

# Package ‘emplik2’

July 22, 2025

**Version** 1.33

**Title** Empirical Likelihood Ratio Test for Two-Sample U-Statistics with  
Censored Data

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**Depends** R (>= 3.2.5)

**Imports** stats

**Description** Calculates the empirical likelihood ratio and p-value for a mean-type hypothesis  
(or multiple mean-type hypotheses) based on two samples with possible censored data.

**License** GPL (>= 2)

**NeedsCompilation** no

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**Repository** CRAN

**Date/Publication** 2024-08-31 10:10:03 UTC

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el2.cen.EMm	<i>Computes empirical likelihood ratio and p-value for multiple mean-type hypotheses, based on two independent samples that may contain censored data.</i>
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## Description

This function is similar to `el2.cen.EMs` but for several mean type restrictions. This function uses the EM algorithm to calculate a maximized empirical likelihood ratio for a set of  $p$  simultaneous hypotheses as follows:

$$H_o : E(g(x, y) - \text{mean}) = 0$$

where  $E$  indicates expected value;  $g(x, y)$  is a vector of user-defined functions:  $g_1(x, y), \dots, g_p(x, y)$ ; and  $\text{mean}$  is a vector of  $p$  hypothesized values of  $E(g(x, y))$ . The two samples  $x$  and  $y$  are assumed independent. They may be uncensored, right-censored, left-censored, or left-and-right (“doubly”) censored. A p-value for  $H_o$  is also calculated, based on the assumption that  $-2 \cdot \log(\text{empirical likelihood ratio})$  is asymptotically distributed as  $\text{chisq}(\text{df}=p)$ .

## Usage

```
el2.cen.EMm(x, dx, wx=rep(1,length(x)), y, dy, wy=rep(1,length(y)),
            p, H, xc=1:length(x), yc=1:length(y), mean, maxit=35)
```

## Arguments

<code>x</code>	a vector of the data for the first sample
<code>dx</code>	a vector of the censoring indicators for x: 0=right-censored, 1=uncensored, 2=left-censored
<code>wx</code>	a vector of data case weight for x
<code>y</code>	a vector of the data for the second sample
<code>dy</code>	a vector of the censoring indicators for y: 0=right-censored, 1=uncensored, 2=left-censored
<code>wy</code>	a vector of data case weight for y
<code>p</code>	the number of hypotheses
<code>H</code>	a matrix defined as $H = [H_1, H_2, \dots, H_p]$ , where $H_k = [g_k(x_i, y_j) - \text{mean}_k], k = 1, \dots, p$
<code>xc</code>	a vector containing the indices of the x datapoints, controls if tied x collapse or not
<code>yc</code>	a vector containing the indices of the y datapoints, ditto
<code>mean</code>	the hypothesized value of $E(g(x, y))$
<code>maxit</code>	a positive integer used to control the maximum number of iterations of the EM algorithm; default is 35

## Details

The value of  $\text{mean}_k$  should be chosen between the maximum and minimum values of  $g_k(x_i, y_j)$ ; otherwise there may be no distributions for  $x$  and  $y$  that will satisfy  $H_o$ . If  $\text{mean}_k$  is inside this interval, but the convergence is still not satisfactory, then the value of  $\text{mean}_k$  should be moved closer to the NPMLE for  $E(g_k(x, y))$ . (The NPMLE itself should always be a feasible value for  $\text{mean}_k$ .)

**Value**

e12.cen.EMm returns a list of values as follows:

xd1	a vector of unique, uncensored $x$ -values in ascending order
yd1	a vector of unique, uncensored $y$ -values in ascending order
temp3	a list of values returned by the e12.test.wtm function (which is called by e12.cen.EMm)
mean	the hypothesized value of $E(g(x, y))$
NPMLE	a non-parametric-maximum-likelihood-estimator vector of $E(g(x, y))$
logel00	the log of the unconstrained empirical likelihood
logel	the log of the constrained empirical likelihood
"-2LLR"	$-2 \times (\text{log-likelihood-ratio})$ for the $p$ simultaneous hypotheses
Pval	the $p$ -value for the $p$ simultaneous hypotheses, equal to $1 - \text{pchisq}(-2\text{LLR}, \text{df} = p)$
logvec	the vector of successive values of logel computed by the EM algorithm (should converge toward a fixed value)
sum_muvec	sum of the probability jumps for the uncensored $x$ -values, should be 1
sum_nuvec	sum of the probability jumps for the uncensored $y$ -values, should be 1

