_args	Optional named list; specifies arguments to pass to update.distfreereg.
global_override	
	Optional named list; specifies arguments to pass to the override argument of distfreereg on each call to that function.
	Additional arguments passed to distfreereg. See details.

#### Details

This function allows the user to explore the asymptotic behavior of the distributions involved in the test conducted by distfreereg. If the sample size is large enough and the true covariance matrix of the errors is known or is estimated well enough, then the observed and simulated statistics have nearly the same distribution. How large the sample size must be depends on the details of the situation. This function can be used to determine how large the sample size must be to obtain approximately equal distributions, and to estimate the power of the test against a specific alternative.

The user specifies a particular true model which is used to generate outcome values. There are three cases:

- When true\_mean is a function, this function determines the mean of the outcome values and err\_dist\_fun is used to generate errors. The error-generating function will usually include an element of true\_covariance as an argument, and in that case must accept the appropriate class of object. For example, if the true covariance is a list of matrices corresponding to a block-diagonal covariance matrix, then err\_dist\_fun must accept such a list as an argument.
- When true\_mean is an nls object, or when it is a formula and true\_method is "nls", the function determined by the formula (in the model call or user-specified, respectively) is used to determine the mean function, and err\_dist\_fun generates the errors.
- When true\_mean is a model object that is not an nls object, or a formula and method is not "nls", then simulate is used to generate outcome values.

If none of these cases apply to true\_mean, then compare() cannot be used. (E.g., true\_mean cannot be a glm object fitted using a "quasi" family, because simulate does not work for that family.)

The user also specifies arguments to pass to distfreereg, most notably a model to test comprising a mean function test\_mean and a covariance structure specified by covariance. For each repetition, compare sends the simulated data, as Y or as part of data, to distfreereg.

The true\_covariance argument specifies the covariance structure that is available to err\_dist\_fun for generating errors. The needs of err\_dist\_fun can vary (for example, the default function uses SqrtSigma to generate multivariate normal errors), so any one of the elements Sigma, SqrtSigma, P, and Q (defined in the documentation of distfreereg) can be specified. Any element needed by err\_dist\_fun is calculated automatically if not supplied.

The value of err\_dist\_fun must be a function whose output is a numeric matrix with n rows and reps columns. Each column is used as the vector of errors in one repetition. The error function's arguments can include the special values n, reps, Sigma, SqrtSigma, P, and Q. These arguments are automatically assigned their corresponding values from the values passed to compare. For example, the default value rmvnorm uses SqrtSigma to generate multivariate normal values with mean 0 and covariance Sigma.

The argument keep is useful for diagnosing problems, but caution should be used lest a very large object be created. It is often sufficient to save the distfreereg objects from only the first few replications.

For more specialized needs, the manual argument allows the calculation and saving of objects during each repetition. For example, using manual = function(x) residuals(x) will save the (raw) residuals from each repetition.

The first repetition creates a distfreereg object. During each subsequent repetition, this object is passed to update.distfreereg to create a new object. The update\_args argument can be used to modify this call.

If necessary, global\_override can be used to pass an override argument to distfreereg in each repetition. For example, using gobal\_override = list(theta\_hat = theta) forces the estimated parameter vector used in the test in each call to be the true parameter vector theta.

# Value

An object of class compare with the following components:

call	The matched call.
Y	The matrix whose columns contain the model outcome values used for the corresponding repetitions.
theta	Supplied vector of parameter values.
true_mean	Supplied object specifying the true mean function.
true_covariance	2
	List containing element(s) that specify the true covariance structure.
true_X	Supplied matrix of true covariate values.
true_data	Supplied data frame of true covariate values.
test_mean	Supplied object specifying the mean function being tested.
covariance	List containing element(s) that specify the test covariance structure.
Х	Supplied matrix of test covariate values.
data	Supplied data frame of test covariate values.
observed_stats	The observed statistics collected in each repetition.
mcsim_stats	The simulated statistics from the first repetition. (They are the same for each repetition, because compare uses update.distfreereg.)
р	The p-values for the observed statistics.
dfrs	A list containing the outputs of distfreereg for repetitions specified in keep. Included when keep is not NULL.
manual	A list containing the results of the function specified by the argument manual. Included when manual is not NULL.

#### compare

### Warnings

The generation of new outcome values requires specifying an error distribution. The default behavior when true\_mean is a function, an nls object, or a formula with method equal to "nls" is to use a multivariate normal error distribution, but different error-generating functions can be defined by the user. When true\_mean is a model object that is not an nls object, or a formula and method is not "nls", then the errors are generated using simulate and are therefore distributed according to that function's specifications.

In short, the asymptotic behavior is determined for a specific (true) error distribution, even though the test itself is distribution-free.

#### Note

Some of the processing of the elements of true\_covariance is analogous to the processing of covariance by distfreereg. Any values of solve\_tol and symmetric specified in distfreereg's control argument are used by compare to similar effect in processing true\_covariance.

Support for glm objects is limited to those created using a family that has a simulate element.

