# Package 'fGarch'

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Title Rmetrics - Autoregressive Conditional Heteroskedastic Modelling Version 4033.92 Description Analyze and model heteroskedastic behavior in financial time series. Imports fBasics, timeDate, timeSeries, fastICA, Matrix (>= 1.5-0), cvar (>= 0.5), graphics, methods, stats, utils Suggests RUnit, tcltk, goftest LazyData yes License GPL (>= 2) URL https://geobosh.github.io/fGarchDoc/(doc), https://www.rmetrics.org (devel) BugReports https://r-forge.r-project.org/projects/rmetrics NeedsCompilation yes Author Diethelm Wuertz [aut] (original code), Yohan Chalabi [aut], Tobias Setz [aut], Martin Maechler [aut] (ORCID: <https://orcid.org/0000-0002-8685-9910>),

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# Contents

fGarch-package												•	•	 																2
absMoments	•		•	•								•		 										•	•		•	•	•	5
coef-methods .			•	•	•	•	•	•	•	•	•	•	•	 		•	•	•	•			•			•	•		•	•	6
fGARCH-class			•					•	•	•	•	•	•	 		•	•				•				•			•		7

fGarchData	8
fGARCHSPEC-class	9
fitted-methods	10
formula-methods	11
fUGARCHSPEC-class	12
garchFit	13
garchFitControl	18
garchSim	21
garchSpec	24
ged	27
gedFit	29
gedSlider	30
plot-methods	31
predict-methods	33
residuals-methods	35
sged	36
sgedFit	37
sgedSlider	38
snorm	39
snormFit	41
snormSlider	42
sstd	43
sstdFit	44
sstdSlider	46
stats-tsdiag	47
std	49
stdFit	50
stdSlider	52
summary-methods	53
VaR	54
volatility-methods	56
	58

# Index

fGarch-package

Modelling heterskedasticity in financial time series

# Description

The Rmetrics **fGarch** package is a collection of functions to analyze and model heteroskedastic behavior in financial time series.

### fGarch-package

### **1** Introduction

GARCH, Generalized Autoregressive Conditional Heteroskedastic, models have become important in the analysis of time series data, particularly in financial applications when the goal is to analyze and forecast volatility.

For this purpose, the family of GARCH functions offers functions for simulating, estimating and forecasting various univariate GARCH-type time series models in the conditional variance and an ARMA specification in the conditional mean. The function garchFit is a numerical implementation of the maximum log-likelihood approach under different assumptions, Normal, Student-t, GED errors or their skewed versions. The parameter estimates are checked by several diagnostic analysis tools including graphical features and hypothesis tests. Functions to compute n-step ahead forecasts of both the conditional mean and variance are also available.

The number of GARCH models is immense, but the most influential models were the first. Beside the standard ARCH model introduced by Engle [1982] and the GARCH model introduced by Bollerslev [1986], the function garchFit also includes the more general class of asymmetric power ARCH models, named APARCH, introduced by Ding, Granger and Engle [1993]. The APARCH models include as special cases the TS-GARCH model of Taylor [1986] and Schwert [1989], the GJR-GARCH model of Glosten, Jaganathan, and Runkle [1993], the T-ARCH model of Zakoian [1993], the N-ARCH model of Higgins and Bera [1992], and the Log-ARCH model of Geweke [1986] and Pentula [1986].

There exist a collection of review articles by Bollerslev, Chou and Kroner [1992], Bera and Higgins [1993], Bollerslev, Engle and Nelson [1994], Engle [2001], Engle and Patton [2001], and Li, Ling and McAleer [2002] which give a good overview of the scope of the research.

# 2 Time series simulation

Functions to simulate artificial GARCH and APARCH time series processes.

garchSpec specifies an univariate GARCH time series model garchSim simulates a GARCH/APARCH process

### **3** Parameter estimation

Functions to fit the parameters of GARCH and APARCH time series processes.

garchFit fits the parameters of a GARCH process

# **Extractor Functions::**

residuals	extracts residuals from a fitted "fGARCH" object
fitted	extracts fitted values from a fitted "fGARCH" object
volatility	extracts conditional volatility from a fitted "fGARCH" object
coef	extracts coefficients from a fitted "fGARCH" object
formula	extracts formula expression from a fitted "fGARCH" object

### **4** Forecasting

Functions to forcecast mean and variance of GARCH and APARCH processes.

predict forecasts from an object of class "fGARCH"

### **5** Standardized distributions

This section contains functions to model standardized distributions.

### Skew normal distribution::

[dpqr]norm	Normal distribution (base R)
[dpqr]snorm	Skew normal distribution
snormFit	fits parameters of Skew normal distribution

### Skew generalized error distribution::

[dpqr]ged	Generalized error distribution
[dpqr]sged	Skew Generalized error distribution
gedFit	fits parameters of Generalized error distribution
sgedFit	fits parameters of Skew generalized error distribution

#### Skew standardized Student-t distribution::

[dpqr]std	Standardized Student-t distribution
[dpqr]sstd	Skew standardized Student-t distribution
stdFit	fits parameters of Standardized Student-t distribution
sstdFit	fits parameters of Skew standardized Student-t distribution

### Absolute moments::

absMoments computes absolute moments of these distribution

# **About Rmetrics**

The fGarch Rmetrics package is written for educational support in teaching "Computational Finance and Financial Engineering" and licensed under the GPL.

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absMoments

# Description

Computes absolute moments of the standard normal, standardized GED, and standardized skew Student-t distributions.

### Usage

```
absMoments(n, density = c("dnorm", "dged", "dstd"), ...)
```

### Arguments

n	the order of the absolute moment, can be a vector to compute several absolute moments at once.
density	a character string naming a symmetric density function.
	parameters passed to the density function.

# Details

absMoments returns a numeric vector of length n with the values of the absolute moments, as specified by n, of the selected probability density function (pdf).

If density names one of the densities in the signature of absMoments, the moments are calculated from known formulas.

Otherwise, numerical integration is used and an attribute is attached to the results to report an estimate of the error. Note that the density is assumed symmetric without a check.

### Value

a numeric vector

### Author(s)

Diethelm Wuertz for the Rmetrics R-port

### References

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

### See Also

ged, std

### Examples

## absMoment -

```
absMoments(1, "dstd", nu = 6)
absMoments(1, "dstd", nu = 600)
absMoments(1, "dstd", nu = 60000)
absMoments(1, "dstd", nu = 600000)
absMoments(1, "dnorm")
## excess kurtosis of t_nu is 6/(nu - 4)
nu <- 6
absMoments(2*2, "dstd", nu = nu) / absMoments(2*1, "dstd", nu = nu)^2 - 3
6/(nu-4)
## 4th moment for t_4 is infinite
absMoments(4, "dstd", nu = 4)
absMoments(1, "dged", nu = 4)
```

coef-methods GARCH coefficients methods

# Description

Coefficients methods coef() for GARCH Models.

# Methods

Methods for coef defined in package **fGarch**:

object = "fGARCH" Extractor function for coefficients from a fitted GARCH model.

**object = "fGARCHSPEC"** Extractor function for coefficients from a GARCH specification structure.

# Note

coef is a generic function which extracts coefficients from objects returned by modeling functions.

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

6

# fGARCH-class

# Examples

```
## garchSpec -
    # Use default parameters beside alpha:
    spec = garchSpec(model = list(alpha = c(0.05, 0.05)))
    spec
    coef(spec)
## garchSim -
    # Simulate an univariate "timeSeries" series from specification 'spec':
    x = garchSim(spec, n = 2000)
    x = x[,1]
## garchFit --
    fit = garchFit( ~ garch(1, 1), data = x, trace = FALSE)
## coef -
    coef(fit)
```

fGARCH-class Class "fGARCH"

### Description

The class 'fGARCH' represents a model of an heteroskedastic time series process.

### **Objects from the Class**

Objects can be created by calls of the function garchFit. This object is a parameter estimate of an empirical GARCH process.

### Slots

call: Object of class "call": the call of the garch function.

formula: Object of class "formula": a formula object specifying the mean and variance equations.

- method: Object of class "character": a string denoting the optimization method, by default "Max Log-Likelihood Estimation".
- data: Object of class "list": a list with one entry named x, containing the data of the time series to be estimated, the same as given by the input argument series.
- fit: Object of class "list": a list with the results from the parameter estimation. The entries of the list depend on the selected algorithm, see below.
- residuals: Object of class "numeric": a numeric vector with the (raw, unstandardized) residual values.
- fitted: Object of class "numeric": a numeric vector with the fitted values.
- h.t: Object of class "numeric":

a numeric vector with the conditional variances  $(h_t = \sigma_t^{\delta})$ .

sigma.t: Object of class "numeric": a numeric vector with the conditional standard deviations. title: Object of class "character": a title string.

description: Object of class "character": a string with a brief description.

# Methods

plot signature(x = "fGARCH", y = "missing"): plots an object of class "fGARCH".

show signature(object = "fGARCH"): prints an object of class "fGARCH".

summary signature(object = "fGARCH"): summarizes an object of class "fGARCH".

predict signature(object = "fGARCH"): forecasts mean and volatility from an object of class
 "fGARCH".

fitted signature(object = "fGARCH"): extracts fitted values from an object of class "fGARCH".

residuals signature(object = "fGARCH"): extracts fresiduals from an object of class "fGARCH".

volatility signature(object = "fGARCH"): extracts conditional volatility from an object of class "fGARCH".

**coef** signature(object = "fGARCH"): extracts fitted coefficients from an object of class "fGARCH".

formula signature(x = "fGARCH"): extracts formula expression from an object of class "fGARCH".

### Author(s)

Diethelm Wuertz and Rmetrics Core Team

### See Also

garchFit, garchSpec, garchFitControl

### Examples

```
## simulate a time series, fit a GARCH(1,1) model, and show it:
x <- garchSim( garchSpec(), n = 500)
fit <- garchFit(~ garch(1, 1), data = x, trace = FALSE)
fit # == print(fit) and also == show(fit)
```

fGarchData Time series datasets

### Description

Datasets used in the examples, including DEM/GBP foreign exchange rates and data on SP500 index.

# Format

dem2gbp is a data frame with one column "DEM2GBP" and 1974 rows (observations). sp500dge is a data frame with one column "SP500DGE" and 17055 rows (observations).

# fGARCHSPEC-class

### Details

The data represent returns. No further details have been recorded.

