# Package 'fitdistrplus'

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**Title** Help to Fit of a Parametric Distribution to Non-Censored or Censored Data

Version 1.2-4

Description Extends the fitdistr() function (of the MASS package) with several functions to help the fit of a parametric distribution to non-censored or censored data.
Censored data may contain left censored, right censored and interval censored values, with several lower and upper bounds. In addition to maximum likelihood estimation (MLE), the package provides moment matching (MME), quantile matching (QME), maximum goodness-of-fit estimation (MGE) and maximum spacing estimation (MSE) methods (available only for non-censored data). Weighted versions of MLE, MME, QME and MSE are available. See e.g. Casella & Berger (2002), Statistical inference, Pacific Grove, for a general introduction

**Depends** R (>= 3.5.0), MASS, grDevices, survival, methods

**Imports** stats, rlang

to parametric estimation.

**Suggests** actuar, rgenoud, mc2d, gamlss.dist, knitr, ggplot2, GeneralizedHyperbolic, rmarkdown, Hmisc, bookdown

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BuildVignettes true

**License** GPL (>= 2)

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https://lbbe.univ-lyon1.fr/fr/fitdistrplus,

https://github.com/lbbe-software/fitdistrplus

BugReports https://github.com/lbbe-software/fitdistrplus/issues

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NeedsCompilation no

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fitdistrplus-package Overview of the fitdistrplus package

### **Description**

The idea of this package emerged in 2008 from a collaboration between J.B. Denis, R. Pouillot and M.L. Delignette who at this time worked in the area of quantitative risk assessment. The implementation of this package was a part of a more general project named "Risk assessment with R" gathering different packages and hosted in R-forge.

The **fitdistrplus** package was first written by M.L. Delignette-Muller and made available in CRAN on 2009 and presented at the 2009 useR conference in Rennes. A few months after, C. Dutang joined the project by starting to participate to the implementation of the **fitdistrplus** package. The package has also been presented at the 2011 useR conference at the 2eme rencontres R in 2013 (https://r2013-lyon.sciencesconf.org/), and the 2019 useR conference. Since 2020, A. Siberchicot helps the development of **fitdistrplus** and maintains the package.

Four vignettes are available within the package:

- a general overview of the package published in the Journal of Statistical Software (doi:10.18637/jss.v064.i04),
- a document answering the most Frequently Asked Questions,
- a document presenting a benchmark of optimization algorithms when finding parameters,
- a document about starting values.

The **fitdistrplus** package is a general package that aims at helping the fit of univariate parametric distributions to censored or non-censored data. The two main functions are fitdist for fit on non-censored data and **fitdistcens** for fit on censored data.

The choice of candidate distributions to fit may be helped using functions descdist and plotdist for non-censored data and plotdistcens for censored data).

Using functions fitdist and fitdistcens, different methods can be used to estimate the distribution parameters:

- maximum likelihood estimation by default (mledist),
- moment matching estimation (mmedist),
- quantile matching estimation (qmedist),
- maximum goodness-of-fit estimation (mgedist).

For classical distributions initial values are automatically calculated if not provided by the user. Graphical functions plotdist and plotdistcens can be used to help a manual calibration of initial values for parameters of non-classical distributions. Function prefit is proposed to help the definition of good starting values in the special case of constrained parameters. In the case where maximum likelihood is chosen as the estimation method, function llplot enables to visualize log-likelihood contours.

The goodness-of-fit of fitted distributions (a single fit or multiple fits) can be explored using different graphical functions (cdfcomp, denscomp, qqcomp and ppcomp for non-censored data and

cdfcompcens for censored data). Goodness-of-fit statistics are also provided for non-censored data using function gofstat.

Bootstrap is proposed to quantify the uncertainty on parameter estimates (functions bootdist and bootdistcens) and also to quantify the uncertainty on CDF or quantiles estimated from the fitted distribution (quantile and CIcdfplot).

### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

bootdist

Bootstrap simulation of uncertainty for non-censored data

### **Description**

Uses parametric or nonparametric bootstrap resampling in order to simulate uncertainty in the parameters of the distribution fitted to non-censored data.

### Usage

### **Arguments**

f	An object of class "fitdist", output of the fitdist function.
bootmethod	A character string coding for the type of resampling: "param" for a parametric resampling and "nonparam" for a nonparametric resampling of data.
niter	The number of samples drawn by bootstrap.
silent	A logical to remove or show warnings and errors when bootstraping.
parallel	The type of parallel operation to be used, "snow" or "multicore" (the second one not being available on Windows), or "no" if no parallel operation.

ncpus	Number of processes to be used in parallel operation : typically one would fix it to the number of available CPUs.
х	An object of class "bootdist" or "density.bootdist".
object	An object of class "bootdist".
main	an overall title for the plot: see $\mbox{\ensuremath{\text{title}}},$ default to "Bootstrapped values of parameters".
enhance	a logical to get an enhanced plot.
trueval	when relevant, a numeric vector with the true value of parameters (for backfitting purposes).
rampcol	colors to interpolate; must be a valid argument to colorRampPalette().
nbgrid	Number of grid points in each direction. Can be scalar or a length-2 integer vector.
nbcol	An integer argument, the required number of colors
• • •	Further arguments to be passed to generic methods or "bootdist" objects for density.
bw, adjust, kernel	
	resp. the smoothing bandwidth, the scaling factor, the kernel used, see density.
mar	A numerical vector of the form c(bottom, left, top, right), see par.
lty, col, lwd	resp. the line type, the color, the line width, see par.

#### **Details**

Samples are drawn by parametric bootstrap (resampling from the distribution fitted by fitdist) or nonparametric bootstrap (resampling with replacement from the data set). On each bootstrap sample the function mledist (or mmedist, qmedist, mgedist according to the component f\$method of the object of class "fitdist") is used to estimate bootstrapped values of parameters. When that function fails to converge, NA values are returned. Medians and 2.5 and 97.5 percentiles are computed by removing NA values. The medians and the 95 percent confidence intervals of parameters (2.5 and 97.5 percentiles) are printed in the summary. If inferior to the whole number of iterations, the number of iterations for which the function converges is also printed in the summary.

By default (when enhance=FALSE), the plot of an object of class "bootdist" consists in a scatterplot or a matrix of scatterplots of the bootstrapped values of parameters. It uses the function stripchart when the fitted distribution is characterized by only one parameter, the function plot when there are two parameters and the function pairs in other cases. In these last cases, it provides a representation of the joint uncertainty distribution of the fitted parameters.

When enhance=TRUE, a personalized plot version of pairs is used where upper graphs are scatter-plots and lower graphs are heatmap image using image based on a kernel based estimator for the 2D density function (using kde2d from MASS package). Arguments rampcol, nbgrid, nbcol can be used to customize the plots. Defautls values are rampcol=c("green", "yellow", "orange", "red"), nbcol=100 (see colorRampPalette()), nbgrid=100 (see kde2d). In addition, when fitting parameters on simulated datasets for backtesting purposes, an additional argument trueval can be used to plot a cross at the true value.

It is possible to accelerate the bootstrap using parallelization. We recommend you to use parallel = "multicore", or parallel = "snow" if you work on Windows, and to fix ncpus to the number of available processors.

density computes the empirical density of bootdist objects using the density function (with Gaussian kernel by default). It returns an object of class density bootdist for which print and plot methods are provided.