The presence of call in the value allows a compare object to be passed to update.

#### Author(s)

Jesse Miller

#### See Also

asymptotics, distfreereg, rejection, plot.compare, ks.test.compare

## Examples

cdfr\$p

confint.distfreereg Calculate confidence intervals with a distfreereg object

## Description

This is a **confint** method for objects of class distfreereg. It calculates confidence intervals for the estimated parameters of a model in a distfreereg object.

## Usage

```
## S3 method for class 'distfreereg'
confint(object, parm, level = 0.95, ...)
```

# Arguments

object	Object of class distfreereg.
parm	Numeric or character vector; specifies which parameters are to be given confi- dence intervals. If missing, all parameters are considered.
level	Numeric vector of length one; specifies the confidence level.
	Additional parameters passed to other methods. Currently ignored.

# Details

When object contains a model object (either in the test\_mean or model element), then this model is sent to confint. Otherwise, object is sent to confint.default.

# Value

The output from the appropriate confint method.

## Note

If object was created by calling distfreereg.default directly, there is no estimated parameter vector, and therefore confint.distfreereg does not apply.

## Author(s)

Jesse Miller

## See Also

distfreereg, vcov.distfreereg, confint

distfreereg

#### Description

Conduct distribution-free parametric regression testing using the process introduced in *Khmaladze* (2021). A parametric model for the conditional mean (specified by test\_mean) is checked against the data by fitting the model, transforming the resulting residuals, and then calculating a statistic on the empirical partial sum process of the transformed residuals. The statistic's null distribution can be simulated in a straight-forward way, thereby producing a p-value.

Using f to denote the mean function being tested, the specific test has the following null and alternative hypotheses:

 $H_0: \exists \theta \in \Theta \subseteq \mathbb{R}^p \mid \mathrm{E}(Y|X) = f(X;\theta) \text{ against } H_1: \forall \theta \in \Theta \subseteq \mathbb{R}^p \mid \mathrm{E}(Y|X) \neq f(X;\theta).$ 

This assumes a known or adequately accurately estimated covariance matrix. See the An Introduction to the distfreereg Package vignette for an introduction.

# Usage

```
distfreereg(test_mean, ordering = "simplex", group = TRUE,
stat = c("KS", "CvM"), B = 1e4, control = NULL, override = NULL, verbose = TRUE,
...)
## Default S3 method:
distfreereg(test_mean = NULL, ordering = "simplex", group = TRUE,
stat = c("KS", "CvM"), B = 1e4, control = NULL, override = NULL, verbose = TRUE,
..., Y, X = NULL, covariance, J, fitted_values)
## S3 method for class 'formula'
distfreereg(test_mean, ordering = "simplex", group = TRUE,
stat = c("KS", "CvM"), B = 1e4, control = NULL, override = NULL, verbose = TRUE,
..., data, method, method_args = NULL)
## S3 method for class 'function'
distfreereg(test_mean, ordering = "simplex", group = TRUE,
stat = c("KS", "CvM"), B = 1e4, control = NULL, override = NULL, verbose = TRUE,
..., Y, X = NULL, covariance, theta_init)
## S3 method for class 'glm'
distfreereg(test_mean, ordering = "simplex", group = TRUE,
stat = c("KS", "CvM"), B = 1e4, control = NULL, override = NULL, verbose = TRUE,
...)
## S3 method for class 'lm'
distfreereg(test_mean, ordering = "simplex", group = TRUE,
stat = c("KS", "CvM"), B = 1e4, control = NULL, override = NULL, verbose = TRUE,
```

```
...)
## S3 method for class 'lmerMod'
distfreereg(test_mean, ordering = "simplex", group = TRUE,
stat = c("KS", "CvM"), B = 1e4, control = NULL, override = NULL, verbose = TRUE,
...)
## S3 method for class 'nls'
distfreereg(test_mean, ordering = "simplex", group = TRUE,
stat = c("KS", "CvM"), B = 1e4, control = NULL, override = NULL, verbose = TRUE,
...)
```

# Arguments

test_mean	A specification of the mean function to be tested. Methods exist for objects of classes function, formula, glm, lm, lmerMod (from the <b>lme4</b> package), and nls. See details.
covariance	Named list; specifies the covariance structure of the model's error distribution. Valid element names are "Sigma", "SqrtSigma", "P", and "Q", corresponding to the covariance matrix, the square root of the covariance matrix, the precision matrix, and the square root of the precision matrix, respectively. Each element must be one of the following:
	• a numeric matrix.
	• a list of numeric matrices.
	• a numeric vector whose length is the sample size.
	• a numeric vector of length 1.
	See details.
ordering	A character string or a list; specifies how to order the residuals to form the empirical partial sum process. Valid character strings are:
	• "asis": leaves the order unchanged (that is, in the order in which the ob- servations appear in the supplied data).
	• "natural": orders residuals using column-wise ordering of the covariates.
	• "optimal": orders the residuals by ordering the observations using optimal transport on the covariates. The solution is estimated using the Hungarian method as implemented by solve_LSAP. This option can be very slow for large sets of covariates.
	• "simplex": (the default) orders residuals in order of increasing row sums of the covariates after each column has been scaled to the interval [0, 1].
	If ordering is a list, then its elements specify names columns of X or data to use to determine the order.
group	Logical; if TRUE, then residuals with the same rank (as determined by ordering) are grouped when calculating the empirical partial sum process.
J	Numeric matrix; specifies the Jacobian of the function evaluated at the covariates and the estimated parameters.