Further datasets are available in the packages that fGarch imports, see fBasicsData and TimeSeriesData.

# See Also

data(package = "fBasics") and data(package = "timeSeries") for related datasets

# Examples

```
data(dem2gbp)
head(dem2gbp)
tail(dem2gbp)
str(dem2gbp)
plot(dem2gbp[[1]])
data(sp500dge)
head(sp500dge)
tail(sp500dge)
str(sp500dge)
plot(sp500dge[[1]])
```

fGARCHSPEC-class Class "fGARCHSPEC"

### Description

Specification structure for an univariate GARCH time series model.

### **Objects from the Class**

Objects can be created by calls of the function garchSpec. This object specifies the parameters of an empirical GARCH process.

# Slots

call: Object of class "call": the call of the garch function.

formula: Object of class "formula": a list with two formula entries for the mean and variance equation.

model: Object of class "list": a list with the model parameters.

presample: Object of class "matrix": a numeric matrix with presample values.

distribution: Object of class "character": a character string with the name of the conditional distribution.

rseed: Object of class "numeric": an integer with the random number generator seed.

### Methods

show signature(object = "fGARCHSPEC"): prints an object of class 'fGARCHSPEC'.

### Note

With Rmetrics Version 2.6.1 the class has been renamed from "garchSpec" to "fGARCHSPEC".

### Author(s)

Diethelm Wuertz for the Rmetrics R-port

# Examples

```
## garchSpec -
   spec = garchSpec()
   spec # print() or show() it
```

fitted-methods Extract GARCH model fitted values

# Description

Extracts fitted values from a fitted GARCH object.

#### Details

The method for "fGARCH" objects extracts the @fitted value slot from an object of class "fGARCH" as returned by the function garchFit.

### Methods

Methods for fitted defined in package fGarch:

**object = "fGARCH"** Extractor function for fitted values.

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# See Also

predict, residuals, garchFit, class fGARCH,
plot

# Examples

## see examples for 'residuals()'

10

formula-methods

# Description

Extracts formula from a formula GARCH object.

### Details

formula is a generic function which extracts the formula expression from objects returned by modeling functions.

The "fGARCH" method extracts the @formula expression slot from an object of class "fGARCH" as returned by the function garchFit.

The returned formula has always a left hand side. If the argument data was an univariate time series and no name was specified to the series, then the left hand side is assigned the name of the data.set. In the multivariate case the rectangular data object must always have column names, otherwise the fitting will be stopped with an error message

The class of the returned value depends on the input to the function garchFit who created the object. The returned value is always of the same class as the input object to the argument data in the function garchFit, i.e. if you fit a "timeSeries" object, you will get back from the function fitted also a "timeSeries" object, if you fit an object of class "zoo", you will get back again a "zoo" object. The same holds for a "numeric" vector, for a "data.frame", and for objects of class "ts", "mts".

In contrast, the slot itself returns independent of the class of the data input always a numeric vector, i.e. the function call rslot(object, "fitted") will return a numeric vector.

# Methods

Methods for formula defined in package fGarch:

object = "fGARCH" Extractor function for formula expression.

### Note

(GNB) Contrary to the description of the returned value of the "fGARCH" method, it is always "numeric".

TODO: either implement the documented behaviour or fix the documentation.

### Author(s)

Diethelm Wuertz for the Rmetrics R-port

### See Also

garchFit, class fGARCH

### Examples

```
## garchFit -
  fit = garchFit(~garch(1, 1), data = garchSim(), trace = FALSE)
## formula -
  formula(fit)
## A Bivariate series and mis-specified formula:
  x = garchSim(n = 500)
  y = garchSim(n = 500)
  z = cbind(x, y)
  colnames(z)
  class(z)
  ## Not run:
  garchFit(z ~garch(1, 1), data = z, trace = FALSE)
## End(Not run)
  # Returns:
  # Error in .garchArgsParser(formula = formula, data = data, trace = FALSE) :
  # Formula and data units do not match.
## Doubled column names in data set - formula can't fit:
  colnames(z) <- c("x", "x")
  z[1:6,]
   ## Not run:
  garchFit(x ~garch(1, 1), data = z, trace = FALSE)
## End(Not run)
  # Again the error will be noticed:
  # Error in garchFit(x ~ garch(1, 1), data = z) :
  # Column names of data are not unique.
## Missing column names in data set - formula can't fit:
  z.mat <- as.matrix(z)</pre>
  colnames(z.mat) <- NULL</pre>
  z.mat[1:6,]
   ## Not run:
  garchFit(x ~ garch(1, 1), data = z.mat, trace = FALSE)
## End(Not run)
  # Again the error will be noticed:
  # Error in .garchArgsParser(formula = formula, data = data, trace = FALSE) :
  # Formula and data units do not match
```

fUGARCHSPEC-class Class 'fUGARCHSPEC'

# Description

Class 'fUGARCHSPEC'.

12

# garchFit

# **Objects from the Class**

Objects can be created by calls of the form new("fUGARCHSPEC", ...).

### Slots

model: Object of class "list" ~~
distribution: Object of class "list" ~~
optimization: Object of class "list" ~~
documentation: Object of class "list" ~~

# Methods

No methods defined with class "fUGARCHSPEC" in the signature.

# Note

(GNB) This class seems to be meant for internal use by the package.

### See Also

class "fGARCH"

### Examples

showClass("fUGARCHSPEC")

garchFit

Univariate or multivariate GARCH time series fitting

### Description

Estimates the parameters of a univariate ARMA-GARCH/APARCH process, or — experimentally — of a multivariate GO-GARCH process model. The latter uses an algorithm based on fastICA(), inspired from Bernhard Pfaff's package gogarch.

# Usage

```
hessian = c("ropt", "rcd"),
        control = list(),
        title = NULL, description = NULL, ...)
garchKappa(cond.dist = c("norm", "ged", "std", "snorm", "sged", "sstd", "snig"),
           gamma = 0, delta = 2, skew = NA, shape = NA)
.gogarchFit(formula = ~garch(1, 1), data, init.rec = c("mci", "uev"),
            delta = 2, skew = 1, shape = 4,
            cond.dist = c("norm", "snorm", "ged", "sged",
                          "std", "sstd", "snig", "QMLE"),
            include.mean = TRUE, include.delta = NULL, include.skew = NULL,
            include.shape = NULL,
            leverage = NULL, trace = TRUE,
            algorithm = c("nlminb", "lbfgsb", "nlminb+nm", "lbfgsb+nm"),
            hessian = c("ropt", "rcd"),
            control = list(),
            title = NULL, description = NULL, ...)
```

# Arguments

algorithm	a string parameter that determines the algorithm used for maximum likelihood estimation.
cond.dist	a character string naming the desired conditional distribution. Valid values are "dnorm", "dged", "dstd", "dsnorm", "dsged", "dsstd" and "QMLE". The default value is the normal distribution. See Details for more information.
control	control parameters, the same as used for the functions from nlminb, and 'bfgs' and 'Nelder-Mead' from optim.
data	an optional timeSeries or data frame object containing the variables in the model. If not found in data, the variables are taken from environment(formula), typ- ically the environment from which armaFit is called. If data is an univariate series, then the series is converted into a numeric vector and the name of the response in the formula will be neglected.
delta	a numeric value, the exponent delta of the variance recursion. By default, this value will be fixed, otherwise the exponent will be estimated together with the other model parameters if include.delta=FALSE.
description	optional character string with a brief description.
formula	<b>formula</b> object describing the mean and variance equation of the ARMA-GARCH/APARCH model. A pure GARCH(1,1) model is selected e.g., for formula = ~garch(1,1). To specify an ARMA(2,1)-APARCH(1,1) process, use ~ arma(2,1) + aparch(1,1).
gamma	APARCH leverage parameter entering into the formula for calculating the expectation value.
hessian	a string denoting how the Hessian matrix should be evaluated, either hessian ="rcd", or "ropt". The default, "rcd" is a central difference approximation implemented in R and "ropt" uses the internal R function optimhess.

# garchFit

include.delta	a logical determining if the parameter for the recursion equation delta will be estimated or not. If false, the shape parameter will be kept fixed during the process of parameter optimization.
include.mean	this flag determines if the parameter for the mean will be estimated or not. If include.mean=TRUE this will be the case, otherwise the parameter will be kept fixed durcing the process of parameter optimization.
include.shape	a logical flag which determines if the parameter for the shape of the conditional distribution will be estimated or not. If include.shape=FALSE then the shape parameter will be kept fixed during the process of parameter optimization.
include.skew	a logical flag which determines if the parameter for the skewness of the con- ditional distribution will be estimated or not. If include.skew=FALSE then the skewness parameter will be kept fixed during the process of parameter optimiza- tion.
init.rec	a character string indicating the method how to initialize the mean and varaince recursion relation.
leverage	a logical flag for APARCH models. Should the model be leveraged? By default leverage=TRUE.
shape	a numeric value, the shape parameter of the conditional distribution.
skew	a numeric value, the skewness parameter of the conditional distribution.
title	a character string which allows for a project title.
trace	a logical flag. Should the optimization process of fitting the model parameters be printed? By default trace=TRUE.
	additional arguments to be passed.

# Details

"QMLE" stands for Quasi-Maximum Likelihood Estimation, which assumes normal distribution and uses robust standard errors for inference. Bollerslev and Wooldridge (1992) proved that if the mean and the volatility equations are correctly specified, the QML estimates are consistent and asymptotically normally distributed. However, the estimates are not efficient and "the efficiency loss can be marked under asymmetric ... distributions" (Bollerslev and Wooldridge (1992), p. 166). The robust variance-covariance matrix of the estimates equals the (Eicker-White) sandwich estimator, i.e.

$$V = H^{-1}G'GH^{-1},$$

where V denotes the variance-covariance matrix, H stands for the Hessian and G represents the matrix of contributions to the gradient, the elements of which are defined as

$$G_{t,i} = \frac{\partial l_t}{\partial \zeta_i},$$

where  $t_t$  is the log likelihood of the t-th observation and  $\zeta_i$  is the i-th estimated parameter. See sections 10.3 and 10.4 in Davidson and MacKinnon (2004) for a more detailed description of the robust variance-covariance matrix.

### Value

for garchFit, an S4 object of class "fGARCH". Slot @fit contains the results from the optimization.

for .gogarchFit(): Similar definition for GO-GARCH modeling. Here, data must be *multivariate*. Still "preliminary", mostly undocumented, and untested(!). At least mentioned here...