#### Value

bootdist returns an object of class "bootdist", a list with 6 components,

estim a data frame containing the bootstrapped values of parameters.

converg a vector containing the codes for convergence obtained if an iterative method

is used to estimate parameters on each bootstraped data set (and 0 if a closed

formula is used).

method A character string coding for the type of resampling: "param" for a parametric

resampling and "nonparam" for a nonparametric resampling.

nbboot The number of samples drawn by bootstrap.

CI bootstrap medians and 95 percent confidence percentile intervals of parameters. fitpart The object of class "fitdist" on which the bootstrap procedure was applied.

#### Generic functions:

print The print of a "bootdist" object shows the bootstrap parameter estimates. If inferior to the whole number of bootstrap iterations, the number of iterations for which the estimation converges is also printed.

summary The summary provides the median and 2.5 and 97.5 percentiles of each parameter. If inferior to the whole number of bootstrap iterations, the number of iterations for which the estimation converges is also printed in the summary.

plot The plot shows the bootstrap estimates with stripchart function for univariate parameters and plot function for multivariate parameters.

density The density computes empirical densities and return an object of class density. bootdist.

#### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

#### References

Cullen AC and Frey HC (1999), *Probabilistic techniques in exposure assessment*. Plenum Press, USA, pp. 181-241.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

### See Also

See fitdistrplus for an overview of the package. fitdist, mledist, qmedist, mmedist, mgedist, quantile.bootdist for another generic function to calculate quantiles from the fitted distribution and its bootstrap results and CIcdfplot for adding confidence intervals on quantiles to a CDF plot of the fitted distribution.

Please visit the Frequently Asked Questions.

### **Examples**

```
# We choose a low number of bootstrap replicates in order to satisfy CRAN running times
# For practical applications, we recommend to use at least niter=501 or niter=1001.
# (1) Fit of a gamma distribution to serving size data
# using default method (maximum likelihood estimation)
# followed by parametric bootstrap
#
data(groundbeef)
x1 <- groundbeef$serving</pre>
f1 <- fitdist(x1, "gamma")</pre>
b1 <- bootdist(f1, niter=51)</pre>
print(b1)
plot(b1)
plot(b1, enhance=TRUE)
summary(b1)
quantile(b1)
CIcdfplot(b1, CI.output = "quantile")
density(b1)
plot(density(b1))
# (2) non parametric bootstrap on the same fit
b1b <- bootdist(f1, bootmethod="nonparam", niter=51)</pre>
summary(b1b)
quantile(b1b)
# (3) Fit of a normal distribution on acute toxicity values of endosulfan in log10 for
# nonarthropod invertebrates, using maximum likelihood estimation
# to estimate what is called a species sensitivity distribution
# (SSD) in ecotoxicology, followed by estimation of the 5 percent quantile value of
# the fitted distribution, what is called the 5 percent hazardous concentration (HC5)
# in ecotoxicology, with its two-sided 95 percent confidence interval calculated by
# parametric bootstrap
data(endosulfan)
ATV <- subset(endosulfan, group == "NonArthroInvert")$ATV
log10ATV <- log10(subset(endosulfan, group == "NonArthroInvert")$ATV)</pre>
fln <- fitdist(log10ATV, "norm")</pre>
bln <- bootdist(fln, bootmethod = "param", niter=51)</pre>
quantile(bln, probs = c(0.05, 0.1, 0.2))
# (4) comparison of sequential and parallel versions of bootstrap
# to be tried with a greater number of iterations (1001 or more)
niter <- 1001
data(groundbeef)
x1 <- groundbeef$serving</pre>
```

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```
f1 <- fitdist(x1, "gamma")

# sequential version
ptm <- proc.time()
summary(bootdist(f1, niter = niter))
proc.time() - ptm

# parallel version using snow
require("parallel")
ptm <- proc.time()
summary(bootdist(f1, niter = niter, parallel = "snow", ncpus = 2))
proc.time() - ptm

# parallel version using multicore (not available on Windows)
ptm <- proc.time()
summary(bootdist(f1, niter = niter, parallel = "multicore", ncpus = 2))
proc.time() - ptm</pre>
```

bootdistcens

Bootstrap simulation of uncertainty for censored data

### Description

Uses nonparametric bootstrap resampling in order to simulate uncertainty in the parameters of the distribution fitted to censored data.

### Usage

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#### **Arguments**

f An object of class "fitdisteens", output of the fitdisteens function.

niter The number of samples drawn by bootstrap.

silent A logical to remove or show warnings and errors when bootstraping.

parallel The type of parallel operation to be used, "snow" or "multicore" (the second

one not being available on Windows), or "no" if no parallel operation.

ncpus Number of processes to be used in parallel operation: typically one would fix it

to the number of available CPUs.

x An object of class "bootdistcens".
object An object of class "bootdistcens".

.. Further arguments to be passed to generic methods or "bootdistcens" objects

for density.

bw, adjust, kernel

resp. the smoothing bandwidth, the scaling factor, the kernel used, see density.

mar A numerical vector of the form c(bottom, left, top, right), see par.

lty, col, lwd resp. the line type, the color, the line width, see par.

#### **Details**

Samples are drawn by nonparametric bootstrap (resampling with replacement from the data set). On each bootstrap sample the function mledist is used to estimate bootstrapped values of parameters. When mledist fails to converge, NA values are returned. Medians and 2.5 and 97.5 percentiles are computed by removing NA values. The medians and the 95 percent confidence intervals of parameters (2.5 and 97.5 percentiles) are printed in the summary. If inferior to the whole number of iterations, the number of iterations for which mledist converges is also printed in the summary.

The plot of an object of class "bootdistcens" consists in a scatterplot or a matrix of scatterplots of the bootstrapped values of parameters. It uses the function stripchart when the fitted distribution is characterized by only one parameter, and the function plot in other cases. In these last cases, it provides a representation of the joint uncertainty distribution of the fitted parameters.

It is possible to accelerate the bootstrap using parallelization. We recommend you to use parallel = "multicore", or parallel = "snow" if you work on Windows, and to fix ncpus to the number of available processors.

density computes the empirical density of bootdistcens objects using the density function (with Gaussian kernel by default). It returns an object of class density. bootdistcens for which print and plot methods are provided.

### Value

bootdistcens returns an object of class "bootdistcens", a list with 6 components,

estim a data frame containing the bootstrapped values of parameters.

converg a vector containing the codes for convergence of the iterative method used to

estimate parameters on each bootstraped data set.

method A character string coding for the type of resampling: in this case "nonparam"

as it is the only available method for censored data.

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nbboot The number of samples drawn by bootstrap.

CI bootstrap medians and 95 percent confidence percentile intervals of parameters.

fitpart The object of class "fitdistcens" on which the bootstrap procedure was ap-

plied.

Generic functions:

print The print of a "bootdistcens" object shows the bootstrap parameter estimates. If inferior to the whole number of bootstrap iterations, the number of iterations for which the estimation converges is also printed.

summary The summary provides the median and 2.5 and 97.5 percentiles of each parameter. If inferior to the whole number of bootstrap iterations, the number of iterations for which the estimation converges is also printed in the summary.

plot The plot shows the bootstrap estimates with the stripchart function for univariate parameters and plot function for multivariate parameters.

density The density computes empirical densities and return an object of class density.bootdistcens.

#### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

#### References

Cullen AC and Frey HC (1999), *Probabilistic techniques in exposure assessment*. Plenum Press, USA, pp. 181-241.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

#### See Also

See fitdistrplus for an overview of the package. fitdistcens, mledist, quantile.bootdistcens for another generic function to calculate quantiles from the fitted distribution and its bootstrap results and CIcdfplot for adding confidence intervals on quantiles to a CDF plot of the fitted distribution.

Please visit the Frequently Asked Questions.

### **Examples**