**Author(s)**

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**References**

- Barton, W. (2010). Comparison of two samples by a nonparametric likelihood-ratio test. PhD dissertation at University of Kentucky.
- Chang, M. and Yang, G. (1987). "Strong Consistency of a Nonparametric Estimator of the Survival Function with Doubly Censored Data." *Ann. Stat.*, 15, pp. 1536-1547.
- Dempster, A., Laird, N., and Rubin, D. (1977). "Maximum Likelihood from Incomplete Data via the EM Algorithm." *J. Roy. Statist. Soc., Series B*, 39, pp.1-38.
- Gomez, G., Julia, O., and Utzet, F. (1992). "Survival Analysis for Left-Censored Data." In Klein, J. and Goel, P. (ed.), *Survival Analysis: State of the Art*. Kluwer Academic Publishers, Boston, pp. 269-288.
- Li, G. (1995). "Nonparametric Likelihood Ratio Estimation of Probabilities for Truncated Data." *J. Amer. Statist. Assoc.*, 90, pp. 997-1003.
- Owen, A.B. (2001). *Empirical Likelihood*. Chapman and Hall/CRC, Boca Raton, pp. 223-227.
- Turnbull, B. (1976). "The Empirical Distribution Function with Arbitrarily Grouped, Censored and Truncated Data." *J. Roy. Statist. Soc., Series B*, 38, pp. 290-295.
- Zhou, M. (2005). "Empirical likelihood ratio with arbitrarily censored/truncated data by EM algorithm." *J. Comput. Graph. Stat.*, 14, pp. 643-656.
- Zhou, M. (2009) *emplik* package on CRAN website. The function e12.cen.EMm here extends e1.cen.EM2 inside *emplik* package from one-sample to two-samples.

### Examples

```
x<-c(10, 80, 209, 273, 279, 324, 391, 415, 566, 85, 852, 881, 895, 954, 1101, 1133,
1337, 1393, 1408, 1444, 1513, 1585, 1669, 1823, 1941)
dx<-c(1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1, 0, 0, 0, 0, 1, 1, 0)
y<-c(21, 38, 39, 51, 77, 185, 240, 289, 524, 610, 612, 677, 798, 881, 899, 946, 1010,
1074, 1147, 1154, 1199, 1269, 1329, 1484, 1493, 1559, 1602, 1684, 1900, 1952)
dy<-c(1,1,1,1,1,1,2,2,1,1,1,1,1,2,1,1,1,1,1,1,0,0,1,1,0,0,1,0,0,0)
nx<-length(x)
ny<-length(y)
xc<-1:nx
yc<-1:ny
wx<-rep(1,nx)
wy<-rep(1,ny)
mu=c(0.5,0.5)
p <- 2
H1<-matrix(NA,nrow=nx,ncol=ny)
H2<-matrix(NA,nrow=nx,ncol=ny)
for (i in 1:nx) {
  for (j in 1:ny) {
    H1[i,j]<-(x[i]>y[j])
    H2[i,j]<-(x[i]>1060) } }
H=matrix(c(H1,H2),nrow=nx,ncol=p*ny)

# Ho1: X is stochastically equal to Y (i.e. P(X>Y)=0.5)
# Ho2: P(X>1060)=0.5

el2.cen.EMm(x=x, dx=dx, y=y, dy=dy, p=2, H=H, mean=mu)

# Result: Pval is 0.6310234, so we cannot with 95 percent confidence reject the two
# simultaneous hypotheses Ho1 and Ho2
```

---

el2.cen.EMs

---

*Computes empirical likelihood ratio and p-value for a single mean-type hypothesis, based on two independent samples that may contain censored data.*