### Author(s)

Diethelm Wuertz for the Rmetrics R-port, R Core Team for the 'optim' R-port, Douglas Bates and Deepayan Sarkar for the 'nlminb' R-port, Bell-Labs for the underlying PORT Library, Ladislav Luksan for the underlying Fortran SQP Routine, Zhu, Byrd, Lu-Chen and Nocedal for the underlying L-BFGS-B Routine. Martin Maechler for cleaning up; *mentioning* .gogarchFit().

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Nocedal J., Wright S.J. (1999); Numerical Optimization, Springer, New York.

### See Also

garchSpec, garchFitControl, class "fGARCH"

# Examples

## UNIVARIATE TIME SERIES INPUT:

# In the univariate case the lhs formula has not to be specified ....

# A numeric Vector from default GARCH(1,1) - fix the seed:

### garchFit

```
N = 200
   x.vec = as.vector(garchSim(garchSpec(rseed = 1985), n = N)[,1])
  garchFit(~ garch(1,1), data = x.vec, trace = FALSE)
  # An univariate timeSeries object with dummy dates:
  stopifnot(require("timeSeries"))
   x.timeSeries = dummyDailySeries(matrix(x.vec), units = "GARCH11")
  garchFit(~ garch(1,1), data = x.timeSeries, trace = FALSE)
## Not run:
   # An univariate zoo object:
  require("zoo")
  x.zoo = zoo(as.vector(x.vec), order.by = as.Date(rownames(x.timeSeries)))
  garchFit(~ garch(1,1), data = x.zoo, trace = FALSE)
## End(Not run)
  # An univariate "ts" object:
  x.ts = as.ts(x.vec)
  garchFit(~ garch(1,1), data = x.ts, trace = FALSE)
## MULTIVARIATE TIME SERIES INPUT:
   # For multivariate data inputs the lhs formula must be specified ...
  # A numeric matrix binded with dummy random normal variates:
  X.mat = cbind(GARCH11 = x.vec, R = rnorm(N))
   garchFit(GARCH11 ~ garch(1,1), data = X.mat)
   # A multivariate timeSeries object with dummy dates:
  X.timeSeries = dummyDailySeries(X.mat, units = c("GARCH11", "R"))
  garchFit(GARCH11 ~ garch(1,1), data = X.timeSeries)
## Not run:
   # A multivariate zoo object:
  X.zoo = zoo(X.mat, order.by = as.Date(rownames(x.timeSeries)))
  garchFit(GARCH11 ~ garch(1,1), data = X.zoo)
## End(Not run)
   # A multivariate "mts" object:
  X.mts = as.ts(X.mat)
   garchFit(GARCH11 ~ garch(1,1), data = X.mts)
## MODELING THE PERCENTUAL SPI/SBI SPREAD FROM LPP BENCHMARK:
   stopifnot(require("timeSeries"))
  X.timeSeries = as.timeSeries(data(LPP2005REC))
  X.mat = as.matrix(X.timeSeries)
   ## Not run: X.zoo = zoo(X.mat, order.by = as.Date(rownames(X.mat)))
  X.mts = ts(X.mat)
  garchFit(100*(SPI - SBI) ~ garch(1,1), data = X.timeSeries)
   # The remaining are not yet supported ...
   # garchFit(100*(SPI - SBI) ~ garch(1,1), data = X.mat)
```

```
# garchFit(100*(SPI - SBI) ~ garch(1,1), data = X.zoo)
# garchFit(100*(SPI - SBI) ~ garch(1,1), data = X.mts)
## MODELING HIGH/LOW RETURN SPREADS FROM MSFT PRICE SERIES:
X.timeSeries = MSFT
garchFit(Open ~ garch(1,1), data = returns(X.timeSeries))
garchFit(100*(High-Low) ~ garch(1,1), data = returns(X.timeSeries))
## GO-GARCH Modelling (not yet!!) % FIXME
## data(DowJones30, package="fEcofin") # no longer exists
## X = returns(as.timeSeries(DowJones30)); head(X)
## N = 5; ans = .gogarchFit(data = X[, 1:N], trace = FALSE); ans
## ans@h.t
```

garchFitControl Control GARCH fitting algorithms

### Description

Control parameters for the GARCH fitting algorithms.

# Usage

```
garchFitControl(
    llh = c("filter", "internal", "testing"),
    nlminb.eval.max = 2000,
    nlminb.iter.max = 1500,
    nlminb.abs.tol = 1.0e-20,
    nlminb.rel.tol = 1.0e-14,
   nlminb.x.tol = 1.0e-14,
    nlminb.step.min = 2.2e-14,
    nlminb.scale = 1,
    nlminb.fscale = FALSE,
    nlminb.xscale = FALSE,
    sqp.mit = 200,
    sqp.mfv = 500,
    sqp.met = 2,
    sqp.mec = 2,
    sqp.mer = 1,
    sqp.mes = 4,
    sqp.xmax = 1.0e3,
    sqp.tolx = 1.0e-16,
    sqp.tolc = 1.0e-6,
    sqp.tolg = 1.0e-6,
    sqp.told = 1.0e-6,
```

# garchFitControl

```
sqp.tols = 1.0e-4,
sqp.rpf = 1.0e-4,
lbfgsb.REPORT = 10,
lbfgsb.lmm = 20,
lbfgsb.pgtol = 1e-14,
lbfgsb.factr = 1,
lbfgsb.fnscale = FALSE,
lbfgsb.parscale = FALSE,
nm.ndeps = 1e-14,
nm.maxit = 10000,
nm.abstol = 1e-14,
nm.reltol = 1e-14,
nm.alpha = 1.0,
nm.beta = 0.5,
nm.gamma = 2.0,
nm.fnscale = FALSE,
nm.parscale = FALSE)
```

# Arguments

<pre>llh = c("filter", "internal", "testing")[1], defaults to "filter".</pre>
maximum number of evaluations of the objective function, defaults to 200.
maximum number of iterations, defaults to 150.
absolute tolerance, defaults to 1e-20.
relative tolerance, defaults to 1e-10.
X tolerance, defaults to 1.5e-8.
defaults to FALSE.
defaulkts to FALSE.
minimum step size, defaults to 2.2e-14.
defaults to 1.
maximum number of iterations, defaults to 200.
maximum number of function evaluations, defaults to 500.
specifies scaling strategy:
sqp.met=1 - no scaling,
sqp.met=2 - preliminary scaling in 1st iteration (default),
sqp.met=3 - controlled scaling,
sup met=5 - permanent scaling in all iterations
compation for possible compating
son mec $-1$ - no correction
sqp.mec=2 - Powell correction (default).

sqp.mer	restarts after unsuccessful variable metric updates: sqp.mer=0 - no restarts, sqp.mer=1 - standard restart.
sqp.mes	interpolation method selection in a line search: sqp.mes=1 - bisection, sqp.mes=2 - two point quadratic interpolation, sqp.mes=3 - three point quadratic interpolation, sqp.mes=4 - three point cubic interpolation (default).
sqp.xmax	maximum stepsize, defaults to 1.0e+3.
sqp.tolx	tolerance for the change of the coordinate vector, defaults to 1.0e-16.
sqp.tolc	tolerance for the constraint violation, defaults to 1.0e-6.
sqp.tolg	tolerance for the Lagrangian function gradient, defaults to 1.0e-6.
sqp.told	defaults to 1.0e-6.
sqp.tols	defaults to 1.0e-4.
sqp.rpf	value of the penalty coefficient, default to1.0D-4. The default velue may be rel- atively small. Therefore, larger value, say one, can sometimes be more suitable.
lbfgsb.REPORT	the frequency of reports for the "BFGS" and "L-BFGS-B" methods if control\$trace is positive. Defaults to every 10 iterations.
lbfgsb.lmm	an integer giving the number of BFGS updates retained in the "L-BFGS-B" method, It defaults to 5.
lbfgsb.factr	controls the convergence of the "L-BFGS-B" method. Convergence occurs when the reduction in the objective is within this factor of the machine tolerance. De- fault is 1e7, that is a tolerance of about 1.0e-8.
lbfgsb.pgtol	helps control the convergence of the "L-BFGS-B" method. It is a tolerance on the projected gradient in the current search direction. This defaults to zero, when the check is suppressed.
lbfgsb.fnscale	defaults to FALSE.
lbfgsb.parscale	
	defaults to FALSE.
nm.ndeps	a vector of step sizes for the finite-difference approximation to the gradient, on par/parscale scale. Defaults to 1e-3.
nm.maxit	the maximum number of iterations. Defaults to 100 for the derivative-based methods, and 500 for "Nelder-Mead". For "SANN" maxit gives the total number of function evaluations. There is no other stopping criterion. Defaults to 10000.
nm.abstol	the absolute convergence tolerance. Only useful for non-negative functions, as a tolerance for reaching zero.
nm.reltol	relative convergence tolerance. The algorithm stops if it is unable to reduce the value by a factor of reltol * (abs(val) + reltol) at a step. Defaults to sqrt(.Machine\$double.eps), typically about 1e-8.
nm.alpha,nm.bet	a, nm. gamma
	scaling parameters for the "Nelder-Mead" method. alpha is the reflection factor (default 1.0), beta the contraction factor (0.5), and gamma the expansion factor (2.0).

# garchSim

nm.fnscale	an overall scaling to be applied to the value of fn and gr during optimization.
	If negative, turns the problem into a maximization problem. Optimization is
	performed on fn(par) / nm.fnscale.
nm.parscale	a vector of scaling values for the parameters. Optimization is performed on par/parscale and these should be comparable in the sense that a unit change in any element produces about a unit change in the scaled value.

# Value

a list

# Author(s)

Diethelm Wuertz for the Rmetrics R-port, R Core Team for the 'optim' R-port, Douglas Bates and Deepayan Sarkar for the 'nlminb' R-port, Bell-Labs for the underlying PORT Library, Ladislav Luksan for the underlying Fortran SQP Routine, Zhu, Byrd, Lu-Chen and Nocedal for the underlying L-BFGS-B Routine.

# See Also

garchFit

### Examples

##

Simulate univariate GARCH/APARCH time series

# Description

Simulates univariate GARCH/APARCH time series.