```
# We choose a low number of bootstrap replicates in order to satisfy CRAN running times
# constraint.
# For practical applications, we recommend to use at least niter=501 or niter=1001.
# (1) Fit of a normal distribution to fluazinam data in log10
# followed by nonparametric bootstrap and calculation of quantiles
# with 95 percent confidence intervals
# data(fluazinam)
(d1 <-log10(fluazinam))
f1 <- fitdistcens(d1, "norm")</pre>
```

```
b1 <- bootdistcens(f1, niter = 51)
summary(b1)
plot(b1)
quantile(b1)
CIcdfplot(b1, CI.output = "quantile")
plot(density(b1))
# (2) Estimation of the mean of the normal distribution
# by maximum likelihood with the standard deviation fixed at 1
# using the argument fix.arg
# followed by nonparametric bootstrap
# and calculation of quantiles with 95 percent confidence intervals
f1b <- fitdistcens(d1, "norm", start = list(mean = 1),fix.arg = list(sd = 1))</pre>
b1b <- bootdistcens(f1b, niter = 51)</pre>
summary(b1b)
plot(b1b)
quantile(b1b)
# (3) comparison of sequential and parallel versions of bootstrap
# to be tried with a greater number of iterations (1001 or more)
niter <- 1001
data(fluazinam)
d1 <-log10(fluazinam)</pre>
f1 <- fitdistcens(d1, "norm")</pre>
# sequential version
ptm <- proc.time()</pre>
summary(bootdistcens(f1, niter = niter))
proc.time() - ptm
# parallel version using snow
require("parallel")
ptm <- proc.time()</pre>
summary(bootdistcens(f1, niter = niter, parallel = "snow", ncpus = 2))
proc.time() - ptm
# parallel version using multicore (not available on Windows)
ptm <- proc.time()</pre>
summary(bootdistcens(f1, niter = niter, parallel = "multicore", ncpus = 2))
proc.time() - ptm
```

CIcdfplot

Empirical cumulative distribution function with pointwise confidence intervals on probabilities or on quantiles

### **Description**

cdfband plots the empirical cumulative distribution function with the bootstraped pointwise confidence intervals on probabilities of on quantiles.

### Usage

```
CIcdfplot(b, CI.output, CI.type = "two.sided", CI.level = 0.95, CI.col = "red", CI.lty = 2, CI.fill = NULL, CI.only = FALSE, xlim, ylim, xlogscale = FALSE, ylogscale = FALSE, main, xlab, ylab, datapch, datacol, fitlty, fitcol, fitlwd, horizontals = TRUE, verticals = FALSE, do.points = TRUE, use.ppoints = TRUE, a.ppoints = 0.5, name.points = NULL, lines01 = FALSE, plotstyle = "graphics", ...)
```

### **Arguments**

b	One "bootdist" object.
CI.output	The quantity on which (bootstraped) bootstraped confidence intervals are computed: either "probability" or "quantile").
CI.type	Type of confidence intervals: either "two.sided" or one-sided intervals ("less" or "greater").
CI.level	The confidence level.
CI.col	the color of the confidence intervals.
CI.lty	the line type of the confidence intervals.
CI.fill	a color to fill the confidence area. Default is NULL corresponding to no filling.
CI.only	A logical whether to plot empirical and fitted distribution functions or only the confidence intervals. Default to FALSE.
xlim	The <i>x</i> -limits of the plot.
ylim	The $y$ -limits of the plot.
xlogscale	If TRUE, uses a logarithmic scale for the x-axis.
ylogscale	If TRUE, uses a logarithmic scale for the y-axis.
main	A main title for the plot, see also title.
xlab	A label for the x-axis, defaults to a description of x.
ylab	A label for the $y$ -axis, defaults to a description of y.
datapch	An integer specifying a symbol to be used in plotting data points, see also points (only for non censored data).
datacol	A specification of the color to be used in plotting data points.
fitcol	A (vector of) color(s) to plot fitted distributions. If there are fewer colors than fits they are recycled in the standard fashion.
fitlty	A (vector of) line type(s) to plot fitted distributions/densities. If there are fewer values than fits they are recycled in the standard fashion. See also par.
fitlwd	A (vector of) line size(s) to plot fitted distributions/densities. If there are fewer values than fits they are recycled in the standard fashion. See also par.
horizontals	If TRUE, draws horizontal lines for the step empirical cdf function (only for non censored data). See also plot.stepfun.

verticals	If TRUE, draws also vertical lines for the empirical cdf function. Only taken into account if horizontals=TRUE (only for non censored data).
do.points	logical; if TRUE, also draw points at the x-locations. Default is TRUE (only for non censored data).
use.ppoints	If TRUE, probability points of the empirical distribution are defined using function ppoints as $(1:n-a.ppoints)/(n-2a.ppoints+1)$ (only for non censored data). If FALSE, probability points are simply defined as $(1:n)/n$ . This argument is ignored for discrete data.
a.ppoints	If use.ppoints=TRUE, this is passed to function ppoints (only for non censored data).
name.points	Label vector for points if they are drawn i.e. if do.points = TRUE (only for non censored data).
lines01	A logical to plot two horizontal lines at h=0 and h=1 for cdfcomp.
plotstyle	"graphics" or "ggplot". If "graphics", the display is built with graphics functions. If "ggplot", a graphic object output is created with ggplot2 functions (the ggplot2 package must be installed).
• • •	Further graphical arguments passed to matlines or polygon, respectively when CI.fill=FALSE and CI.fill=TRUE.

### **Details**

CIcdfplot provides a plot of the empirical distribution using cdfcomp or cdfcompcens, with bootstraped pointwise confidence intervals on probabilities (y values) or on quantiles (x values). Each interval is computed by evaluating the quantity of interest (probability associated to an x value or quantile associated to an y value) using all the bootstraped values of parameters to get a bootstraped sample of the quantity of interest and then by calculating percentiles on this sample to get a confidence interval (classically 2.5 and 97.5 percentiles for a 95 percent confidence level). If CI.fill!= NULL, then the whole confidence area is filled by the color CI.fill thanks to the function polygon, otherwise only borders are drawn thanks to the function matline. Further graphical arguments can be passed to these functions using the three dots arguments . . . .

### Author(s)

Christophe Dutang and Marie-Laure Delignette-Muller.

#### References

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

### See Also

See also cdfcomp, cdfcompcens, bootdist and quantile.

Please visit the Frequently Asked Questions.

#### **Examples**