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### Description

This function uses the EM algorithm to calculate a maximized empirical likelihood ratio for the hypothesis

$$H_o : E(g(x,y) - mean) = 0$$

where  $E$  indicates expected value;  $g(x,y)$  is a user-defined function of  $x$  and  $y$ ; and  $mean$  is the hypothesized value of  $E(g(x,y))$ . The default:  $g(x,y) = I[x \geq y]$ ,  $mean = 0.5$ . The samples  $x$  and  $y$  are assumed independent. They may be uncensored, right-censored, left-censored, or left-and-right (“doubly”) censored. A p-value for  $H_o$  is also calculated, based on the assumption that  $-2 \cdot \log(\text{empirical likelihood ratio})$  is approximately distributed as  $\text{chisq}(df=1)$ .

**Usage**

```
e12.cen.EMs(x,dx,y,dy,fun=function(x,y){x>=y},mean=0.5,
            tol.u=1e-6,tol.v=1e-6,maxit=50)
```

**Arguments**

<code>x</code>	a vector of the data for the first sample
<code>dx</code>	a vector of the censoring indicators for <code>x</code> : 0=right-censored, 1=uncensored, 2=left-censored
<code>y</code>	a vector of the data for the second sample
<code>dy</code>	a vector of the censoring indicators for <code>y</code> : 0=right-censored, 1=uncensored, 2=left-censored
<code>fun</code>	a user-defined, weight-function $g(x, y)$ used to define the mean in the hypothesis $H_o$ . The default is <code>fun=function(x,y){x&gt;=y}</code> .
<code>mean</code>	the hypothesized value of $E(g(x, y))$ ; default is 0.5
<code>tol.u</code>	Error tolerance for iteration control. L1 norm of the u-uOLD is used. Default 1e-6
<code>tol.v</code>	Error tolerance for iteration control. L1 norm of the v-vOLD is used. Default 1e-6
<code>maxit</code>	a positive integer used to set the maximum number of iterations of the EM algorithm; default is 50

**Details**

The empirical likelihood used here is

$$EL(mean) = \max_{\mu_i, \nu_j} \left\{ \prod \mu_i \prod \nu_j; s.t. \sum_i \sum_j g(x_i, y_j) \mu_i \nu_j = mean; \sum \mu_i = 1; \sum \nu_j = 1. \right\}$$

for uncensored data. If data were censored, appropriate adjustments are used accordingly. See Owen (2001) section 11.4.

The value of *mean* should be chosen between the maximum and minimum values of  $g(x_i, y_j)$ ; otherwise there may be no distributions for  $x$  and  $y$  that will satisfy  $H_o$ . If *mean* is inside this interval, but the convergence is still not satisfactory, then the value of *mean* should be moved closer to the NPMLE for  $E(g(x, y))$ . (The NPMLE itself should always be a feasible value for *mean*. This NPMLE value is in the output.)

**Value**

`e12.cen.EMs` returns a list of values as follows:

<code>xd1</code>	a vector of the unique, uncensored $x$ -values in ascending order
<code>yd1</code>	a vector of the unique, uncensored $y$ -values in ascending order
<code>temp3</code>	a list of values returned by the <code>e12.test.wts</code> function (which is called by <code>e12.cen.EMs</code> )

mean	the hypothesized value of $E(g(x, y))$
funNPMLE	the non-parametric-maximum-likelihood-estimator of $E(g(x, y))$
logel00	the log of the unconstrained empirical likelihood
logel	the log of the constrained empirical likelihood
"-2LLR"	$-2*(\text{logel}-\text{logel00})$
Pval	the estimated p-value for $H_0$ , computed as $1-\text{pchisq}(-2\text{LLR}, \text{df} = 1)$
logvec	the vector of successive values of logel computed by the EM algorithm (should converge toward a fixed value)
sum_muvec	sum of the probability jumps for the uncensored $x$ -values, should be 1
sum_nuvec	sum of the probability jumps for the uncensored $y$ -values, should be 1
constraint	the realized value of $\sum_{i=1}^n \sum_{j=1}^m (g(x_i, y_j) - \text{mean})\mu_i\nu_j$ , where $\mu_i$ and $\nu_j$ are the probability jumps at $x_i$ and $y_j$ , respectively, that maximize the empirical likelihood ratio. The value of constraint should be close to 0.