# Usage

```
garchSim(spec = garchSpec(), n = 100, n.start = 100, extended = FALSE)
```

# Arguments

spec	a specification object of class "fGARCHSPEC" as returned by garchSpec. See also below for further details.	
n	length of the output series, an integer value, by default n=100.	
n.start	length of 'burn-in' period, by default 100.	
extended	logical parameter specifying what to return. If FALSE, return the univariate GARCH/APARCH time series. If TRUE, return a multivariate time series con- taining also the volatility and conditional innovations time series.	

### Details

garchSim simulates an univariate GARCH or APARCH time series process as specified by argument spec. The default model specifies Bollerslev's GARCH(1,1) model with normally distributed innovations.

spec is an object of class "fGARCHSPEC" as returned by the function garchSpec. It comes with a slot @model which is a list of just the numeric parameter entries. These are recognized and extracted for use by the function garchSim.

One can estimate the parameters of a GARCH process from empirical data using the function garchFit and then simulate statistically equivalent GARCH processes with the same set of model parameters using the function garchSim.

### Value

the simulated time series as an objects of class "timeSeries" with attribute "spec" containing the specification of the model.

If extended is TRUE, then the time series is multivariate and contains also the volatility, sigma, and the conditional innovations, eps.

### Note

An undocumented feature (so, it should not be relied on) is that the returned time series is timed so that the last observation is the day before the date when the function is executed. This probably should be controlled by an additional argument in garchSim.

### Author(s)

Diethelm Wuertz for the Rmetrics R-port

### See Also

garchSpec, garchFit

### Examples

```
## garchSpec -
   spec = garchSpec()
   spec
## garchSim -
    # Simulate a "timeSeries" object:
   x = garchSim(spec, n = 50)
   class(x)
   print(x)
## More simulations ...
```

```
# Default GARCH(1,1) - uses default parameter settings
spec = garchSpec(model = list())
garchSim(spec, n = 10)
```

```
# ARCH(2) - use default omega and specify alpha, set beta=0!
spec = garchSpec(model = list(alpha = c(0.2, 0.4), beta = 0))
garchSim(spec, n = 10)
# AR(1)-ARCH(2) - use default mu, omega
spec = garchSpec(model = list(ar = 0.5, alpha = c(0.3, 0.4), beta = 0))
garchSim(spec, n = 10)
# AR([1,5])-GARCH(1,1) - use default garch values and subset ar[.]
spec = garchSpec(model = list(mu = 0.001, ar = c(0.5,0,0,0,0.1)))
garchSim(spec, n = 10)
# ARMA(1,2)-GARCH(1,1) - use default garch values
spec = garchSpec(model = list(ar = 0.5, ma = c(0.3, -0.3)))
garchSim(spec, n = 10)
# GARCH(1,1) - use default omega and specify alpha/beta
spec = garchSpec(model = list(alpha = 0.2, beta = 0.7))
garchSim(spec, n = 10)
# GARCH(1,1) - specify omega/alpha/beta
spec = garchSpec(model = list(omega = 1e-6, alpha = 0.1, beta = 0.8))
garchSim(spec, n = 10)
# GARCH(1,2) - use default omega and specify alpha[1]/beta[2]
spec = garchSpec(model = list(alpha = 0.1, beta = c(0.4, 0.4)))
garchSim(spec, n = 10)
# GARCH(2,1) - use default omega and specify alpha[2]/beta[1]
spec = garchSpec(model = list(alpha = c(0.12, 0.04), beta = 0.08))
garchSim(spec, n = 10)
# snorm-ARCH(1) - use defaults with skew Normal
spec = garchSpec(model = list(beta = 0, skew = 0.8), cond.dist = "snorm")
garchSim(spec, n = 10)
# sged-GARCH(1,1) - using defaults with skew GED
model = garchSpec(model = list(skew = 0.93, shape = 3), cond.dist = "sged")
garchSim(model, n = 10)
# Taylor Schwert GARCH(1,1) - this belongs to the family of APARCH Models
spec = garchSpec(model = list(delta = 1))
garchSim(spec, n = 10)
# AR(1)-t-APARCH(2, 1) - a little bit more complex specification ...
spec = garchSpec(model = list(mu = 1.0e-4, ar = 0.5, omega = 1.0e-6,
    alpha = c(0.10, 0.05), gamma = c(0, 0), beta = 0.8, delta = 1.8,
    shape = 4, skew = 0.85), cond.dist = "sstd")
garchSim(spec, n = 10)
garchSim(spec, n = 10, extended = TRUE)
```

garchSpec

### Description

Specifies an univariate ARMA-GARCH or ARMA-APARCH time series model.

# Usage

```
garchSpec(model = list(), presample = NULL,
    cond.dist = c("norm", "ged", "std", "snorm", "sged", "sstd"),
    rseed = NULL)
```

# Arguments

cond.dist	a character string naming the desired conditional distribution. Valid values are "norm", "ged", "std", "snorm", "sged", "sstd". The default value is "norm", the standard normal distribution.
model	a list of GARCH model parameters, see section 'Details'. The default model=list() specifies Bollerslev's GARCH(1,1) model with normal conditional distributed innovations.
presample	a numeric three column matrix with start values for the series, for the innovations, and for the conditional variances. For an ARMA(m,n)-GARCH(p,q) process the number of rows must be at least $max(m,n,p,q)+1$ , longer presamples are truncated. Note, all presamples are initialized by a normal-GARCH(p,q) process.
rseed	single integer argument, the seed for the intitialization of the random number generator for the innovations. If rseed=NULL, the default, then the state of the random number generator is not touched by this function.

# Details

The function garchSpec specifies a GARCH or APARCH time series process which we can use for simulating artificial GARCH and/or APARCH models. This is very useful for testing the GARCH parameter estimation results, since your model parameters are known and well specified.

Argument model is a list of model parameters. For the GARCH part of the model they are:

omega the constant coefficient of the variance equation, by default 1e-6;

alpha the value or vector of autoregressive coefficients, by default 0.1, specifying a model of order 1;

beta the value or vector of variance coefficients, by default 0.8, specifying a model of order 1.

If the model is APARCH, then the following additional parameters are available:

delta a positive number, the power of sigma in the volatility equation, it is 2 for GARCH models;

gamma the leverage parameters, a vector of length alpha, containing numbers in the interval (0,1).

The values for the linear part (conditional mean) are:

mu the mean value, by default NULL;

- ar the autoregressive ARMA coefficients, by default NULL;
- ma the moving average ARMA coefficients, by default NULL.

The parameters for the conditional distributions are:

- skew the skewness parameter (also named "xi"), by default 0.9, effective only for the "dsnorm", the "dsged", and the "dsstd" skewed conditional distributions;
- shape the shape parameter (also named "nu"), by default 2 for the "dged" and "dsged", and by default 4 for the "dstd" and "dsstd" conditional distributions.

For example, specifying a subset AR(5[1,5])-GARCH(2,1) model with a standardized Student-t distribution with four degrees of freedom will return the following printed output:

```
garchSpec(model = list(ar = c(0.5,0,0,0,0.1), alpha =
    c(0.1, 0.1), beta = 0.75, shape = 4), cond.dist = "std")
Formula:
~ ar(5) + garch(2, 1)
Model:
        0.5 0 0 0 0.1
 ar:
 omega: 1e-06
 alpha: 0.1 0.1
 beta: 0.75
Distribution:
 std
Distributional Parameter:
nu = 4
Presample:
   time
                 Ζ
                       h y
0
      0 -0.3262334 2e-05 0
-1
    -1 1.3297993 2e-05 0
-2
   -2 1.2724293 2e-05 0
-3
    -3 0.4146414 2e-05 0
-4
     -4 -1.5399500 2e-05 0
```

Its interpretation is as follows. 'Formula' describes the formula expression specifying the generating process, 'Model' lists the associated model parameters, 'Distribution' the type of the conditional distribution function in use, 'Distributional Parameters' lists the distributional parameter (if any), and the 'Presample' shows the presample input matrix.

If we have specified presample = NULL in the argument list, then the presample is generated automatically by default as norm-AR()-GARCH() process.

### Value

an object of class "fGARCHSPEC"

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# See Also

garchSim, garchFit

### Examples

```
## garchSpec -
   # Normal Conditional Distribution:
  spec = garchSpec()
  spec
   # Skewed Normal Conditional Distribution:
   spec = garchSpec(model = list(skew = 0.8), cond.dist = "snorm")
   spec
   # Skewed GED Conditional Distribution:
   spec = garchSpec(model = list(skew = 0.9, shape = 4.8), cond.dist = "sged")
  spec
## More specifications ...
   # Default GARCH(1,1) - uses default parameter settings
  garchSpec(model = list())
  # ARCH(2) - use default omega and specify alpha, set beta=0!
  garchSpec(model = list(alpha = c(0.2, 0.4), beta = 0))
  # AR(1)-ARCH(2) - use default mu, omega
  garchSpec(model = list(ar = 0.5, alpha = c(0.3, 0.4), beta = 0))
  # AR([1,5])-GARCH(1,1) - use default garch values and subset ar[.]
  garchSpec(model = list(mu = 0.001, ar = c(0.5,0,0,0,0.1)))
   # ARMA(1,2)-GARCH(1,1) - use default garch values
  garchSpec(model = list(ar = 0.5, ma = c(0.3, -0.3)))
  # GARCH(1,1) - use default omega and specify alpha/beta
  garchSpec(model = list(alpha = 0.2, beta = 0.7))
   # GARCH(1,1) - specify omega/alpha/beta
  garchSpec(model = list(omega = 1e-6, alpha = 0.1, beta = 0.8))
  # GARCH(1,2) - use default omega and specify alpha[1]/beta[2]
  garchSpec(model = list(alpha = 0.1, beta = c(0.4, 0.4)))
```

26



Standardized generalized error distribution

### Description

Functions to compute density, distribution function, quantile function and to generate random variates for the standardized generalized error distribution.

# Usage

dged(x, mean = 0, sd = 1, nu = 2, log = FALSE)
pged(q, mean = 0, sd = 1, nu = 2)
qged(p, mean = 0, sd = 1, nu = 2)
rged(n, mean = 0, sd = 1, nu = 2)

#### Arguments

x, q	a numeric vector of quantiles.
р	a numeric vector of probabilities.
n	number of observations to simulate.
mean	location parameter.
sd	scale parameter.
nu	shape parameter.
log	logical; if TRUE, densities are given as log densities.