```
# We choose a low number of bootstrap replicates in order to satisfy CRAN running times
# For practical applications, we recommend to use at least niter=501 or niter=1001.
if (requireNamespace ("ggplot2", quietly = TRUE)) {ggplotEx <- TRUE}</pre>
# (1) Fit of an exponential distribution
set.seed(123)
s1 < -rexp(50, 1)
f1 <- fitdist(s1, "exp")</pre>
b1 <- bootdist(f1, niter= 11) #voluntarily low to decrease computation time
# plot 95 percent bilateral confidence intervals on y values (probabilities)
CIcdfplot(b1, CI.level= 95/100, CI.output = "probability")
if (ggplotEx) CIcdfplot(b1, CI.level= 95/100, CI.output = "probability", plotstyle = "ggplot")
# plot of the previous intervals as a band
CIcdfplot(b1, CI.level= 95/100, CI.output = "probability",
  CI.fill = "pink", CI.col = "red")
if (ggplotEx) CIcdfplot(b1, CI.level= 95/100, CI.output = "probability",
  CI.fill = "pink", CI.col = "red", plotstyle = "ggplot")
# plot of the previous intervals as a band without empirical and fitted dist. functions
CIcdfplot(b1, CI.level= 95/100, CI.output = "probability", CI.only = TRUE,
  CI.fill = "pink", CI.col = "red")
if (ggplotEx) CIcdfplot(b1, CI.level= 95/100, CI.output = "probability", CI.only = TRUE,
  CI.fill = "pink", CI.col = "red", plotstyle = "ggplot")
# same plot without contours
CIcdfplot(b1, CI.level= 95/100, CI.output = "probability", CI.only = TRUE,
  CI.fill = "pink", CI.col = "pink")
if (ggplotEx) CIcdfplot(b1, CI.level= 95/100, CI.output = "probability", CI.only = TRUE,
  CI.fill = "pink", CI.col = "pink", plotstyle = "ggplot")
# plot 95 percent bilateral confidence intervals on x values (quantiles)
CIcdfplot(b1, CI.level= 95/100, CI.output = "quantile")
if (ggplotEx) CIcdfplot(b1, CI.level= 95/100, CI.output = "quantile", plotstyle = "ggplot")
# plot 95 percent unilateral confidence intervals on quantiles
CIcdfplot(b1, CI.level = 95/100, CI.output = "quant", CI.type = "less",
  CI.fill = "grey80", CI.col = "black", CI.lty = 1)
if (ggplotEx) CIcdfplot(b1, CI.level = 95/100, CI.output = "quant", CI.type = "less",
  CI.fill = "grey80", CI.col = "black", CI.lty = 1, plotstyle = "ggplot")
CIcdfplot(b1, CI.level= 95/100, CI.output = "quant", CI.type = "greater",
  CI.fill = "grey80", CI.col = "black", CI.lty = 1)
if (ggplotEx) CIcdfplot(b1, CI.level= 95/100, CI.output = "quant", CI.type = "greater",
```

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```
CI.fill = "grey80", CI.col = "black", CI.lty = 1, plotstyle = "ggplot")
# (2) Fit of a normal distribution on acute toxicity log-transformed values of
# endosulfan for nonarthropod invertebrates, using maximum likelihood estimation
# to estimate what is called a species sensitivity distribution
# (SSD) in ecotoxicology, followed by estimation of the 5, 10 and 20 percent quantile
# values of the fitted distribution, which are called the 5, 10, 20 percent hazardous
# concentrations (HC5, HC10, HC20) in ecotoxicology, with their
# confidence intervals, from a small number of bootstrap
# iterations to satisfy CRAN running times constraint and plot of the band
# representing pointwise confidence intervals on any quantiles (any HCx values)
# For practical applications, we recommend to use at least niter=501 or niter=1001.
data(endosulfan)
log10ATV <- log10(subset(endosulfan, group == "NonArthroInvert")$ATV)</pre>
namesATV <- subset(endosulfan, group == "NonArthroInvert")$taxa</pre>
fln <- fitdist(log10ATV, "norm")</pre>
bln <- bootdist(fln, bootmethod ="param", niter=101)</pre>
quantile(bln, probs = c(0.05, 0.1, 0.2))
CIcdfplot(bln, CI.output = "quantile", CI.fill = "lightblue", CI.col = "blue",
          xlim = c(0,5), name.points=namesATV)
if (ggplotEx) CIcdfplot(bln, CI.output = "quantile", CI.fill = "lightblue", CI.col = "blue",
  xlim = c(0,5), name.points=namesATV, plotstyle = "ggplot")
# (3) Same type of example as example (2) from ecotoxicology
# with censored data
data(salinity)
log10LC50 <-log10(salinity)</pre>
fln <- fitdistcens(log10LC50,"norm")</pre>
bln <- bootdistcens(fln, niter=101)</pre>
(HC5ln <- quantile(bln,probs = 0.05))
CIcdfplot(bln, CI.output = "quantile", CI.fill = "lightblue", CI.col = "blue",
    xlab = "log10(LC50)", xlim=c(0.5,2), lines01 = TRUE)
if (ggplotEx) CIcdfplot(bln, CI.output = "quantile", CI.fill = "lightblue", CI.col = "blue",
                  xlab = "log10(LC50)",xlim=c(0.5,2),lines01 = TRUE, plotstyle = "ggplot")
# zoom around the HC5
CIcdfplot(bln, CI.output = "quantile", CI.fill = "lightblue", CI.col = "blue",
          xlab = "log10(LC50)", lines01 = TRUE, xlim = c(0.8, 1.5), ylim = c(0, 0.1))
abline(h = 0.05, lty = 2) # line corresponding to a CDF of 5 percent
if (ggplotEx) CIcdfplot(bln, CI.output = "quantile", CI.fill = "lightblue", CI.col = "blue",
    xlab = "log10(LC50)", lines01 = TRUE, xlim = c(0.8, 1.5), ylim = c(0, 0.1),
    plotstyle = "ggplot") +
 ggplot2::geom_hline(yintercept = 0.05, lty = 2) # line corresponding to a CDF of 5 percent
```

16 danish

### **Description**

The univariate dataset was collected at Copenhagen Reinsurance and comprise 2167 fire losses over the period 1980 to 1990. They have been adjusted for inflation to reflect 1985 values and are expressed in millions of Danish Krone.

The multivariate data set is the same data as above but the total claim has been divided into a building loss, a loss of contents and a loss of profits.

### Usage

```
data(danishuni)
data(danishmulti)
```

### **Format**

danishuni contains two columns:

Date The day of claim occurence.

Loss The total loss amount in millions of Danish Krone (DKK).

danishmulti contains five columns:

Date The day of claim occurence.

Building The loss amount (mDKK) of the building coverage.

Contents The loss amount (mDKK) of the contents coverage.

Profits The loss amount (mDKK) of the profit coverage.

Total The total loss amount (mDKK).

All columns are numeric except Date columns of class Date.

### Source

Embrechts, P., Kluppelberg, C. and Mikosch, T. (1997) *Modelling Extremal Events for Insurance and Finance*. Berlin: Springer.

### References

Dataset used in McNeil (1996), Estimating the Tails of Loss Severity Distributions using Extreme Value Theory, ASTIN Bull. Davison, A. C. (2003) Statistical Models. Cambridge University Press. Page 278.