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В

stat Character vector; specifies the names of the functions used to calculate the desired statistics. By default, a Kolmogorov–Smirnov statistic and a Cramer–von Mises-like statistic are calculated:

$$\operatorname{KS} = \max_{i} |a_{i}|$$
 and  $\operatorname{CvM} = \frac{1}{n} \sum_{i=1}^{n} a_{i}^{2}$ 

where  $a_i$  is term *i* in the empirical partial sum process and *n* is the sample size.

Numeric vector of length one; specifies the Monte Carlo sample size used when simulating statistics. Silently converted to integer.

- control Optional named list of elements that control the details of the algorithm's computations. The following elements are accepted for all methods:
  - symmetric: Optional named list or FALSE; if a named list, its elements are passed as arguments to isSymmetric when testing elements of covariance for symmetry. If FALSE, then this test is skipped.
  - matsqrt\_tol: Numeric; specifies the threshold for considering an eigenvalue "too negative" when calculating the square root of a matrix. Must be non-positive. The default value is -.Machine\$double.eps^0.25.
  - solve\_tol: Numeric; passed as tol argument to solve, used in particular to invert Sigma. The default value is .Machine\$double.eps.
  - qr\_tol: Numeric; passed as tol argument to qr. The default value is sqrt(.Machine\$double.eps). This value might need to be decreased when the dimensions of the Jacobian are sufficiently large.
  - orth\_tol: Numeric; passed as tolerance argument to all.equal when testing whether or not  $r^T r$  and  $\mu^T \mu$  are the identity matrix. The default value is sqrt(.Machine\$double.eps).
  - trans\_tol: Numeric; passed as tolerance argument to all.equal to internal transformation function when determining whether the normalizing scalar is non-zero. The default value is sqrt(.Machine\$double.eps).
  - sym\_tol, sym\_tol1: Numeric; passed as tol and tol1 arguments, respectively, to isSymmetric for checking Sigma and P elements of covariance. The default values are sqrt(.Machine\$double.eps) and 8\*sqrt(.Machine\$double.eps), respectively. See Warnings.
  - return\_on\_error: Logical; determines whether or not partial output is returned when an error is encountered. Default value is TRUE.

The following named elements, all but the first of which control the process of calculating the generalized least squares estimation of the parameter vector, are accepted for the function method:

- jacobian\_args: Optional list; specifies arguments to pass to jacobian.
- optimization\_fun: Optional function; specifies the function used to estimate the parameters. If not specified, optim is used with method = "BFGS".
- fun\_to\_optimize\_arg: Optional character string, required when optimization\_fun is specified; specifies the name of the argument of optimization\_fun that is assigned the function to optimize. For example, optim uses "fn".

	<ul> <li>theta_init_arg: Optional character string, required when optimization_fun is specified; specifies the name of the argument of optimization_fun that is assigned the initial parameter values for optimization. For example, optim uses "par".</li> <li>theta_hat_name: Optional character string, required when optimization_fun is specified; specifies the name of the element of the output of optimization_fun that contains the estimated parameters. For example, optim uses "par" (the same character string that specifies the argument containing the initial values). See Warnings.</li> <li>optimization_args: Optional list; specifies additional arguments to pass</li> </ul>
override	to optimization_fun. Optional named list of arguments that override internally calculated values. Used primarily by update.distfreereg, but can be accessed directly. The following named elements are accepted:
	• J: Numeric matrix. Overrides the calculation of J by non-default methods.
	<ul> <li>fitted_values: Numeric vector of fitted values.</li> </ul>
	• res_order: Integer vector specifying the ordering used to order the resid- uals for the computation of the empirical partial sum process. Overrides ordering. See details.
	<ul> <li>theta_hat: Numeric vector. Used as the estimated parameter vector when test_mean has class function, overriding internal computation that would have used optimization_fun.</li> </ul>
	<ul> <li>r: Orthogonal (numeric) matrix. Overrides the construction of the transfor- mation anchor matrix.</li> </ul>
	• mcsim_stats: List. Overrides the creation of the list of simulated statistics.
verbose	Logical; if TRUE, progress messages are printed. Default value is TRUE.
	Additional arguments to pass to various methods; should be empty except in a call to the generic function.
data	Data frame of covariate values used when test_mean is a formula.
method	Character vector; specifies the function to use for fitting the model when test_mean is a formula. Possible values are "glm", "lm", "lmer", and "nls".
method_args	Optional list of argument values to be passed to the function specified by the method argument.
Υ	Numeric vector of observations. A non-vector value is converted to a vector.
Х	Optional numeric matrix of covariates. A non-matrix value is converted to a single-column matrix.
theta_init	Numeric vector; specifies the starting parameter values passed to the optimizing function to be used to estimate the parameter vector.