#### Author(s)

William H. Barton <bbarton@lexmark.com> ; modified by Mai Zhou.

#### References

- Barton, W. (2010). Comparison of two samples by a nonparametric likelihood-ratio test. PhD dissertation at University of Kentucky.
- Chang, M. and Yang, G. (1987). "Strong Consistency of a Nonparametric Estimator of the Survival Function with Doubly Censored Data." *Ann. Stat.*, 15, pp. 1536-1547.
- Dempster, A., Laird, N., and Rubin, D. (1977). "Maximum Likelihood from Incomplete Data via the EM Algorithm." *J. Roy. Statist. Soc., Series B*, 39, pp.1-38.
- Gomez, G., Julia, O., and Utzet, F. (1992). "Survival Analysis for Left-Censored Data." In Klein, J. and Goel, P. (ed.), *Survival Analysis: State of the Art*. Kluwer Academic Publishers, Boston, pp. 269-288.
- Li, G. (1995). "Nonparametric Likelihood Ratio Estimation of Probabilities for Truncated Data." *J. Amer. Statist. Assoc.*, 90, pp. 997-1003.
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- Turnbull, B. (1976). "The Empirical Distribution Function with Arbitrarily Grouped, Censored and Truncated Data." *J. Roy. Statist. Soc., Series B*, 38, pp. 290-295.
- Zhou, M. (2005). "Empirical likelihood ratio with arbitrarily censored/truncated data by EM algorithm." *J. Comput. Graph. Stat.*, 14, pp. 643-656.
- Zhou, M. (2009) *emplik* package on CRAN website. The e12.cen.EMs function here extends the e1.cen.EM function inside *emplik* package from one sample to two-samples.

### Examples

```
x<-c(10,80,209,273,279,324,391,415,566,785,852,881,895,954,1101,
1133,1337,1393,1408,1444,1513,1585,1669,1823,1941)
dx<-c(1,2,1,1,1,1,1,2,1,1,1,1,1,1,0,0,1,0,0,0,0,1,1,0)
y<-c(21,38,39,51,77,185,240,289,524,610,612,677,798,881,899,946,
1010,1074,1147,1154,1199,1269,1329,1484,1493,1559,1602,1684,1900,1952)
dy<-c(1,1,1,1,1,1,1,1,1,1,1,1,1,1,0,1,1,1,0,0,0,0,0,1,0,0,0)

# Ho1: X is stochastically equal to Y (i.e. P(X>Y)=0.5)
e12.cen.EMs(x, dx, y, dy, fun=function(x,y){x>y}, mean=0.5)
# Result: Pval = 0.7090658, so we cannot with 95 percent confidence reject Ho1
# Remark: may be we should be more careful for the (x=y) cases, if any.

# Ho2: mean of X equals mean of Y
e12.cen.EMs(x, dx, y, dy, fun=function(x,y){x-y}, mean=0)
# Result: Pval = 0.9716493, so we cannot with 95 percent confidence reject Ho2
```

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e12.test.wtm

---

*Computes maximum-likelihood probability jumps for multiple mean-type hypotheses, based on two independent uncensored samples*


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### Description

This function computes the maximum-likelihood probability jumps for multiple mean-type hypotheses, based on two samples that are independent, uncensored, and weighted. The target function for the maximization is the (Lagrangian) constrained log(empirical likelihood) which can be expressed as,

$$\sum_{dx_i=1} wx_i \log \mu_i + \sum_{dy_j=1} wy_j \log \nu_j - \eta(1 - \sum_{dx_i=1} \mu_i) - \delta(1 - \sum_{dy_j=1} \nu_j) - \lambda(\mu^T H_1 \nu, \dots, \mu^T H_p \nu)^T$$

where the variables are defined as follows:

$x$  is a vector of uncensored data for the first sample

$y$  is a vector of uncensored data for the second sample

$wx$  is a vector of estimated weights for the first sample

$wy$  is a vector of estimated weights for the second sample

$\mu$  is a vector of estimated probability jumps for the first sample

$\nu$  is a vector of estimated probability jumps for the second sample

$H_k = [g_k(x_i, y_j) - mean_k], k = 1, \dots, p$ , where  $g_k(x, y)$  is a user-chosen function

$H = [H_1, \dots, H_p]$  (used as argument in `e1.cen.EMm` function, which calls `e12.test.wtm`)

$mean$  is a vector of length  $p$  of hypothesized means, such that  $mean_k$  is the hypothesized value of  $E(g_k(x, y))$

$E$  indicates “expected value”

**Usage**

```
el2.test.wtm(xd1,yd1,wxd1new, wyd1new, muvec, nuvec, Hu, Hmu, Hnu, p, mean, maxit=35)
```

**Arguments**

xd1	a vector of uncensored data for the first sample
yd1	a vector of uncensored data for the second sample
wxd1new	a vector of estimated weights for xd1
wyd1new	a vector of estimated weights for yd1
muvec	a vector of estimated probability jumps for xd1
nuvec	a vector of estimated probability jumps for yd1
Hu	$H_u = [H_1 - [mean_1], \dots, H_p - [mean_p]], dx_i = 1, dy_j = 1$
Hmu	a matrix, whose calculation is shown in the example below
Hnu	a matrix, whose calculation is shown in the example below
p	the number of hypotheses
mean	a vector of hypothesized values of $E(g_k(u, v)), k = 1, \dots, p$
maxit	a positive integer used to control the maximum number of iterations in the Newton-Raphson algorithm; default is 35

**Details**

This function is called by `el2.cen.EMm`. It is listed here because the user may find it useful elsewhere.

The value of  $mean_k$  should be chosen between the maximum and minimum values of  $g_k(xd1_i, yd1_j)$ ; otherwise there may be no distributions for  $xd1$  and  $yd1$  that will satisfy the the mean-type hypothesis. If  $mean_k$  is inside this interval, but the convergence is still not satisfactory, then the value of  $mean_k$  should be moved closer to the NPMLE for  $E(g(xd1, yd1))$ . (The NPMLE itself should always be a feasible value for  $mean_k$ .) The calculations for this function are derived in Owen (2001).

**Value**

`el2.test.wtm` returns a list of values as follows:

constmat	a matrix of row vectors, where the $k$ th row vector holds successive values of $\mu^T H_k \nu, k = 1, \dots, p$ , generated by the Newton-Raphson algorithm
lam	the vector of Lagrangian multipliers used in the calculations
muvec1	the vector of probability jumps for the first sample that maximize the weighted empirical likelihood
nuvec1	the vector of probability jumps for the second sample that maximize the weighted empirical likelihood
mean	the vector of hypothesized means



**Author(s)**

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**References**

Owen, A.B. (2001). Empirical Likelihood. Chapman and Hall/CRC, Boca Raton, pp.223-227.