### Examples

```
# (1) load of data
#
data(danishuni)
# (2) plot and description of data
#
```

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```
plotdist(danishuni$Loss)

# (3) load of data
#
data(danishmulti)

# (4) plot and description of data
#
idx <- sample(1:NROW(danishmulti), 10)
barplot(danishmulti$Building[idx], col = "grey25",
    ylim = c(0, max(danishmulti$Total[idx])), main = "Some claims of danish data set")
barplot(danishmulti$Content[idx], add = TRUE, col = "grey50", axes = FALSE)
barplot(danishmulti$Profits[idx], add = TRUE, col = "grey75", axes = FALSE)
legend("topleft", legend = c("Building", "Content", "Profits"),
    fill = c("grey25", "grey50", "grey75"))</pre>
```

dataFAQ

Datasets for the FAQ

### **Description**

Datasets used in the FAQ vignette.

### Usage

```
data(dataFAQlog1)
data(dataFAQscale1)
data(dataFAQscale2)
```

### **Format**

dataFAQlog1 dataFAQscale1 dataFAQscale2 are vectors of numeric data.

### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

18 descdist

descdist	Description of an empirical distribution for non-censored data
	1 3 1

### **Description**

Computes descriptive parameters of an empirical distribution for non-censored data and provides a skewness-kurtosis plot.

### Usage

```
descdist(data, discrete = FALSE, boot = NULL, method = "unbiased",
graph = TRUE, print = TRUE, obs.col = "red", obs.pch = 16, boot.col = "orange")
## S3 method for class 'descdist'
print(x, ...)
```

### **Arguments**

data	A numeric vector.
discrete	If TRUE, the distribution is considered as discrete.
boot	If not NULL, boot values of skewness and kurtosis are plotted from bootstrap samples of data. boot must be fixed in this case to an integer above 10.
method	"unbiased" for unbiased estimated values of statistics or "sample" for sample values.
graph	If FALSE, the skewness-kurtosis graph is not plotted.
print	If FALSE, the descriptive parameters computed are not printed.
obs.col	Color used for the observed point on the skewness-kurtosis graph.
obs.pch	plotting character used for the observed point on the skewness-kurtosis graph.
boot.col	Color used for bootstrap sample of points on the skewness-kurtosis graph.
x	An object of class "descdist".
	Further arguments to be passed to generic functions

### **Details**

Minimum, maximum, median, mean, sample sd, and sample (if method=="sample") or by default unbiased estimations of skewness and Pearsons's kurtosis values are printed (Sokal and Rohlf, 1995). A skewness-kurtosis plot such as the one proposed by Cullen and Frey (1999) is given for the empirical distribution. On this plot, values for common distributions are also displayed as a tools to help the choice of distributions to fit to data. For some distributions (normal, uniform, logistic, exponential for example), there is only one possible value for the skewness and the kurtosis (for a normal distribution for example, skewness = 0 and kurtosis = 3), and the distribution is thus represented by a point on the plot. For other distributions, areas of possible values are represented, consisting in lines (gamma and lognormal distributions for example), or larger areas (beta distribution for example). The Weibull distribution is not represented on the graph but it is indicated

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on the legend that shapes close to lognormal and gamma distributions may be obtained with this distribution.

In order to take into account the uncertainty of the estimated values of kurtosis and skewness from data, the data set may be bootstraped by fixing the argument boot to an integer above 10. boot values of skewness and kurtosis corresponding to the boot bootstrap samples are then computed and reported in blue color on the skewness-kurtosis plot.

If discrete is TRUE, the represented distributions are the Poisson, negative binomial distributions, and the normal distribution to which previous discrete distributions may converge. If discrete is FALSE, these are uniform, normal, logistic, lognormal, beta and gamma distributions.

#### Value

descdist returns a list with 7 components,

min the minimum value
max the maximum value
median the median value
mean the mean value

sd the standard deviation sample or estimated value

skewness the skewness sample or estimated value kurtosis the kurtosis sample or estimated value

method the method specified in input ("unbiased" for unbiased estimated values of statis-

tics or "sample" for sample values.

### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

### References

Cullen AC and Frey HC (1999), *Probabilistic techniques in exposure assessment*. Plenum Press, USA, pp. 81-159.

Evans M, Hastings N and Peacock B (2000), *Statistical distributions*. John Wiley and Sons Inc, doi:10.1002/9780470627242.

Sokal RR and Rohlf FJ (1995), Biometry. W.H. Freeman and Company, USA, pp. 111-115.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

### See Also

See plotdist.

Please visit the Frequently Asked Questions.

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### **Examples**

```
# (1) Description of a sample from a normal distribution
# with and without uncertainty on skewness and kurtosis estimated by bootstrap
set.seed(1234)
x1 <- rnorm(100)
descdist(x1)
descdist(x1,boot=11)
# (2) Description of a sample from a beta distribution
# with uncertainty on skewness and kurtosis estimated by bootstrap
# with changing of default colors and plotting character for observed point
descdist(rbeta(100, shape1=0.05, shape2=1), boot=11,
obs.col="blue", obs.pch = 15, boot.col="darkgreen")
# (3) Description of a sample from a gamma distribution
# with uncertainty on skewness and kurtosis estimated by bootstrap
# without plotting
descdist(rgamma(100, shape=2, rate=1), boot=11, graph=FALSE)
# (4) Description of a sample from a Poisson distribution
# with uncertainty on skewness and kurtosis estimated by bootstrap
descdist(rpois(100,lambda=2),discrete=TRUE,boot=11)
# (5) Description of serving size data
# with uncertainty on skewness and kurtosis estimated by bootstrap
data(groundbeef)
serving <- groundbeef$serving</pre>
descdist(serving, boot=11)
```

detectbound

Detect bounds for density function

### **Description**

Manual detection of bounds of parameter of a density function/

### Usage

```
detectbound(distname, vstart, obs, fix.arg=NULL, echo=FALSE)
```

#### **Arguments**

distname

A character string "name" naming a distribution for which the corresponding density function dname must be classically defined.

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vstart	A named vector giving the initial values of parameters of the named distribution.
obs	A numeric vector for non censored data.
fix.arg	An optional named vector giving the values of fixed parameters of the named distribution. Default to NULL.
echo	A logical to show some traces.

### **Details**

This function manually tests the following bounds: -1, 0, and 1.

### Value

detectbound returns a 2-row matrix with the lower bounds in the first row and the upper bounds in the second row.

### Author(s)

Christophe Dutang and Marie-Laure Delignette-Muller.

#### References

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

### See Also

See fitdist.

Please visit the Frequently Asked Questions.

### **Examples**

```
# case where the density returns a Not-an-Numeric value.
detectbound("exp", c(rate=3), 1:10)
detectbound("binom", c(size=3, prob=1/2), 1:10)
detectbound("nbinom", c(size=3, prob=1/2), 1:10)
```

endosulfan

Species Sensitivity Distribution (SSD) for endosulfan

### **Description**

Summary of 48- to 96-hour acute toxicity values (LC50 and EC50 values) for exposure of Australian an Non-Australian taxa to endosulfan.

### Usage

```
data(endosulfan)
```

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#### **Format**

endosulfan is a data frame with 4 columns, named ATV for Acute Toxicity Value (geometric mean of LC50 ou EC50 values in micrograms per liter), Australian (coding for Australian or another origin), group (arthropods, fish or non-arthropod invertebrates) and taxa.

#### Source

Hose, G.C., Van den Brink, P.J. 2004. Confirming the Species-Sensitivity Distribution Concept for Endosulfan Using Laboratory, Mesocosms, and Field Data. *Archives of Environmental Contamination and Toxicology*, **47**, 511-520.

### **Examples**