### Details

The standardized GED is defined so that for a given sd it has the same variance, sd<sup>2</sup>, for all values of the shape parameter, see the reference by Wuertz et al below.

dged computes the density, pged the distribution function, qged the quantile function, and rged generates random deviates from the standardized-t distribution with the specified parameters.

### Value

numeric vector

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# References

Nelson D.B. (1991); Conditional Heteroscedasticity in Asset Returns: A New Approach, Econometrica, 59, 347–370.

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

Wuertz D., Chalabi Y. and Luksan L. (????); *Parameter estimation of ARMA models with GARCH/APARCH errors: An R and SPlus software implementation*, Preprint, 41 pages, https://github.com/GeoBosh/fGarchDoc/blob/master/WurtzEtAlGarch.pdf

# See Also

gedFit, absMoments, sged (skew GED),

gedSlider for visualization

### Examples

```
## sged -
  par(mfrow = c(2, 2))
  set.seed(1953)
  r = rsged(n = 1000)
  plot(r, type = "1", main = "sged", col = "steelblue")
  # Plot empirical density and compare with true density:
  hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
  box()
  x = seq(min(r), max(r), length = 201)
  lines(x, dsged(x), lwd = 2)
  # Plot df and compare with true df:
  plot(sort(r), (1:1000/1000), main = "Probability", col = "steelblue",
    ylab = "Probability")
  lines(x, psged(x), lwd = 2)
  # Compute quantiles:
  round(qsged(psged(q = seq(-1, 5, by = 1))), digits = 6)
```

28

gedFit

# Description

Function to fit the parameters of the generalized error distribution.

### Usage

gedFit(x, ...)

# Arguments

х	a numeric vector of quantiles.
	parameters parsed to the optimization function ${\tt nlm}.$

# Value

gedFit returns a list with the following components:

par	The best set of parameters found.
objective	The value of objective corresponding to par.
convergence	An integer code, 0 indicates successful convergence.
message	A character string giving any additional information returned by the optimizer or NULL. For details, see PORT documentation.
iterations	Number of iterations performed.
evaluations	Number of objective function and gradient function evaluations.

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# References

Nelson D.B. (1991); Conditional Heteroscedasticity in Asset Returns: A New Approach, Econometrica, 59, 347–370.

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

### See Also

ged, sgedFit

# Examples

```
## rged -
    set.seed(1953)
    r = rged(n = 1000)
## gedFit -
    gedFit(r)
```

gedSlider

Generalized error distribution slider

# Description

Displays interactively the dependence of the GED distribution on its parameters.

# Usage

gedSlider(type = c("dist", "rand"))

### Arguments

type

a character string denoting which interactive plot should be displayed. Either a distribution plot type = "dist", the default value, or a random variates plot, type = "rand".

# Value

a Tcl object

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

### References

Nelson D.B. (1991); Conditional Heteroscedasticity in Asset Returns: A New Approach, Econometrica, 59, 347–370.

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

### See Also

ged, gedFit

30

### plot-methods

### Examples

```
## Not run:
## gedSlider -
    require(tcltk)
    gedSlider("dist")
    gedSlider("rand")
```

## End(Not run)

plot-methods GARCH plot methods

### Description

Plot methods for GARCH modelling.

### Usage

```
## S4 method for signature 'fGARCH,missing'
plot(x, which = "ask", ...)
```

# Arguments

Х	an object of class "fGARCH".
which	a character string or a vector of positive integers specifying which plot(s) should be displayed, see section 'Details'.
	optional arguments to be passed.

# Details

The plot method for "fGARCH" objects offers a selection of diagnostic, exploratory, and presentation plots from a menu. Argument which can be used to request specific plots. This is particularly useful in scripts.

If which is of length larger than one, all requested plots are produced. For this to be useful, the graphics window should be split beforehand in subwindows, e.g., using par(mfrow = ...), par(mfcol = ...), or layout() (see section 'Examples'). If this is not done, then only the last plot will be visible.

The following graphs are available:

- 1 Time SeriesPlot
- 2 Conditional Standard Deviation Plot
- 3 Series Plot with 2 Conditional SD Superimposed
- 4 Autocorrelation function Plot of Observations
- 5 Autocorrelation function Plot of Squared Observations
- 6 Cross Correlation Plot
- 7 Residuals Plot

- 8 Conditional Standard Deviations Plot
- 9 Standardized Residuals Plot
- 10 ACF Plot of Standardized Residuals
- 11 ACF Plot of Squared Standardized Residuals
- 12 Cross Correlation Plot between \$r^2\$ and r
- 13 Quantile-Quantile Plot of Standardized Residuals
- 14 Series with -VaR Superimposed
- 15 Series with -ES Superimposed
- 16 Series with -VaR & -ES Superimposed

# Author(s)

Diethelm Wuertz for the Rmetrics R-port;

VaR and ES graphs were added by Georgi N. Boshnakov in v4033.92

# See Also

fGARCH method for tsdiag, garchFit, class fGARCH, predict, fitted, residuals VaR ES plot

# Examples

```
## simulate a Garch(1,1) time series
x \leq garchSim(n = 200)
head(x)
## fit GARCH(1,1) model
fit <- garchFit(formula = ~ garch(1, 1), data = x, trace = FALSE)</pre>
## Not run:
## choose plots interactively
plot(fit)
## End(Not run)
## Batch Plot:
plot(fit, which = 3)
## a 2 by 2 matrix of plots
op <- par(mfrow = c(2,2))
                                    # prepare 2x2 window
plot(fit, which = c(10, 11, 3, 16)) # plot
par(op)
                                    # restore the previous layout
```

predict-methods GA

### Description

Predicts a time series from a fitted GARCH object.

### Usage

# Arguments

an integer value, denoting the number of steps to be forecasted, by default 10.
an object of class "fGARCH" as returned by the function garchFit.
a logical flag. Should the prediction process be traced? By default trace=FALSE.
If set to "cond", meanError is defined as the conditional mean errors $\sqrt{E_t[x_{t+h} - E_t(x_{t+h})]^2}$ If set to "uncond", it is defined as $\sqrt{E[x_{t+h} - E_t(x_{t+h})]^2}$ .
If set to TRUE, the confidence intervals are computed and plotted
The number of observations to be plotted along with the predictions. The default is round( $n*0.25$ ), where n is the sample size.
The critical values for the confidence intervals when plot is set to TRUE. The intervals are defined as $\hat{x}_{t+h} + \text{crit\_val[2]} * \text{meanError}$ and $\hat{x}_{t+h} + \text{crit\_val[1]} * \text{meanError}$ if two critical values are provided and $\hat{x}_{t+h} \pm \text{crit\_val} * \text{meanError}$ if only one is given. If you do not provide critical values, they will be computed automatically.
The confidence level for the confidence intervals if crit_val is not provided. By default it is set to 0.95. The critical values are then computed using the conditional distribution that was chosen to create the object with garchFit using the same shape and skew parameters. If the conditionnal distribution was set to "QMLE", the critical values are computed using the empirical distribution of the standardized residuals.
additional arguments to be passed.
if not null, compute predictions for VaR and ES for loss level p_loss (typically, 0.05 or 0.01).

# Details

The predictions are returned as a data frame with columns "meanForecast", "meanError", and "standardDeviation". Row h contains the predictions for horizon h (so, n.ahead rows in total).

If plot = TRUE, the data frame contain also the prediction limits for each horizon in columns lowerInterval and upperInterval.

If p\_loss is not NULL, predictions of Value-at-Risk (VaR) and Expected Shortfall (ES) are returned in columns VaR and ES. The data frame has attribute "p\_loss" containing p\_loss. Typical values for p\_loss are 0.01 and 0.05.

These are somewhat experimental and the arguments and the returned values may change.

### Value

a data frame containing n. ahead rows and 3 to 7 columns, see section 'Details'

### Author(s)

Diethelm Wuertz for the Rmetrics R-port

### See Also

predict in base R
fitted, residuals,
plot, garchFit, class fGARCH,

### Examples

```
## Parameter Estimation of Default GARCH(1,1) Model
set.seed(123)
fit = garchFit(~ garch(1, 1), data = garchSim(), trace = FALSE)
fit
## predict
predict(fit, n.ahead = 10)
predict(fit, n.ahead = 10, mse="uncond")
## predict with plotting: critical values = +/- 2
predict(fit, n.ahead = 10, plot=TRUE, crit_val = 2)
## include also VaR and ES at 5%
predict(fit, n.ahead = 10, plot=TRUE, crit_val = 2, p_loss = 0.05)
## predict with plotting: automatic critical values
## for different conditional distributions
set.seed(321)
fit2 = garchFit(~ garch(1, 1), data = garchSim(), trace=FALSE, cond.dist="sged")
## 95% confidence level
predict(fit2, n.ahead=20, plot=TRUE)
set.seed(444)
fit3 = garchFit(~ garch(1, 1), data = garchSim(), trace=FALSE, cond.dist="QMLE")
## 90% confidence level and nx=100
predict(fit3, n.ahead=20, plot=TRUE, conf=.9, nx=100)
```

residuals-methods Extract GARCH model residuals

### Description

Extracts residuals from a fitted GARCH object.

# Usage

```
## S4 method for signature 'fGARCH'
residuals(object, standardize = FALSE)
```

# Arguments

object	an object of class "fGARCH" as returned by garchFit.
standardize	a logical, indicating if the residuals should be standardized.

### Details

The "fGARCH" method extracts the @residuals slot from an object of class "fGARCH" as returned by the function garchFit and optionally standardizes them, using conditional standard deviations.

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# See Also

fitted, predict, garchFit, class fGARCH,

### Examples

```
stopifnot(require("timeSeries"))
## Swiss Pension fund Index
data(LPP2005REC, package = "timeSeries")
x <- as.timeSeries(LPP2005REC)
## Fit LPP40 Bechmark:
fit <- garchFit(LPP40 ~ garch(1, 1), data = 100*x, trace = FALSE)
fit
fitted <- fitted(fit)
head(fitted)
class(fitted)
res <- residuals(fit)
head(res)
class(res)</pre>
```

### Description

Functions to compute density, distribution function, quantile function and to generate random variates for the skew generalized error distribution.