# Details

This function implements distribution-free parametric regression testing. The model is specified by a mean structure and a covariance structure.

The mean structure is specified by the argument test\_mean. This can be an object of class function, formula, glm, lm, lmerMod, or nls. It can also be NULL.

#### distfreereg

If test\_mean is a function, then it must have one or two arguments: either theta only, or theta and either X (uppercase) or x (lowercase). An uppercase X is interpreted in the function definition as a matrix, while a lowercase x is interpreted as a vector. (See examples and this vignette.) The primary reason to use a lowercase x is to allow for a function definition using an R function that is not vectorized. In general, an uppercase X should be preferred for speed.

If test\_mean is a formula, then it must be a formula that can be passed to glm, lm, lmer, or nls, and the data argument must be specified. The appropriate model is created and is then sent to distfreereg() for method dispatch.

The function method estimates parameter values, and then uses those to evaluate the Jacobian of the mean function and to calculate fitted values.

All of these methods create a Jacobian matrix and a vector of fitted values. These, along with the covariance structure, are sent the default method. The default method also allows the user to implement the algorithm even when the mean structure is not specified in R, as long as the Jacobian, fitted values, and covariance structure can be imported. (This is useful if a particularly complicated function is defined in another language and cannot easily be copied into R.)

The covariance structure for Y|X must be specified using the covariance argument for the function and default methods. For other methods, the covariance is estimated automatically.

Any element of covariance can be a numeric matrix, a list of numeric matrices, or a numeric vector. If it is a vector, its length must be either 1 or the sample size. This option is mathematically equivalent to setting a covariance list element to a diagonal matrix with the specified value(s) along the diagonal. Using vectors, when possible, is more efficient than using the corresponding matrix. If an element of covariance is a list of numeric matrices, then these matrices are interpreted as the blocks of a block diagonal matrix.

Internally, distfreereg() only needs Q, so some efficiency can be gained by supplying that directly when available. When Q is not specified, it is calculated using whichever element is specified. When more than one of the other elements are specified, Q is calculated using the least expensive path, with no warning given if the specified elements are incompatible. (For example, if both Sigma and SqrtSigma elements are supplied to covariance, then Q is calculated using SqrtSigma with no attempt to verify that SqrtSigma is the matrix square root of Sigma.)

The override argument is used primarily by update.distfreereg to avoid unnecessary and potentially computationally expensive recomputation. This update method imports appropriate values automatically from a previously created object of class distfreereg, and therefore validation is not always done. Use manually with caution.

The res\_order element of override must be a vector of integers from 1 to n (the sample size) that determines the order of the residuals to use when forming the empitical partial sum process. Elements of the vector can be repeated, in which case the residuals corresponding to matching res\_order values are grouped when group is TRUE.

## Value

An object of class distfreereg with the following components:

call	The matched call.
data	A list containing the data argument value, if present, and Y and X.
test_mean	The value supplied to the argument test_mean.

model	The model built when using the formula method; present if and only if using that method.
covariance	The list of covariance matrices, containing at least Q.
theta_hat	The estimated parameter vector. When the model being tested has class lmerMod, this is the vector of fixed effect parameters as returned by fixef.
optimization_output	
	The output of optimization_fun or nls from calculating theta_hat.
fitted_values	The vector of fitted values, $f(X, \hat{\theta})$ . When testing a generalized linear model, these are the fitted values on the response scale.
J	The Jacobian matrix.
mu	The mu matrix.
r	The matrix of transformation anchor vectors.
r_tilde	The matrix of modified transformation anchor vectors.
residuals	A named list of three vectors containing raw, sphered, and transformed residuals.
res_order	A numeric vector indicating the ranking of the residuals used to form the empir- ical partial sum process, in a format to be used as the input of order.
grouping_matri	x
	The matrix used to group residuals; present if group is TRUE and some covariate combinations are repeated.
epsp	The empirical partial sum process formed by calculating the scaled partial sums of the transformed residuals ordered according to res_order.
observed_stat	A named list of the observed statistic(s) corresponding to the transformed resid- uals.
mcsim_stats	A named list, each element of which contains the values of a simulated statistic.
р	A named list with two elements: value, which contains the p-values for each observed statistic, and mcse, which contains the Monte Carlo standard errors for the p-values.

# Warnings

Methods for model objects (e.g., 1m objects) are intended to be used with objects created using a data argument that contains all variables used by the model. This data argument is assumed to be defined in the same environment as the model object, and this is assumed to be the environment in which distfreereg() is called.

Consistency between test\_mean and theta\_init is verified only indirectly. Uninformative errors can occur when, for example, theta\_init does not have the correct length. The most common error message that arises in this case is "f\_out cannot have NA values", which occurs when theta\_init is too short. To be safe, always define test\_mean to use every element of theta.