**Examples**

```
#Ho1: P(X>Y) = 0.5
#Ho2: P(X>1060) = 0.5
#g1(x) = I[x > y]
#g2(y) = I[x > 1060]

mean<-c(0.5,0.5)
p<-2

xd1<-c(10,85,209,273,279,324,391,566,852,881,895,954,1101,1393,1669,1823,1941)
nx1=length(xd1)
yd1<-c(21,38,39,51,77,185,524,610,612,677,798,899,946,1010,1074,1147,1154,1329,1484,1602,1952)
ny1=length(yd1)

wxd1new<-c(2.267983, 1.123600, 1.121683, 1.121683, 1.121683, 1.121683, 1.121683,
  1.000000, 1.000000, 1.000000, 1.000000, 1.000000, 1.000000, 1.261740, 2.912753,
  2.912753, 2.912753)
muvec<-c(0.08835785, 0.04075290, 0.04012084, 0.04012084, 0.04012084, 0.04012084,
  0.04012084, 0.03538020, 0.03389263, 0.03389263, 0.03389263, 0.03322693, 0.04901516,
  0.05902008, 0.13065491, 0.13065491, 0.13065491)

wyd1new<-c(1.431653, 1.431653, 1.431653, 1.431653, 1.431653, 1.438453, 1.079955, 1.080832,
  1.080832, 1.080832, 1.080832, 1.000000, 1.000000, 1.000000, 1.000000, 1.000000, 1.000000,
  1.222883, 1.227865, 1.739636, 5.809616)
nuvec<-c(0.04249966, 0.04249966, 0.04249966, 0.04249966, 0.04249966, 0.04316922, 0.03425722,
  0.03463312, 0.03463312, 0.03463312, 0.03463312, 0.03300598, 0.03300598, 0.03333333,
  0.03333333, 0.03382827, 0.03382827, 0.04136800, 0.04229270, 0.05992020, 0.22762676)

H1u<-matrix(NA,nrow=nx1,ncol=ny1)
H2u<-matrix(NA,nrow=nx1,ncol=ny1)
for (i in 1:nx1) {
  for (j in 1:ny1) {
    H1u[i,j]<-(xd1[i]>yd1[j])
    H2u[i,j]<-(xd1[i]>1060) } }
Hu=matrix(c(H1u,H2u),nrow=nx1,ncol=p*ny1)
for (k in 1:p) {
  M1 <- matrix(mean[k], nrow=nx1, ncol=ny1)
  Hu[,((k-1)*ny1+1):(k*ny1)] <- Hu[,((k-1)*ny1+1):(k*ny1)] - M1}
Hmu <- matrix(NA,nrow=p, ncol=ny1*nx1)
Hnu <- matrix(NA,nrow=p, ncol=ny1*nx1)
for (i in 1:p) {
  for (k in 1:nx1) {
    Hmu[i, ((k-1)*ny1+1):(k*ny1)] <- Hu[k,((i-1)*ny1+1):(i*ny1)] } }
```

```

for (i in 1:p) {
  for (k in 1:ny1) {
    Hnu[i,((k-1)*nx1+1):(k*nx1)] <- Hu[(1:nx1),(i-1)*ny1+k]} }

el2.test.wtm(xd1,yd1,wdx1new, wyd1new, muvec, nuvec, Hu, Hmu,
  Hnu, p, mean, maxit=10)

#muvec1
# [1] 0.08835789 0.04075290 0.04012083 0.04012083 0.04012083 0.04012083 0.04012083
# [8] 0.03538021 0.03389264 0.03389264 0.03389264 0.03322693 0.04901513 0.05902002
# [15] 0.13065495 0.13065495 0.13065495

#nuvec1
# [1] 0.04249967 0.04249967 0.04249967 0.04249967 0.04249967 0.04316920 0.03425722
# [8] 0.03463310 0.03463310 0.03463310 0.03463310 0.03300597 0.03300597 0.03333333
# [15] 0.03333333 0.03382827 0.03382827 0.04136801 0.04229269 0.05992018 0.22762677

# $lam
#      [,1]      [,2]
# [1,] 8.9549 -10.29119

```

---

el2.test.wts

---

*Computes maximum-likelihood probability jumps for a single mean-type hypothesis, based on two independent uncensored samples*


---

## Description

This function computes the maximum-likelihood probability jumps for a single mean-type hypothesis, based on two samples that are independent, uncensored, and weighted. The target function (Lagrangian) for the maximization is the constrained log(empirical likelihood) which can be expressed as,

$$\sum_{dx_i=1} wx_i \log \mu_i + \sum_{dy_j=1} wy_j \log \nu_j - \eta(1 - \sum_{dx_i=1} \mu_i) - \delta(1 - \sum_{dy_j=1} \nu_j) - \lambda \sum_{dx_i=1} \sum_{dy_j=1} (g(x_i, y_j) - \text{mean}) \mu_i \nu_j$$

where the variables are defined as follows:

$x$  is a vector of data for the first sample

$y$  is a vector of data for the second sample

$wx$  is a vector of estimated weights for the first sample

$wy$  is a vector of estimated weights for the second sample

$\mu$  is a vector of estimated probability jumps for the first sample

$\nu$  is a vector of estimated probability jumps for the second sample

## Usage

```
el2.test.wts(u,v,wu,wv,mu0,nu0,indicmat,mean,lamOld=0)
```

**Arguments**

<code>u</code>	a vector of uncensored data for the first sample
<code>v</code>	a vector of uncensored data for the second sample
<code>wu</code>	a vector of estimated weights for <code>u</code>
<code>wv</code>	a vector of estimated weights for <code>v</code>
<code>mu0</code>	a vector of estimated probability jumps for <code>u</code>
<code>nu0</code>	a vector of estimated probability jumps for <code>v</code>
<code>indicmat</code>	a matrix $[g(u_i, v_j) - \text{mean}]$ where $g(u, v)$ is a user-chosen function
<code>mean</code>	a hypothesized value of $E(g(u, v))$ , where $E$ indicates “expected value.”
<code>lamOld</code>	The previous solution of $\lambda$ , used as the starting point to search for new solution of $\lambda$ .

**Details**

This function is called by `e12.cen.EMS`. It is listed here because the user may find it useful elsewhere.

The value of *mean* should be chosen between the maximum and minimum values of  $(u_i, v_j)$ ; otherwise there may be no distributions for  $u$  and  $v$  that will satisfy the mean-type hypothesis. If *mean* is inside this interval, but the convergence is still not satisfactory, then the value of *mean* should be moved closer to the NPMLE for  $E(g(u, v))$ . (The NPMLE itself should always be a feasible value for *mean*.) The calculations for this function are derived in Owen (2001).

**Value**

`e12.test.wts` returns a list of values as follows:

<code>u</code>	the vector of uncensored data for the first sample
<code>wu</code>	the vector of weights for $u$
<code>jumpu</code>	the vector of probability jumps for $u$ that maximize the weighted empirical likelihood
<code>v</code>	the vector of uncensored data for the second sample
<code>wv</code>	the vector of weights for $v$
<code>jumpv</code>	the vector of probability jumps for $v$ that maximize the weighted empirical likelihood
<code>lam</code>	the value of the Lagrangian multiplier found by the calculations

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**References**

Owen, A.B. (2001). Empirical Likelihood. Chapman and Hall/CRC, Boca Raton, pp.223-227.

**Examples**

```

u<-c(10, 209, 273, 279, 324, 391, 566, 785)
v<-c(21, 38, 39, 51, 77, 185, 240, 289, 524)
wu<-c(2.442931, 1.122365, 1.113239, 1.113239, 1.104113, 1.104113, 1.000000, 1.000000)
wv<-c( 1, 1, 1, 1, 1, 1, 1, 1, 1)
mu0<-c(0.3774461, 0.1042739, 0.09649724, 0.09649724, 0.08872055, 0.08872055, 0.0739222, 0.0739222)
nu0<-c(0.1013718, 0.1013718, 0.1013718, 0.1013718, 0.1013718, 0.1013718, 0.1095413, 0.1287447,
      0.1534831)
mean<-0.5

#let fun=function(x,y){x>=y}
indicmat<-matrix(nrow=8,ncol=9,c(
-0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,
-0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,
-0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,
-0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,
-0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,
-0.5, -0.5,  0.5,  0.5,  0.5,  0.5,  0.5,  0.5,
-0.5, -0.5, -0.5, -0.5,  0.5,  0.5,  0.5,  0.5,
-0.5, -0.5, -0.5, -0.5, -0.5, -0.5,  0.5,  0.5))
el2.test.wts(u,v,wu,wv,mu0,nu0,indicmat,mean)

# jumpu
# [1] 0.3774461, 0.1042739, 0.09649724, 0.09649724, 0.08872055, 0.08872055, 0.0739222, 0.0739222

# jumpv
# [1] 0.1013718, 0.1013718, 0.1013718, 0.1013718, 0.1013718, 0.1013718, 0.1095413, 0.1287447,
# [9] 0.1534831

# lam
# [1] 7.055471

```

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