### Usage

```
dsged(x, mean = 0, sd = 1, nu = 2, xi = 1.5, log = FALSE)
psged(q, mean = 0, sd = 1, nu = 2, xi = 1.5)
qsged(p, mean = 0, sd = 1, nu = 2, xi = 1.5)
rsged(n, mean = 0, sd = 1, nu = 2, xi = 1.5)
```

# Arguments

mean, sd, nu, xi	location parameter mean, scale parameter sd, shape parameter nu, skewness parameter xi.
n	the number of observations.
р	a numeric vector of probabilities.
x, q	a numeric vector of quantiles.
log	a logical; if TRUE, densities are given as log densities.

### Details

The distribution is standardized as discussed in the reference by Wuertz et al below.

### Value

d\* returns the density, p\* returns the distribution function, q\* returns the quantile function, and r\* generates random deviates, all values are numeric vectors.

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# References

Nelson D.B. (1991); Conditional Heteroscedasticity in Asset Returns: A New Approach, Econometrica, 59, 347–370.

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

Wuertz D., Chalabi Y. and Luksan L. (????); *Parameter estimation of ARMA models with GARCH/APARCH errors: An R and SPlus software implementation*, Preprint, 41 pages, https://github.com/GeoBosh/fGarchDoc/blob/master/WurtzEtAlGarch.pdf

#### sged

# sgedFit

# See Also

sgedFit (fit), sgedSlider (visualize),
ged (symmetric GED)

# Examples

```
## sged -
  par(mfrow = c(2, 2))
  set.seed(1953)
  r = rsged(n = 1000)
  plot(r, type = "1", main = "sged", col = "steelblue")
  # Plot empirical density and compare with true density:
  hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
  box()
  x = seq(min(r), max(r), length = 201)
  lines(x, dsged(x), lwd = 2)
  # Plot df and compare with true df:
  plot(sort(r), (1:1000/1000), main = "Probability", col = "steelblue",
    ylab = "Probability")
  lines(x, psged(x), lwd = 2)
  # Compute quantiles:
  round(qsged(psged(q = seq(-1, 5, by = 1))), digits = 6)
```

sgedFit

Skew generalized error distribution parameter estimation

# Description

Function to fit the parameters of the skew generalized error distribution.

# Usage

sgedFit(x, ...)

### Arguments

х	a numeric vector of quantiles.
	parameters parsed to the optimization function nlm.

# Value

sgedFit returns a list with the following components:

par	The best set of parameters found.
objective	The value of objective corresponding to par.

convergence	An integer code. 0 indicates successful convergence.
message	A character string giving any additional information returned by the optimizer, or NULL. For details, see PORT documentation.
iterations	Number of iterations performed.
evaluations	Number of objective function and gradient function evaluations.

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

### References

Nelson D.B. (1991); Conditional Heteroscedasticity in Asset Returns: A New Approach, Econometrica, 59, 347–370.

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

### See Also

sged, sgedSlider

# Examples

```
## rsged -
    set.seed(1953)
    r = rsged(n = 1000)
## sgedFit -
    sgedFit(r)
```

sgedSlider

Skew GED distribution slider

### Description

Displays interactively the dependence of the skew GED distribution on its parameters.

### Usage

sgedSlider(type = c("dist", "rand"))

### Arguments

type

a character string denoting which interactive plot should be displayed. Either a distribution plot type="dist", the default value, or a random variates plot, type="rand". snorm

### Value

a Tcl object

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# References

Nelson D.B. (1991); Conditional Heteroscedasticity in Asset Returns: A New Approach, Econometrica, 59, 347–370.

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

### See Also

sged, sgedFit

### Examples

```
## Not run:
## sgedSlider -
require(tcltk)
sgedSlider("dist")
sgedSlider("rand")
```

## End(Not run)

snorm

Skew normal distribution

### Description

Functions to compute density, distribution function, quantile function and to generate random variates for the skew normal distribution.

The distribution is standardized as discussed in the reference by Wuertz et al below.

# Usage

```
dsnorm(x, mean = 0, sd = 1, xi = 1.5, log = FALSE)
psnorm(q, mean = 0, sd = 1, xi = 1.5)
qsnorm(p, mean = 0, sd = 1, xi = 1.5)
rsnorm(n, mean = 0, sd = 1, xi = 1.5)
```

snorm

### Arguments

x, q	a numeric vector of quantiles.
р	a numeric vector of probabilities.
n	the number of observations.
mean	location parameter.
sd	scale parameter.
xi	skewness parameter.
log	a logical; if TRUE, densities are given as log densities.

# Details

dsnorm computed the density, psnorm the distribution function, qsnorm the quantile function, and rsnorm generates random deviates.

### Value

numeric vector

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

### References

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

Wuertz D., Chalabi Y. and Luksan L. (????); *Parameter estimation of ARMA models with GARCH/APARCH errors: An R and SPlus software implementation*, Preprint, 41 pages, https://github.com/GeoBosh/fGarchDoc/blob/master/WurtzEtAlGarch.pdf

# See Also

snormFit (fit), snormSlider (visualize),

sstd (skew Student-t), sged (skew GED)

# Examples

```
## snorm -
    # Ranbdom Numbers:
    par(mfrow = c(2, 2))
    set.seed(1953)
    r = rsnorm(n = 1000)
    plot(r, type = "l", main = "snorm", col = "steelblue")
    # Plot empirical density and compare with true density:
    hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
    box()
    x = seq(min(r), max(r), length = 201)
```

40

# snormFit

```
lines(x, dsnorm(x), lwd = 2)
# Plot df and compare with true df:
plot(sort(r), (1:1000/1000), main = "Probability", col = "steelblue",
    ylab = "Probability")
lines(x, psnorm(x), lwd = 2)
# Compute quantiles:
round(qsnorm(psnorm(q = seq(-1, 5, by = 1))), digits = 6)
```

snormFit

Skew normal distribution parameter estimation

# Description

Fits the parameters of the skew normal distribution.

# Usage

snormFit(x, ...)

# Arguments

Х	a numeric vector of quantiles.
	parameters passed to the optimization function nlm.

# Value

snormFit returns a list with the following components:

par	The best set of parameters found.
objective	The value of objective corresponding to par.
convergence	An integer code. 0 indicates successful convergence.
message	A character string giving any additional information returned by the optimizer, or NULL. For details, see PORT documentation.
iterations	Number of iterations performed.
evaluations	Number of objective function and gradient function evaluations.

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

### References

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

# snormSlider

### See Also

snormFit (fit), snormSlider (visualize), absMoments

# Examples

```
## rsnorm -
    set.seed(1953)
    r = rsnorm(n = 1000)
## snormFit -
    snormFit(r)
```

snormSlider Skew normal distribution slider

# Description

Displays interactively the dependence of the skew Normal distribution on its parameters.

# Usage

```
snormSlider(type = c("dist", "rand"))
```

### Arguments

type a character string denoting which interactive plot should be displayed. Either a distribution plot type="dist", the default value, or a random variates plot, type="rand".

### Value

a Tcl object

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

### References

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

### See Also

snormFit (fit), snorm,

42

sstd

# Examples

```
## Not run:
## snormSlider -
    require(tcltk)
    snormSlider("dist")
    snormSlider("rand")
```

## End(Not run)

sstd

Skew Student-t distribution

# Description

Functions to compute density, distribution function, quantile function and to generate random variates for the skew Student-t distribution.

### Usage

```
dsstd(x, mean = 0, sd = 1, nu = 5, xi = 1.5, log = FALSE)
psstd(q, mean = 0, sd = 1, nu = 5, xi = 1.5)
qsstd(p, mean = 0, sd = 1, nu = 5, xi = 1.5)
rsstd(n, mean = 0, sd = 1, nu = 5, xi = 1.5)
```

### Arguments

x, q	a numeric vector of quantiles.
р	a numeric vector of probabilities.
n	number of observations to simulate.
mean	location parameter.
sd	scale parameter.
nu	shape parameter (degrees of freedom).
xi	skewness parameter.
log	logical; if TRUE, densities are given as log densities.

# Details

The distribution is standardized as discussed in the reference by Wuertz et al below.

dsstd computes the density, psstd the distribution function, qsstd the quantile function, and rsstd generates random deviates.

### Value

numeric vector

### Author(s)

Diethelm Wuertz for the Rmetrics R-port

### References

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

Wuertz D., Chalabi Y. and Luksan L. (????); *Parameter estimation of ARMA models with GARCH/APARCH errors: An R and SPlus software implementation*, Preprint, 41 pages, https://github.com/GeoBosh/fGarchDoc/blob/master/WurtzEtAlGarch.pdf

# See Also

sstdFit (fit), sstdSlider (visualize)

# Examples

```
## sstd -
  par(mfrow = c(2, 2))
  set.seed(1953)
  r = rsstd(n = 1000)
  plot(r, type = "1", main = "sstd", col = "steelblue")
  # Plot empirical density and compare with true density:
  hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
  box()
  x = seq(min(r), max(r), length = 201)
  lines(x, dsstd(x), lwd = 2)
  # Plot df and compare with true df:
  plot(sort(r), (1:1000/1000), main = "Probability", col = "steelblue",
    ylab = "Probability")
  lines(x, psstd(x), lwd = 2)
  # Compute quantiles:
  round(qsstd(psstd(q = seq(-1, 5, by = 1))), digits = 6)
```

sstdFit

Skew Student-t distribution parameter estimation

### Description

Fits the parameters of the skew Student-t distribution.

### Usage

sstdFit(x, ...)

# sstdFit

# Arguments

x	a numeric vector of quantiles.
	parameters passed to the optimization function nlm.

# Value

sstdFit returns a list with the following components:

par	The best set of parameters found.
objective	The value of objective corresponding to par.
convergence	An integer code. 0 indicates successful convergence.
message	A character string giving any additional information returned by the optimizer, or NULL. For details, see PORT documentation.
iterations	Number of iterations performed.
evaluations	Number of objective function and gradient function evaluations.

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# References

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

# See Also

sstd, stdFit

# Examples

```
## sstd -
    set.seed(1953)
    r = rsstd(n = 1000)
## sstdFit -
    sstdFit(r)
```

sstdSlider

# Description

Displays interactively the dependence of the skew Student-t distribution on its parameters.

# Usage

```
sstdSlider(type = c("dist", "rand"))
```

# Arguments

type

a character string denoting which interactive plot should be displayed. Either a distribution plot type="dist", the default value, or a random variates plot, type="rand".