No verification of consistency is done when multiple elements of coviariance are specified. For example, if P and Sigma are both specified, then the code will use only one of these, and will not verify that P is the inverse of Sigma.

When using the control argument element optimization\_fun to specify an optimization function other than optim, the verification that theta\_hat\_name actually matches the name of an element

#### distfreereg

of the optimization function's output is done only after the optimization has been done. If this optimization will likely take a long time, it is important to verify the value of theta\_hat\_name before running distfreereg().

The default values of sym\_tol and sym\_tol1 are intended to check for substantial asymmetry such as would be caused by the user inputting the wrong matrix. Therefore, they do not check for symmetry with high precision. In particular, these default values are orders of magnitude larger than the default values in isSymmetric.

Non-null values for weights argument in glm are not supported.

## Author(s)

Jesse Miller

## References

Khmaladze, Estate V. *Distribution-free testing in linear and parametric regression*, 2021-03, Annals of the Institute of Statistical Mathematics, Vol. 73, No. 6, p. 1063–1087. doi:10.1007/s10463021-007863

## See Also

coef.distfreereg, confint.distfreereg, fitted.distfreereg, formula.distfreereg, plot.distfreereg,
predict.distfreereg, print.distfreereg, residuals.distfreereg, update.distfreereg,
vcov.distfreereg

#### Examples

theta\_init = c(1,1))

fitted.distfreereg Extract fitted values from distfreereg objects

# Description

This is a fitted method for objects of class distfreereg.

# Usage

```
## S3 method for class 'distfreereg'
fitted(object, ...)
```

# Arguments

object	Object of class distfreereg.
	Additional parameters passed to or from other methods. Currently ignored.

# Value

Numeric vector of fitted values.

# Author(s)

Jesse Miller

# See Also

distfreereg

formula.distfreereg Extract formulas from distfreereg objects

# Description

This is a **formula** method for objects of class distfreereg. It extracts the formula from a model in a distfreereg object.

## Usage

## S3 method for class 'distfreereg'
formula(x, ...)

# Arguments

x	Object of class distfreereg.
	Additional parameters passed to or from other methods. Currently ignored.

# ks.test.compare

# Value

Formula extracted from x\$test\_mean, or NULL if such a formula cannot be extracted.

## Author(s)

Jesse Miller

# See Also

distfreereg

ks.test.compare	Formally compare observed and simulated statistics from a compare
	object

## Description

This is a ks.test method for objects of class compare. It performs a two-sample Kolmogorov– Smirnov test to compare the observed and simulated statistics in an object of class compare.

## Usage

## S3 method for class 'compare'
ks.test(x, ..., stat = NULL)

## Arguments

х	Object of class compare.
	Additional parameters passed to ks.test.
stat	Character string specifying the statistic on which to run the test.

#### Details

When stat is NULL, the default value is the first statistic appearing in the observed\_stats element of object.

# Value

A list of the form specified in ks.test.

## Author(s)

Jesse Miller

# See Also

compare, distfreereg, ks.test

## Examples

plot.compare Summary and di

# Summary and diagnostic plots for compare objects

#### Description

This is a plot method for objects of class compare. It automates the creation of four summary and diagnostic plots for compare objects. See the Plotting with the distfreereg Package vignette for examples.

## Usage

```
## S3 method for class 'compare'
plot(x, y, ..., which = "cdf", stat = NULL, hlines = NULL, curve_args = NULL,
confband_args = FALSE, density_args = NULL, poly = NULL, legend = NULL,
qqline = NULL)
```

## Arguments

х	Object of class compare.
У	Optional object of class compare.
	Additional parameters passed to a plotting function depending on the value of which: to plot for "cdf" and "dens"; to qqplot for "qq" and "qqp".
which	Character string. Acceptable values are "cdf", "dens", "qq", and "qqp":
	• "cdf" produces a plot of the estimated cumulative distribution functions of the two vectors of statistics being compared.
	• "dens" produces a plot of the estimated density functions of the two vectors of statistics being compared.
	• "qq" produces a quantile–quantile plot comparing the two vectors of statis- tics.
	• "qqp" produces a quantile–quantile plot comparing the p-values with uni- form quantiles. (This is not available when y is present.)