```
# (1) load of data
data(endosulfan)
# (2) plot and description of data for non Australian fish in decimal logarithm
log10ATV <-log10(subset(endosulfan,(Australian == "no") & (group == "Fish"))$ATV)
plotdist(log10ATV)
descdist(log10ATV,boot=11)
# (3) fit of a normal and a logistic distribution to data in log10
# (classical distributions used for SSD)
# and visual comparison of the fits
fln <- fitdist(log10ATV, "norm")</pre>
summary(fln)
fll <- fitdist(log10ATV, "logis")</pre>
summary(fll)
cdfcomp(list(fln,fll),legendtext=c("normal","logistic"),
xlab="log10ATV")
denscomp(list(fln,fll),legendtext=c("normal","logistic"),
xlab="log10ATV")
qqcomp(list(fln,fll),legendtext=c("normal","logistic"))
ppcomp(list(fln,fll),legendtext=c("normal","logistic"))
gofstat(list(fln,fll), fitnames = c("lognormal", "loglogistic"))
# (4) estimation of the 5 percent quantile value of
# logistic fitted distribution (5 percent hazardous concentration : HC5)
# with its two-sided 95 percent confidence interval calculated by
# parametric bootstrap
# with a small number of iterations to satisfy CRAN running times constraint.
# For practical applications, we recommend to use at least niter=501 or niter=1001.
# in log10(ATV)
```

```
bll <- bootdist(fll,niter=51)</pre>
HC511 <- quantile(bll,probs = 0.05)</pre>
# in ATV
10^(HC5ll$quantiles)
10^(HC5ll$quantCI)
# (5) estimation of the 5 percent quantile value of
# the fitted logistic distribution (5 percent hazardous concentration : HC5)
# with its one-sided 95 percent confidence interval (type "greater")
# calculated by
# nonparametric bootstrap
# with a small number of iterations to satisfy CRAN running times constraint.
# For practical applications, we recommend to use at least niter=501 or niter=1001.
# in log10(ATV)
bllnonpar <- bootdist(fll,niter=51,bootmethod = "nonparam")</pre>
HC5llgreater <- quantile(bllnonpar,probs = 0.05, CI.type="greater")</pre>
# in ATV
10^(HC5llgreater$quantiles)
10^(HC5llgreater$quantCI)
# (6) fit of a logistic distribution
# by minimizing the modified Anderson-Darling AD2L distance
# cf. ?mgedist for definition of this distance
fllAD2L <- fitdist(log10ATV, "logis", method="mge", gof="AD2L")</pre>
summary(fllAD2L)
plot(fllAD2L)
```

fitdist

Fit of univariate distributions to non-censored data

#### **Description**

Fit of univariate distributions to non-censored data by maximum likelihood (mle), moment matching (mme), quantile matching (qme) or maximizing goodness-of-fit estimation (mge). The latter is also known as minimizing distance estimation. Generic methods are print, plot, summary, quantile, logLik, AIC, BIC, vcov and coef.

### Usage

```
fitdist(data, distr, method = c("mle", "mme", "qme", "mge", "mse"),
    start=NULL, fix.arg=NULL, discrete, keepdata = TRUE, keepdata.nb=100,
    calcvcov=TRUE, ...)
## S3 method for class 'fitdist'
print(x, ...)
```

```
## S3 method for class 'fitdist'
plot(x, breaks="default", ...)