### Value

a Tcl object

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# References

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

# See Also

sstd, sstdFit

# Examples

```
## Not run:
## sstdSlider -
require(tcltk)
sstdSlider("dist")
sstdSlider("rand")
```

## End(Not run)

stats-tsdiag

### Description

Produce diagnostics for fitted GARCH/APARCH models. The method offers several tests, plots of autocorrelations and partial autocorrelations of the standardised conditional residuals, ability to control which graphs are produced (including interactively), as well as their layout.

### Usage

### Arguments

object	an object from class "fGARCH", as returned by garchFit.
gof.lag	maximal lag for portmanteau tests.
ask	if TRUE present a menu of available plots, see Details.
	not used.
plot	if TRUE all available plots; a vector of positive integers specifies a subset of the available plots.
layout	a list with arguments for graphics::layout for the plots. The default plots the autocorrelations of the standardised conditional residuals and their squares, as well as a QQ-plot for the fitted conditional distribution.

### Details

Compute and graph diagnostics for fitted ARMA-GARCH/APARCH models.

plot can be TRUE to ask for all plots or a vector of positive integers specifying which plots to consider. Currently the following options are available:

- 1 Residuals
- 2 Conditional SDs
- 3 Standardized Residuals
- 4 ACF of Standardized Residuals
- 5 ACF of Squared Standardized Residuals
- 6 Cross Correlation between r^2 and r
- 7 QQ-Plot of Standardized Residuals

The default produces plots of autocorrelations and partial autocorrelations of the standardised conditional residuals, as well as a QQ-plot for the fitted conditional distribution. If plot is TRUE, you probably need also ask = TRUE. If argument plot is of length two the graphics window is split into 2 equal subwindows. Argument layout can still be used to change this. If argument plot is of length one the graphics window is not split at all.

In interactive sessions, if the number of requested graphs (as specified by argument plot) is larger than the number of graphs specified by the layout (by default 3), the function makes the first graph and then presents a menu of the requested plots.

Argument layout can be used to change the layout of the plot, for example to put two graphs per plot, see the examples. Currently it should be a list of arguments for layout, see ?layout. Don't call layout youself, as that will change the graphics device prematurely.

The computed results are returned (invisibly). This is another difference from stats::tsdiag which doesn't return them.

### Value

(experimental, may change) a list with components:

residuals	standardised conditional residuals,
gof	goodness-of-fit tests, pretending parameters are known,
<pre>gof_composite</pre>	goodness-of-fit tests taking into account that the parameters are estimated

Only components that are actually computed are included, the rest are NULL or absent.

### Author(s)

Georgi N. boshnakov

### See Also

fGARCH method for plot,

tsdiag

### Examples

```
set.seed(20230612)
x <- garchSim(n = 200)
fit <- garchFit(formula = ~ garch(1, 1), data = x, trace = FALSE)
fit_test <- tsdiag(fit)
fit_test
## 2x2 matrix with acf of r, r^2 on diag, cor(r,r^2) below it, and qq-plot</pre>
```

```
tsdiag(fit, plot = c(4, 6, 7, 5), layout = list(matrix(1:4, nrow = 2)))
```

48

# Description

Functions to compute density, distribution function, quantile function and to generate random variates for the standardized Student-t distribution.

# Usage

```
dstd(x, mean = 0, sd = 1, nu = 5, log = FALSE)
pstd(q, mean = 0, sd = 1, nu = 5)
qstd(p, mean = 0, sd = 1, nu = 5)
rstd(n, mean = 0, sd = 1, nu = 5)
```

# Arguments

x, q	a numeric vector of quantiles.
р	a numeric vector of probabilities.
n	number of observations to simulate.
mean	location parameter.
sd	scale parameter.
nu	shape parameter (degrees of freedom).
log	logical; if TRUE, densities are given as log densities.

# Details

The standardized Student-t distribution is defined so that for a given sd it has the same variance,  $sd^2$ , for all degrees of freedom. For comparison, the variance of the usual Student-t distribution is nu/(nu-2), where nu is the degrees of freedom. The usual Student-t distribution is obtained by setting sd = sqrt(nu/(nu-2)).

Argument nu must be greater than 2. Although there is a default value for nu, it is rather arbitrary and relying on it is strongly discouraged.

dstd computes the density, pstd the distribution function, qstd the quantile function, and rstd generates random deviates from the standardized-t distribution with the specified parameters.

# Value

numeric vector

### Author(s)

Diethelm Wuertz for the Rmetrics R-port

std

# std

# References

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

Wuertz D., Chalabi Y. and Luksan L. (2006); *Parameter estimation of ARMA models with GARCH/APARCH errors: An R and SPlus software implementation*, Preprint, 41 pages, https://github.com/GeoBosh/fGarchDoc/blob/master/WurtzEtAlGarch.pdf

# See Also

stdFit (fit). stdSlider (visualize),

absMoments

# Examples

## std -

pstd(1, sd = sqrt(5/(5-2)), nu = 5) == pt(1, df = 5) # TRUE

```
par(mfrow = c(2, 2))
set.seed(1953)
r = rstd(n = 1000)
plot(r, type = "1", main = "sstd", col = "steelblue")
# Plot empirical density and compare with true density:
hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
box()
```

```
x = seq(min(r), max(r), length = 201)
```

```
lines(x, dstd(x), lwd = 2)
```

```
# Plot df and compare with true df:
plot(sort(r), (1:1000/1000), main = "Probability", col = "steelblue",
    ylab = "Probability")
lines(x, pstd(x), lwd = 2)
```

```
# Compute quantiles:
round(qstd(pstd(q = seq(-1, 5, by = 1))), digits = 6)
```

std	Fit

```
Student-t distribution parameter estimation
```

### Description

Fits the parameters of the standardized Student-t distribution.

### Usage

stdFit(x, ...)

# stdFit

# Arguments

x	a numeric vector of quantiles.
	parameters parsed to the optimization function nlm.

# Value

stdFit returns a list with the following components:

par	The best set of parameters found.
objective	The value of objective corresponding to par.
convergence	An integer code. 0 indicates successful convergence.
message	A character string giving any additional information returned by the optimizer, or NULL. For details, see PORT documentation.
iterations	Number of iterations performed.
evaluations	Number of objective function and gradient function evaluations.

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# References

Fernandez C., Steel M.F.J. (2000); On Bayesian Modelling of Fat Tails and Skewness, Preprint, 31 pages.

# See Also

std, stdSlider

# Examples

```
## std -
    set.seed(1953)
    r = rstd(n = 1000)
```

## stdFit stdFit(r)

stdSlider

# Description

Displays interactively the dependence of the Student-t distribution on its parameters.

### Usage

```
stdSlider(type = c("dist", "rand"))
```

# Arguments

type

a character string denoting which interactive plot should be displayed. Either a distribution plot type="dist", the default value, or a random variates plot, type="rand".

## Value

a Tcl object

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

### See Also

std, stdFit,

### Examples

```
## Not run:
## stdSlider -
    require(tcltk)
    stdSlider("dist")
    stdSlider("rand")
```

## End(Not run)

summary-methods GA

### GARCH summary methods

### Description

Summary methods for GARCH modelling.

### Methods

Methods for summary defined in package fGarch:

object = "fGARCH" Summary function for objects of class "fGARCH".

### How to read a diagnostic summary report?

The first five sections return the title, the call, the mean and variance formula, the conditional distribution and the type of standard errors:

Title: GARCH Modelling Call: garchFit(~ garch(1, 1), data = garchSim(), trace = FALSE) Mean and Variance Equation: ~arch(0) Conditional Distribution: norm Std. Errors: based on Hessian

The next three sections return the estimated coefficients and an error analysis including standard errors, t values, and probabilities, as well as the log Likelihood values from optimization:

Coeffi	cient(s):				
	mu	omega	alpha1	b	eta1
-5.797	88e-05 7.9	3017e-06 1	.59456e-01	2.30772	e-01
Error Analysis:					
	Estimate	Std. Error	t value Pr	(> t )	
mu	-5.798e-05	2.582e-04	-0.225	0.822	
omega	7.930e-06	5.309e-06	1.494	0.135	
alpha1	1.595e-01	1.026e-01	1.554	0.120	
beta1	2.308e-01	4.203e-01	0.549	0.583	

```
Log Likelihood:
-843.3991 normalized: -Inf
```

The next section provides results on standardized residuals tests, including statistic and p values, and on information criterion statistic including AIC, BIC, SIC, and HQIC:

Standardized Residuals Tests: Statistic p-Value Jarque-Bera Test Chi<sup>2</sup> 0.4172129 0.8117146 R Shapiro-Wilk Test R 0.9957817 0.8566985 W Ljung-Box Test R Q(10) 13.05581 0.2205680 Ljung-Box Test R Q(15) 14.40879 0.4947788 Ljung-Box Test R Q(20) 38.15456 0.008478302 Ljung-Box Test R^2 Q(10) 7.619134 0.6659837 Ljung-Box Test R^2 Q(15) 13.89721 0.5333388 Ljung-Box Test R^2 Q(20) 15.61716 0.7400728 LM Arch Test R TR<sup>2</sup> 7.049963 0.8542942 Information Criterion Statistics: AIC BIC SIC HQIC 8.473991 8.539957 8.473212 8.500687

# Author(s)

Diethelm Wuertz for the Rmetrics R-port

# Examples

```
## garchSim -
    x = garchSim(n = 200)
## garchFit -
    fit = garchFit(formula = x ~ garch(1, 1), data = x, trace = FALSE)
    summary(fit)
```

```
VaR
```

Compute Value-at-Risk (VaR) and expected shortfall (ES)

### Description

Compute Value-at-Risk (VaR) and Expected Shortfall (ES) for a fitted GARCH-APARCH model.

VaR

# Usage

```
## S3 method for class 'fGARCH'
VaR(dist, p_loss = 0.05, ..., tol)
## S3 method for class 'fGARCH'
ES(dist, p_loss = 0.05, ...)
```

# Arguments

dist	an object from class "fGARCH", obtained from garchFit().
p_loss	level, default is 0.05.
	not used.
tol	tollerance

# Details

We provide methods for the generic functions cvar::VaR and cvar::ES.

# Note

We use the traditional definition of VaR as the negated lower quantile. For example, if X are returns on an asset,  $VAR_{\alpha} = -q_{\alpha}$ , where  $q_{\alpha}$  is the lower  $\alpha$  quantile of X. Equivalently,  $VAR_{\alpha}$  is equal to the lower  $1 - \alpha$  quantile of -X (the loss series). For details see the vignette in package **cvar** available at https://cran.r-project.org/package=cvar/vignettes/Guide\_cvar.pdf (or by calling vignette("Guide\_cvar", package = "cvar")).