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stat	Character string, specifies the statistic to plot.
hlines	An optional list of arguments to pass to abline, used to create the horizontal dashed lines when which is "cdf". Setting equal to FALSE prevents the call, and no lines are drawn.
curve_args	An optional list used to pass arguments to lines (not curve!), used to cre- ate the curves when which is "cdf" or "dens". It can have two special named arguments, obs and mcsim, whose values must be lists. Those lists contain argu- ments passed to the calls to lines for plotting the curves for the observed and simulated statistics, respectively. Any other elements are passed to both calls.
confband_args	An optional list of values that control the calculation and plotting of confidence bands when which is "cdf" or "dens". Any of the following named elements are allowed.
	<ul> <li>w: Numeric; the sequence of points on which to evaluate the confidence band. By default, the sequence is seq(from = min(x) + buffer, to = max(x) - buffer, length.out = m), where x is the vector of values of the statistic in question, and buffer is explained below.</li> <li>m: Integer; the length of w, used only when w is NULL. The default value is</li> </ul>
	• m: integer, the length of w, used only when w is NOLL. The default value is 100.
	• batch_len: Integer; the batch length for the algorithm. The default value is 50.
	• N: Integer; the number of multivariate $t$ samples to use in the simulation.
	• conf.level: Numeric; the desired confidence level.
	• buffer: Numeric; the proportion of either side of the range of data to ignore when defining w, used only when w is NULL.
	• curve_args: An optional list of arguments passed to lines (again, not curve!), used to create the boundaries of the confidence band. It can have two special named arguments, obs and mcsim, which function in the same way as the corresponding elements of the curve_args argument described above.
	• polygon_args: An optional list of arguments passed to polygon, used to shade the confidence region. Setting equal to FALSE prevents the call, and no shading is done.
	• shade_col: This provides a shortcut to the col argument of polygon to change the color of the shaded region.
	Setting equal to FALSE prevents calculation and plotting of the band.
density_args	An optional list of arguments passed to density when which is "dens", which calculates the points used to plot the density curves. The list can have two special named elements, obs and mcsim, which function in the same way as the corresponding elements of the curve_args argument described above.
poly	An optional list of arguments passed to polygon when which is "dens", which shades the area under the density curves. The list can have two special named elements, obs and mcsim, which modify the shadings for their respective curves, analogous to their behavior in the curve_args argument. When poly is equal to FALSE, no call is made, and therefore no shading is done.
legend	An optional list of arguments passed to legend when which is "cdf" or "dens". When equal to FALSE, no call is made, and therefore no legend is created.

qqline An optional list of arguments passed to abline when which is "qq" or "qqp". By default, this plots the line y = x. When equal to FALSE, no call is made, and therefore no line is plotted.

## Details

This function produces a plot of a type specified by which. The values plotted depend on whether or not y is present and the value of which. When y is present, the plots compare the observed statistics in x and the observed statistics in y. When y is missing, the plots compare the observed and simulated statistics in x. (The exception is when which is "qqp", which is only available when y is missing.)

When which is "cdf" or "dens", the plotting region and associated labels, tick marks, etc., are created by an initial call to plot. The curves themselves are drawn with lines. The arguments specified in . . . are passed to the initial call to plot.

#### Value

The values used to create the curves (or points, in the case of a Q–Q plot) are returned invisibly. The details depend on the value of which:

- cdf: A list with two or four elements, all lists. The first two sub-lists contain the x- and y-values cdf curves. If confidence bands are plotted, then two additional elements are included with output from the confidence band calculations, including elements w, cb\_lower, and cb\_upper, which contain, respectively, the x-coordinates for both the upper and lower bounds of the band, the y-coordinates for the lower band, and the y-coordinates for the upper band.
- dens: A list with two or four elements, all lists. The first two sub-lists contain x- and y-values for the density curves. If confidence bands are plotted, then two additional sub-lists are supplied, with contents identical to what is described for "cdf".
- qq, qqp: The output of qqplot.

For "cdf" and "dens", the names of the elements of the returned list depend on whether or not a value for the argument y was supplied.

# Author(s)

Jesse Miller

#### References

Flegal, James M. et al. Simultaneous confidence bands for (Markov chain) Monte Carlo simulations, forthcoming.

#### See Also

distfreereg, compare

plot.distfreereg Summary and diagnostic plots for distfreereg objects

# Description

This is a plot method for objects of class distfreereg. It automates the creation of three summary and diagnostic plots for distfreereg objects. See the Plotting with the distfreereg Package vignette for examples.

# Usage

```
## S3 method for class 'distfreereg'
plot(x, which = "dens", stat = NULL, density_args = NULL, polygon_args = NULL,
confband_args = NULL, abline_args = NULL, shade_col = rgb(1,0,0,0.5),
text_args = NULL, ...)
```

# Arguments

х	Object of class distfreereg.
which	Character string. Acceptable values are "dens", "residuals", and "epsp":
	• "dens" produces a plot of the estimated density curve of the specified statis- tic.
	<ul> <li>"residuals" produces a plot of the transformed residuals in the order spec- ified by x\$res_order.</li> </ul>
	• "epsp" produces a plot of the empirical partial sum process of the (ordered) transformed residuals.
stat	Character vector of length one specifying the name of the statistic to plot when which is "dens". By default, the first statistic in x\$observed_stats is used.
density_args	An optional list of arguments to pass to density.
polygon_args	An optional list of arguments to pass to polygon, used to shade under the density curve to the right of the value of the observed statistic. Setting equal to FALSE prevents the call, and no shading is done.
confband_args	An optional list of values that control the calculation and plotting of confidence bands. Any of the following named elements are allowed.
	<ul> <li>w: Numeric; the sequence of points on which to evaluate the confidence band. By default, the sequence is seq(from = min(x) + buffer, to = max(x) - buffer, length.out = m, where x is the vector of values of the statistic in question, and buffer is explained below.</li> </ul>
	• m: Integer; the length of w, used only when w is NULL. The default value is 100.
	• batch_len: Integer; the batch length for the algorithm. The default value is 50.
	• N: Integer; the number of multivariate $t$ samples to use in the simulation.
	• conf.level: Numeric; the desired confidence level.