## S3 method for class 'fitdist'
summary(object, ...)

## S3 method for class 'fitdist'
logLik(object, ...)

## S3 method for class 'fitdist'
AIC(object, ..., k = 2)

## S3 method for class 'fitdist'
BIC(object, ...)

## S3 method for class 'fitdist'
vcov(object, ...)

## S3 method for class 'fitdist'
vcov(object, ...)

## S3 method for class 'fitdist'
coef(object, ...)
```

#### **Arguments**

data	A numeric vector
data	A numeric vector.

distr A character string "name" naming a distribution for which the corresponding

density function dname, the corresponding distribution function pname and the corresponding quantile function qname must be defined, or directly the density

function.

method A character string coding for the fitting method: "mle" for 'maximum likeli-

hood estimation', "mme" for 'moment matching estimation', "qme" for 'quantile matching estimation', "mge" for 'maximum goodness-of-fit estimation' and

"mse" for 'maximum spacing estimation'.

start A named list giving the initial values of parameters of the named distribution

or a function of data computing initial values and returning a named list. This argument may be omitted (default) for some distributions for which reasonable starting values are computed (see the 'details' section of mledist). It may not

be into account for closed-form formulas.

fix.arg An optional named list giving the values of fixed parameters of the named dis-

tribution or a function of data computing (fixed) parameter values and returning a named list. Parameters with fixed value are thus NOT estimated by this maximum likelihood procedure. The use of this argument is not possible if

method="mme" and a closed-form formula is used.

keepdata a logical. If TRUE, dataset is returned, otherwise only a sample subset is returned.

keepdata.nb When keepdata=FALSE, the length (>1) of the subset returned.

calcvcov A logical indicating if (asymptotic) covariance matrix is required.

discrete If TRUE, the distribution is considered as discrete. If discrete is missing,

discrete is automaticaly set to TRUE when distr belongs to "binom", "nbinom", "geom", "hyper" or "pois" and to FALSE in the other cases. It is thus recommended to enter this argument when using another discrete distribution. This argument will not directly affect the results of the fit but will be passed to func-

tions gofstat, plotdist and cdfcomp.

x An object of class "fitdist".

object An object of class "fitdist".

breaks If "default" the histogram is plotted with the function hist with its default

breaks definition. Else breaks is passed to the function hist. This argument is not taken into account with discrete distributions: "binom", "nbinom", "geom",

"hyper" and "pois".

k penalty per parameter to be passed to the AIC generic function (2 by default).

Further arguments to be passed to generic functions, or to one of the functions "mledist", "mmedist", "qmedist" or "mgedist" depending of the chosen method. See mledist, mmedist, qmedist, mgedist for details on parameter

estimation.

#### **Details**

It is assumed that the distr argument specifies the distribution by the probability density function, the cumulative distribution function and the quantile function (d, p, q).

The four possible fitting methods are described below:

When method="mle" Maximum likelihood estimation consists in maximizing the log-likelihood. A numerical optimization is carried out in mledist via optim to find the best values (see mledist for details).

When method="mme" Moment matching estimation consists in equalizing theoretical and empirical moments. Estimated values of the distribution parameters are computed by a closed-form formula for the following distributions: "norm", "lnorm", "pois", "exp", "gamma", "nbinom", "geom", "beta", "unif" and "logis". Otherwise the theoretical and the empirical moments are matched numerically, by minimization of the sum of squared differences between observed and theoretical moments. In this last case, further arguments are needed in the call to fitdist: order and memp (see mmedist for details).

Since Version 1.2-0, mmedist automatically computes the asymptotic covariance matrix, hence the theoretical moments mdist should be defined up to an order which equals to twice the maximal order given order.

When method = "qme" Quantile matching estimation consists in equalizing theoretical and empirical quantile. A numerical optimization is carried out in qmedist via optim to minimize of the sum of squared differences between observed and theoretical quantiles. The use of this method requires an additional argument probs, defined as the numeric vector of the probabilities for which the quantile(s) is(are) to be matched (see qmedist for details).

When method = "mge" Maximum goodness-of-fit estimation consists in maximizing a goodness-of-fit statistics. A numerical optimization is carried out in mgedist via optim to minimize the goodness-of-fit distance. The use of this method requires an additional argument gof coding for the goodness-of-fit distance chosen. One can use the classical Cramer-von Mises distance

("CvM"), the classical Kolmogorov-Smirnov distance ("KS"), the classical Anderson-Darling distance ("AD") which gives more weight to the tails of the distribution, or one of the variants of this last distance proposed by Luceno (2006) (see mgedist for more details). This method is not suitable for discrete distributions.

When method = "mse" Maximum goodness-of-fit estimation consists in maximizing the average log spacing. A numerical optimization is carried out in msedist via optim.

By default, direct optimization of the log-likelihood (or other criteria depending of the chosen method) is performed using optim, with the "Nelder-Mead" method for distributions characterized by more than one parameter and the "BFGS" method for distributions characterized by only one parameter. The optimization algorithm used in optim can be chosen or another optimization function can be specified using ... argument (see mledist for details). start may be omitted (i.e. NULL) for some classic distributions (see the 'details' section of mledist). Note that when errors are raised by optim, it's a good idea to start by adding traces during the optimization process by adding control=list(trace=1, REPORT=1) in ... argument.

Once the parameter(s) is(are) estimated, fitdist computes the log-likelihood for every estimation method and for maximum likelihood estimation the standard errors of the estimates calculated from the Hessian at the solution found by optim or by the user-supplied function passed to mledist.

By default (keepdata = TRUE), the object returned by fitdist contains the data vector given in input. When dealing with large datasets, we can remove the original dataset from the output by setting keepdata = FALSE. In such a case, only keepdata.nb points (at most) are kept by random subsampling keepdata.nb-2 points from the dataset and adding the minimum and the maximum. If combined with bootdist, and use with non-parametric bootstrap be aware that bootstrap is performed on the subset randomly selected in fitdist. Currently, the graphical comparisons of multiple fits is not available in this framework.

Weighted version of the estimation process is available for method = "mle", "mme", "qme" by using weights=.... See the corresponding man page for details. Weighted maximum GOF estimation (when method = "mge") is not allowed. It is not yet possible to take into account weighths in functions plotdist, plot.fitdist, cdfcomp, denscomp, ppcomp, qqcomp, gofstat and descdist (developments planned in the future).

Once the parameter(s) is(are) estimated, gofstat allows to compute goodness-of-fit statistics.

NB: if your data values are particularly small or large, a scaling may be needed before the optimization process. See example (14) in this man page and examples (14,15) in the test file of the package. Please also take a look at the Rmpfr package available on CRAN for numerical accuracy issues.

#### Value

fitdist returns an object of class "fitdist", a list with the following components:

estimate	the parameter estimates.
method	the character string coding for the fitting method: "mle" for 'maximum likelihood estimation', "mme" for 'matching moment estimation', "qme" for 'matching quantile estimation' "mge" for 'maximum goodness-of-fit estimation' and "mse" for 'maximum spacing estimation'.
sd	the estimated standard errors, NA if numerically not computable or NULL if not available.

cor the estimated correlation matrix, NA if numerically not computable or NULL if

not available.

vcov the estimated variance-covariance matrix, NULL if not available for the estima-

tion method considered.

loglik the log-likelihood.

aic the Akaike information criterion.

bic the the so-called BIC or SBC (Schwarz Bayesian criterion).

n the length of the data set.

data the data set.

distname the name of the distribution.

fix.arg the named list giving the values of parameters of the named distribution that

must be kept fixed rather than estimated by maximum likelihood or NULL if there

are no such parameters.

fix.arg.fun the function used to set the value of fix.arg or NULL.

dots the list of further arguments passed in ... to be used in bootdist in iterative

calls to mledist, mmedist, gmedist, mgedist or NULL if no such arguments.

convergence an integer code for the convergence of optim/constrOptim defined as below

or defined by the user in the user-supplied optimization function. 0 indicates successful convergence. 1 indicates that the iteration limit of optim has been reached. 10 indicates degeneracy of the Nealder-Mead simplex. 100 indicates

that optim encountered an internal error.

discrete the input argument or the automatic definition by the function to be passed to

functions gofstat, plotdist and cdfcomp.

weights the vector of weights used in the estimation process or NULL.

### Generic functions:

print The print of a "fitdist" object shows few traces about the fitting method and the fitted distribution.

summary The summary provides the parameter estimates of the fitted distribution, the log-likelihood, AIC and BIC statistics and when the maximum likelihood is used, the standard errors of the parameter estimates and the correlation matrix between parameter estimates.

plot The plot of an object of class "fitdist" returned by fitdist uses the function plotdist. An object of class "fitdist" or a list of objects of class "fitdist" corresponding to various fits using the same data set may also be plotted using a cdf plot (function cdfcomp), a density plot(function denscomp), a density Q-Q plot (function qqcomp), or a P-P plot (function ppcomp).

logLik Extracts the estimated log-likelihood from the "fitdist" object.

AIC Extracts the AIC from the "fitdist" object.

BIC Extracts the estimated BIC from the "fitdist" object.

vcov Extracts the estimated var-covariance matrix from the "fitdist" object (only available When method = "mle").

coef Extracts the fitted coefficients from the "fitdist" object.

#### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

#### References

I. Ibragimov and R. Has'minskii (1981), *Statistical Estimation - Asymptotic Theory*, Springer-Verlag, doi:10.1007/9781489900272

Cullen AC and Frey HC (1999), *Probabilistic techniques in exposure assessment*. Plenum Press, USA, pp. 81-155.

Venables WN and Ripley BD (2002), *Modern applied statistics with S.* Springer, New York, pp. 435-446, doi:10.1007/9780387217062.

Vose D (2000), *Risk analysis, a quantitative guide*. John Wiley & Sons Ltd, Chischester, England, pp. 99-143.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

#### See Also

See fitdistrplus for an overview of the package. See mledist, mmedist, qmedist, mgedist, msedist for details on parameter estimation. See gofstat for goodness-of-fit statistics. See plotdist, graphcomp, CIcdfplot for graphs (with or without uncertainty and/or multiple fits). See 11plot for (log-)likelihood plots in the neighborhood of the fitted value. See bootdist for bootstrap procedures and fitdistcens for censored-data fitting methods. See optim for base R optimization procedures. See quantile.fitdist, another generic function, which calculates quantiles from the fitted distribution. See quantile for base R quantile computation.

Please visit the Frequently Asked Questions.

### **Examples**

```
# (1) fit of a gamma distribution by maximum likelihood estimation
#

data(groundbeef)
serving <- groundbeef$serving
fitg <- fitdist(serving, "gamma")
summary(fitg)
plot(fitg)
plot(fitg, demp = TRUE)
plot(fitg, histo = FALSE, demp = TRUE)
cdfcomp(fitg, addlegend=FALSE)
denscomp(fitg, addlegend=FALSE)
ppcomp(fitg, addlegend=FALSE)
qqcomp(fitg, addlegend=FALSE)

# (2) use the moment matching estimation (using a closed formula)
#
fitgmme <- fitdist(serving, "gamma", method="mme")</pre>
```