If you wish to overlay the VaR or ES over returns, just negate the VaR/ES, see the examples.

# See Also

VaR and ES in package cvar

# Examples

```
## simulate a time series of returns
x <- garchSim( garchSpec(), n = 500)
class(x)
## fit a GARCH model
fit <- garchFit(~ garch(1, 1), data = x, trace = FALSE)
head(VaR(fit))
head(ES(fit))
## use plot method for fitted GARCH models
plot(fit, which = 14) # VaR
plot(fit, which = 15) # ES
plot(fit, which = 16) # VaR & ES
## plot(fit) # choose the plot interactively
## time is a second seco
```

```
## overlay VaR and ES over returns
## here x is from class 'timeSeries', so we convert VaR/ES to timeSeries
## don't forget to negate the result of VaR()/ES(),
plot(x)
lines(timeSeries(-VaR(fit)), col = "red")
lines(timeSeries(-ES(fit)), col = "blue")
## alternatively, plot losses (rather than returns) and don't negate VaR()/ES()
plot(-x)
lines(timeSeries(VaR(fit)), col = "red")
lines(timeSeries(ES(fit)), col = "blue")
```

volatility-methods Extract GARCH model volatility

### Description

Extracts volatility from a fitted GARCH object.

### Usage

```
## S3 method for class 'fGARCH'
volatility(object, type = c("sigma", "h"), ...)
```

### Arguments

object	an object of class "fGARCH" as returned by garchFit().
type	a character string denoting if the conditional standard deviations "sigma" or the variances "h" should be returned.
	currently not used.

### Details

volatility is an S3 generic function for computation of volatility, see volatility for the default method.

The method for "fGARCH" objects, described here, extracts the volatility from slot @sigma.t or @h.t of an "fGARCH" object usually obtained from the function garchFit().

The class of the returned value depends on the input to the function garchFit who created the object. The returned value is always of the same class as the input object to the argument data in the function garchFit, i.e. if you fit a "timeSeries" object, you will get back from the function fitted also a "timeSeries" object, if you fit an object of class "zoo", you will get back again a "zoo" object. The same holds for a "numeric" vector, for a "data.frame", and for objects of class "ts", "mts".

In contrast, the slot itself always contains a numeric vector, independently of the class of the input data input, i.e. the function call slot(object, "fitted") will return a numeric vector.

### Methods

Methods for volatility defined in package fGarch:

**object = "fGARCH"** Extractor function for volatility or standard deviation from an object of class "fGARCH".

### Note

(GNB) Contrary to the description of the returned value of the "fGARCH" method, it is always "numeric".

TODO: either implement the documented behaviour or fix the documentation.

### Author(s)

Diethelm Wuertz for the Rmetrics R-port

### See Also

garchFit, class fGARCH

# Examples

```
## Swiss Pension fund Index -
   stopifnot(require("timeSeries")) # need package 'timeSeries'
  x = as.timeSeries(data(LPP2005REC, package = "timeSeries"))
## garchFit
  fit = garchFit(LPP40 ~ garch(1, 1), data = 100*x, trace = FALSE)
  fit
## volatility -
  # Standard Deviation:
  vola = volatility(fit, type = "sigma")
  head(vola)
  class(vola)
  # Variance:
  vola = volatility(fit, type = "h")
  head(vola)
  class(vola)
## slot -
  vola = slot(fit, "sigma.t")
  head(vola)
  class(vola)
  vola = slot(fit, "h.t")
  head(vola)
  class(vola)
```

# Index

\* APARCH model fGARCH-class, 7 fGarch-package, 2 fGARCHSPEC-class, 9 garchFit, 13 garchSim, 21 garchSpec, 24 \* AR-APARCH model fGARCH-class, 7 garchFit, 13 \* AR-GARCH model fGARCH-class, 7 garchFit, 13 \* ARMA-APARCH model fGARCH-class.7 fGARCHSPEC-class, 9 garchFit, 13 garchSpec, 24 \* ARMA-GARCH model fGARCH-class, 7 fGARCHSPEC-class, 9 garchFit, 13 garchSpec, 24 \* **ES** plot-methods, 31 predict-methods, 33 VaR, 54 **\* GARCH diagnostics** plot-methods, 31 \* GARCH goodness=of-fit plot-methods, 31 \* GARCH model fGARCH-class, 7 fGarch-package, 2 fGARCHSPEC-class, 9 garchFit, 13 garchSim, 21 garchSpec, 24 \* GED distribution

ged, 27 \* MA-APARCH model fGARCH-class, 7 garchFit, 13 \* MA-GARCH model fGARCH-class, 7 garchFit, 13 \* SP500 data fGarchData,8 \* Student-t distribution std, 49 \* VaR plot-methods, 31 predict-methods, 33 VaR, 54 \* asymmetric power ARCH model garchSpec, 24 \* classes fUGARCHSPEC-class, 12 \* datasets fGarchData,8 \* diagnostic plots stats-tsdiag, 47 \* diagnostics stats-tsdiag, 47 \* distribution absMoments, 5 ged, 27 gedFit, 29 gedSlider, 30 sged, 36 sgedFit, 37 sgedSlider, 38 snorm, 39 snormFit, 41 snormSlider, 42 sstd, 43 sstdFit,44 sstdSlider, 46

# INDEX

std, 49 stdFit. 50 stdSlider, 52 \* exchange rates data fGarchData, 8 \* expected shortfall plot-methods, 31 predict-methods, 33 VaR, 54 \* fit APARCH model garchFit, 13 \* fit AR-APARCH model garchFit, 13 \* fit AR-GARCH model garchFit, 13 \* fit ARMA-APARCH model garchFit, 13 \* fit ARMA-GARCH model garchFit, 13 \* fit GARCH model garchFit. 13 \* fit MA-APARCH model garchFit, 13 \* fit MA-GARCH model garchFit, 13 \* fit skew distribution fGarch-package, 2 \* htest stats-tsdiag, 47 \* models coef-methods. 6 fitted-methods, 10 formula-methods, 11 garchFit, 13 garchFitControl, 18 garchSim, 21 garchSpec, 24 plot-methods, 31 predict-methods, 33 residuals-methods, 35 volatility-methods, 56 \* package fGarch-package, 2 \* programming fGARCH-class, 7 fGARCHSPEC-class, 9 \* simulate APARCH garchSim, 21

\* simulate GARCH garchSim, 21 \* skew GED distribution sged, 36 \* skew distribution fGarch-package, 2 sged, 36 snorm. 39 snormFit, 41 \* skewed GED distribution sged, 36\* skewed distribution sged, 36 snorm, 39 snormFit, 41 \* skewed normal distribution snorm. 39 \* standardized GED distribution ged, 27 \* standardized Student t distribution std. 49 \* standardized Student t-distribution std. 49 \* standardized skew GED distribution sged, 36 \* t-distribution std, 49 \* ts fGARCH-class, 7 fGarchData, 8 garchSim, 21 garchSpec, 24 predict-methods, 33 stats-tsdiag, 47 \* value-at-risk plot-methods, 31 predict-methods, 33 VaR, 54 \* volatility fGarch-package, 2 .gogarchFit(garchFit), 13 .ugarchFit(fUGARCHSPEC-class), 12 .ugarchSpec (fUGARCHSPEC-class), 12 [dpqr]ged, 4 [dpqr]norm, 4 [dpqr]sged, 4 [dpqr]snorm, 4 [dpqr]sstd, 4

# INDEX

[dpqr]std,4

absMoments, 4, 5, 28, 42, 50

coef, 3, 6
coef (coef-methods), 6
coef, fGARCH-method (coef-methods), 6
coef, fGARCHSPEC-method (coef-methods), 6
coef-methods, 6

dem2gbp (fGarchData), 8 dged (ged), 27 dsged (sged), 36 dsnorm (snorm), 39 dsstd (sstd), 43 dstd (std), 49

ES, *32*, *55* ES (VaR), 54

fBasicsData, 9 fGARCH, 10, 11, 13, 16, 32, 34, 35, 48, 57 fGarch (fGarch-package), 2 fGARCH-class, 7 fGarch-package, 2 fGarchData, 8 fGARCHSPEC, 21, 26 fGARCHSPEC-class, 9 fitted, 3, 32, 34, 35 fitted (fitted-methods), 10 fitted, fGARCH-method (fitted-methods), 10 fitted-methods. 10 formula, 3, 14 formula (formula-methods), 11 formula, fGARCH-method (formula-methods), 11 formula-methods, 11 fUGARCHSPEC-class. 12

logical, 15 pged (ged), 27plot, 10, 32, 34 plot (plot-methods), 31 plot, fGARCH, missing-method (plot-methods), 31 plot-methods, 31 predict, 4, 10, 32, 34, 35 predict (predict-methods), 33 predict,fGARCH-method (predict-methods), 33 predict-methods, 33 psged (sged), 36 psnorm (snorm), 39 psstd (sstd), 43 pstd (std), 49 qged (ged), 27 qsged (sged), 36 qsnorm (snorm), 39 qsstd (sstd), 43 qstd (std), 49 residuals, 3, 10, 32, 34 residuals (residuals-methods), 35 residuals,fGARCH-method (residuals-methods), 35 residuals-methods, 35 rged (ged), 27 rsged (sged), 36 rsnorm (snorm), 39 rsstd (sstd), 43 rstd (std), 49 sged, 28, 36, 38-40 sgedFit, 4, 29, 37, 37, 39 sgedSlider, *37*, *38*, 38 show, fGARCH-method (fGARCH-class), 7 show, fGARCHSPEC-method (fGARCHSPEC-class), 9 snorm, 39, 42 snormFit, 4, 40, 41, 42 snormSlider, 40, 42, 42 sp500dge (fGarchData), 8 sstd, 40, 43, 45, 46 sstdFit, 4, 44, 44, 46 sstdSlider, 44, 46

layout, 48

60

# INDEX

TimeSeriesData,9 tsdiag,48 tsdiag(stats-tsdiag),47

update,fGARCH-method(fGARCH-class),7 update,fGARCHSPEC-method (fGARCHSPEC-class),9

VaR, 32, 54, 55 volatility, 3, 56 volatility (volatility-methods), 56 volatility-methods, 56