	• buffer: Numeric; the proportion of either side of the range of data to ignore when defining w, used only when w is NULL.
	• curve_args: An optional list of arguments passed to lines (not curve!), used to create the boundaries of the confidence band.
	• polygon_args: An optional list of arguments passed to polygon, used to shade the confidence region. Setting equal to FALSE prevents the call, and no shading is done.
	• shade_col: This provides a shortcut to the col argument of polygon to change the color of the shaded region.
	Setting equal to FALSE prevents calculation and plotting of the confidence band.
abline_args	An optional list of arguments to pass to abline, used to draw a vertical line at the value of the observed statistic. Setting equal to FALSE prevents the call, and no line is drawn.
shade_col	Character string or other value specifying the color to use to shade the upper tail of the distribution. Default value is red with 50% transparency. This is a convenience argument, and the same functionality is available by defining a col element in the polygon_args argument.
text_args	An optional list of arguments to pass to text, used to label the vertical line with the p-value of the observed statistic. Setting equal to FALSE prevents the call, and no text is printed.
	Additional arguments to pass to plot.

#### Details

This function produces one of three specified plots, depending on the value of which.

When which is "dens", a plot of the estimated density of the simulated statistics is produced, including a vertical line at the value of the observed test statistic with the p-value displayed.

The default placement of the p-value text is on the left side of the line indicating the statistic value. Specifically, the default values of x and y passed to text are the statistic value itself and the midpoint between zero and the maximum value of the density curve. The default value passed to adj is c(1,0.5), meaning that the text is aligned to the left of the value (x, y) and centered vertically on it. (The default value for the text itself, which can be modified via the label argument of text, includes a space on the left and the right for padding so the text does not overlap the vertical line itself.) To align the text so it appears on the right side (for example, to avoid overlapping the density curve), use text\_args = list(adj = c(0, 0.5)). See documentation for text for details on this and other arguments.

When which is "residuals", a time-series-like plot is produced showing transformed residuals in the order given by x\$res\_order. In the case that the null hypothesis is rejected, this plot can help determine where (in terms of the linearly ordered covariates) a discrepancy between the model and the data occurs.

When which is "epsp", a plot of the empirical partial sum process is produced; that is, the y-values are

$$y_j = \frac{1}{\sqrt{n}} \sum_{i=1}^j \hat{e}_i$$

## predict.distfreereg

where  $\hat{e}_i$  is the *i*th transformed residual in the order given by x\$res\_order. Similar to the case when which is "residuals", this plot can help determine where (in terms of the linearly ordered covariates) a discrepancy between the model and the data occurs.

## Value

When which is "dens", the values used to create the density plot are returned invisibly in a list with two named elements, x and y. If the confidence band is plotted, then it is included as an element named confband.

For other values of which, nothing is returned.

#### Author(s)

Jesse Miller

# References

Flegal, James M. et al. Simultaneous confidence bands for (Markov chain) Monte Carlo simulations, forthcoming.

## See Also

distfreereg

predict.distfreereg Generate predicted values from distfreereg objects

#### Description

This is a predict method for objects of class distfreereg.

#### Usage

## S3 method for class 'distfreereg'
predict(object, ...)

# Arguments

object	Object of class distfreereg.
•••	Additional arguments passed to other predict methods. In particular, can include a newdata value.

# Details

When object\$test\_mean is a model object ("lm", "glm", or "nls"), object\$test\_mean is sent to predict for method dispatch. When object\$test\_mean is of class "formula", object\$model is sent to predict.

# Value

Numeric vector of predicted values.

# Author(s)

Jesse Miller

# See Also

distfreereg

print.compare *Printing* compare *objects* 

# Description

This is a print method for objects of class compare.

# Usage

## S3 method for class 'compare'
print(x, ...)

# Arguments

х	Object of class compare.
	Additional parameters, currently ignored.

# Details

This function prints a useful summary of the compare object x.

# Value

No return value (NULL).

# Author(s)

Jesse Miller

# See Also

compare

# Description

This is a print method for objects of class distfreereg.

# Usage

## S3 method for class 'distfreereg'
print(x, ..., digits = 3, col\_sep = 2, show\_params = TRUE)

# Arguments

x	Object of class distfreereg.
	Additional parameters, currently ignored.
digits	Integer; passed to signif to determine the number of significant digits to display.
col_sep	Integer; specifies the padding (in units of spaces) between columns in the printed table of statistics.
show_params	Logical; determines whether or not the parameter estimates, if present in x, are displayed.

# Details

This function prints a useful summary of the distfreereg object x.

# Value

No return value (NULL).

# Author(s)

Jesse Miller

# See Also

distfreereg

rejection

## Description

Compute the rejection rates of the tests simulated in a compare object. Specifically, this function estimates the rejection rates of the tests conducted with specified statistics of the hypothesis that the mean function is test\_mean when the true mean function is true\_mean.

## Usage

```
rejection(object, alpha = 0.05, stat = names(object[["observed_stats"]]), ...)
```

# Arguments

object	Object of class compare.
alpha	Numeric vector; specifies the $\alpha$ -levels to use. Passed as probs argument to quantile.
stat	Character vector; specifies the names of the statistics to use. The default value computes the rejection rate associated with every statistic in object.
	Additional arguments to pass to quantile to estimate the $1 - \alpha$ quantiles of the distribution of simulated statistics.

# Value

Data frame containing estimated rejection rates and associated Monte Carlo standard errors, with one row for each combination of stat and alpha elements.

## Warning

The reported Monte Carlo standard error does not account for the uncertainty of the estimation of the  $1 - \alpha$  quantiles of the distribution of simulated statistics. The number of Monte Carlo simulations should be large enough to make this estimate sufficiently accurate that it can be considered known for practical purposes. The standard errors of estimated quantiles can be calculated using the **mcmcse** package.

## Author(s)

Jesse Miller

#### See Also

distfreereg, compare

# residuals.distfreereg

## Examples

residuals.distfreereg Extract residuals from distfreereg objects

## Description

This is a residuals method for objects of class distfreereg. It can extract any of the three available types of residuals.

# Usage

## S3 method for class 'distfreereg'
residuals(object, ..., type = "raw")

# Arguments

object	Object of class distfreereg.
	Additional parameters passed to or from other methods. Currently ignored.
type	Character string specifying the type of residuals to return. Must be one of "raw", "sphered", and "transformed".

## Value

Numeric vector of residuals.

## Author(s)

Jesse Miller

## See Also

distfreereg

update.distfreereg Update distfreereg objects

#### Description

This is an update method for objects of class distfreereg. The method takes advantage of the override argument of distfreereg to prevent unnecessary recalculation of potentially computationally expensive objects.

## Usage

```
## S3 method for class 'distfreereg'
update(object, ..., smart = TRUE, envir = parent.frame())
```

## Arguments

object	Object of class distfreereg.
	Additional named parameters to pass to distfreereg.
smart	Logical. If TRUE, then saved values from object are passed to distfreereg using the override argument, when they need not themselves be updated. See details.
envir	Environment passed to eval when evaluating modified call.

#### Details

This function updates an object of class distfreereg. By default, it does so "intelligently" in the sense that it does not unnecessarily recompute elements that are already saved in object. For example, if a new value for covariance is not included in . . ., then the value of covariance saved in object is automatically passed to the new call, preventing recalculating Q. If a new value of covariance is specified, then all objects dependent on that (e.g.,  $\hat{\theta}$ ) are recomputed.

In particular, the simulated samples depend on the data and function only through the number of observations, the covariates (if any), and the dimension of the parameter space of the function. If none of these change, then the updated object reuses the simulated samples from the supplied object.

The price paid for this efficiency is a potentially "large" value of call in the updated object.

# Value

An updated object of class distfreereg.

## Note

The usual behavior of update is to create an updated call and then evaluate that call. This is what update.distfreereg does, as well, but some of the updated elements are drawn from object itself for use as override values. In general, an object created by update.distfreereg is not identical to the object created by distfreereg using corresponding arguments, because the call values will differ.

## vcov.distfreereg

## Author(s)

Jesse Miller

# See Also

distfreereg

### Examples

```
func_updated <- function(X, theta) X[,1]^theta[1] + theta[2]*X[,2]^2
dfr_2 <- update(dfr_1, test_mean = func_updated)</pre>
```

vcov.distfreereg Calculate parameter covariance matrices from distfreereg objects

# Description

This is a vcov method for objects of class distfreereg. It calculates an estimated covariance matrix of the estimated parameters in a model from a distfreereg object.

## Usage

```
## S3 method for class 'distfreereg'
vcov(object, ..., jacobian_args, hessian_args)
```

#### Arguments

object	Object of class distfreereg.
	Additional parameters passed to other methods when test_mean element of object is not of class function.
jacobian_args, hessian_args	
	Lists of additional arguments to pass to jacobian and hessian.

# Details

When the test\_mean element of object is of class function, the covariance matrix is estimated using the method described in section 5.3 of *Van der Vaart (2007)*. Otherwise, test\_mean is of a class that has its own method for vcov, which is used to calculate the output.

# Value

Named numeric matrix equal to the estimated covariance matrix of the parameter estimates from object.

# Warning

This calculation can be computationally intensive when the sample size is large and object\$test\_mean is a function.

# Note

If object was created by calling distfreereg.default directly, there is no estimated parameter vector, and therefore vcov.distfreereg does not apply.

## Author(s)

Jesse Miller

# References

Vaart, A. W. Asymptotic statistics, 2007, *Cambridge series on statistical and probabilistic mathematics*, Cambridge University Press.

# See Also

distfreereg, confint.distfreereg

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