```
summary(fitgmme)
# (3) Comparison of various fits
fitW <- fitdist(serving, "weibull")</pre>
fitg <- fitdist(serving, "gamma")</pre>
fitln <- fitdist(serving, "lnorm")</pre>
summary(fitW)
summary(fitg)
summary(fitln)
cdfcomp(list(fitW, fitg, fitln), legendtext=c("Weibull", "gamma", "lognormal"))
denscomp(list(fitW, fitg, fitln), legendtext=c("Weibull", "gamma", "lognormal"))
qqcomp(list(fitW, fitg, fitln), legendtext=c("Weibull", "gamma", "lognormal"))
ppcomp(list(fitW, fitg, fitln), legendtext=c("Weibull", "gamma", "lognormal"))
gofstat(list(fitW, fitg, fitln), fitnames=c("Weibull", "gamma", "lognormal"))
# (4) defining your own distribution functions, here for the Gumbel distribution
# for other distributions, see the CRAN task view
# dedicated to probability distributions
dgumbel \leftarrow function(x, a, b) 1/b*exp((a-x)/b)*exp(-exp((a-x)/b))
pgumbel <- function(q, a, b) exp(-exp((a-q)/b))
qgumbel <- function(p, a, b) a-b*log(-log(p))</pre>
fitgumbel <- fitdist(serving, "gumbel", start=list(a=10, b=10))</pre>
summary(fitgumbel)
plot(fitgumbel)
# (5) fit discrete distributions (Poisson and negative binomial)
#
data(toxocara)
number <- toxocara$number</pre>
fitp <- fitdist(number, "pois")</pre>
summary(fitp)
plot(fitp)
fitnb <- fitdist(number, "nbinom")</pre>
summary(fitnb)
plot(fitnb)
cdfcomp(list(fitp,fitnb))
gofstat(list(fitp,fitnb))
# (6) how to change the optimisation method?
data(groundbeef)
serving <- groundbeef$serving</pre>
fitdist(serving, "gamma", optim.method="Nelder-Mead")
fitdist(serving, "gamma", optim.method="BFGS")
fitdist(serving, "gamma", optim.method="SANN")
```

```
# (7) custom optimization function
#create the sample
set.seed(1234)
mysample <- rexp(100, 5)</pre>
mystart <- list(rate=8)</pre>
res1 <- fitdist(mysample, dexp, start= mystart, optim.method="Nelder-Mead")</pre>
#show the result
summary(res1)
#the warning tell us to use optimise, because the Nelder-Mead is not adequate.
#to meet the standard 'fn' argument and specific name arguments, we wrap optimize,
myoptimize <- function(fn, par, ...)</pre>
    res <- optimize(f=fn, ..., maximum=FALSE)</pre>
    #assume the optimization function minimize
    standardres <- c(res, convergence=0, value=res$objective,</pre>
        par=res$minimum, hessian=NA)
    return(standardres)
}
#call fitdist with a 'custom' optimization function
res2 <- fitdist(mysample, "exp", start=mystart, custom.optim=myoptimize,</pre>
    interval=c(0, 100))
#show the result
summary(res2)
# (8) custom optimization function - another example with the genetic algorithm
    #set a sample
    fit1 <- fitdist(serving, "gamma")</pre>
    summary(fit1)
    #wrap genoud function rgenoud package
    mygenoud <- function(fn, par, ...)</pre>
    {
        require("rgenoud")
        res <- genoud(fn, starting.values=par, ...)</pre>
        standardres <- c(res, convergence=0)</pre>
        return(standardres)
    }
```

```
#call fitdist with a 'custom' optimization function
    fit2 <- fitdist(serving, "gamma", custom.optim=mygenoud, nvars=2,</pre>
        Domains=cbind(c(0, 0), c(10, 10)), boundary.enforcement=1,
        print.level=1, hessian=TRUE)
    summary(fit2)
# (9) estimation of the standard deviation of a gamma distribution
# by maximum likelihood with the shape fixed at 4 using the argument fix.arg
data(groundbeef)
serving <- groundbeef$serving
f1c <- fitdist(serving, "gamma", start=list(rate=0.1), fix.arg=list(shape=4))</pre>
summary(f1c)
plot(f1c)
# (10) fit of a Weibull distribution to serving size data
# by maximum likelihood estimation
# or by quantile matching estimation (in this example
# matching first and third quartiles)
data(groundbeef)
serving <- groundbeef$serving
fWmle <- fitdist(serving, "weibull")</pre>
summary(fWmle)
plot(fWmle)
gofstat(fWmle)
fWqme <- fitdist(serving, "weibull", method="qme", probs=c(0.25, 0.75))</pre>
summary(fWqme)
plot(fWqme)
gofstat(fWqme)
# (11) Fit of a Pareto distribution by numerical moment matching estimation
#
    require("actuar")
    #simulate a sample
    x4 <- rpareto(1000, 6, 2)
    #empirical raw moment
    memp <- function(x, order) mean(x^order)</pre>
    #fit
    fP \leftarrow fitdist(x4, "pareto", method="mme", order=c(1, 2), memp="memp",
      start=list(shape=10, scale=10), lower=1, upper=Inf)
    summary(fP)
```

```
plot(fP)
# (12) Fit of a Weibull distribution to serving size data by maximum
# goodness-of-fit estimation using all the distances available
data(groundbeef)
serving <- groundbeef$serving</pre>
(f1 <- fitdist(serving, "weibull", method="mge", gof="CvM"))</pre>
(f2 <- fitdist(serving, "weibull", method="mge", gof="KS"))</pre>
(f3 <- fitdist(serving, "weibull", method="mge", gof="AD"))

(f4 <- fitdist(serving, "weibull", method="mge", gof="ADR"))

(f5 <- fitdist(serving, "weibull", method="mge", gof="ADL"))
(f6 <- fitdist(serving, "weibull", method="mge", gof="AD2R"))</pre>
(f7 <- fitdist(serving, "weibull", method="mge", gof="AD2L"))</pre>
(f8 <- fitdist(serving, "weibull", method="mge", gof="AD2"))</pre>
cdfcomp(list(f1, f2, f3, f4, f5, f6, f7, f8))
cdfcomp(list(f1, f2, f3, f4, f5, f6, f7, f8),
  xlogscale=TRUE, xlim=c(8, 250), verticals=TRUE)
denscomp(list(f1, f2, f3, f4, f5, f6, f7, f8))
# (13) Fit of a uniform distribution using maximum likelihood
# (a closed formula is used in this special case where the loglikelihood is not defined),
# or maximum goodness-of-fit with Cramer-von Mises or Kolmogorov-Smirnov distance
set.seed(1234)
u <- runif(50, min=5, max=10)
fumle <- fitdist(u, "unif", method="mle")</pre>
summary(fumle)
plot(fumle)
gofstat(fumle)
fuCvM <- fitdist(u, "unif", method="mge", gof="CvM")</pre>
summary(fuCvM)
plot(fuCvM)
gofstat(fuCvM)
fuKS <- fitdist(u, "unif", method="mge", gof="KS")</pre>
summary(fuKS)
plot(fuKS)
gofstat(fuKS)
# (14) scaling problem
# the simulated dataset (below) has particularly small values, hence without scaling (10^0),
# the optimization raises an error. The for loop shows how scaling by 10^i
# for i=1,...,6 makes the fitting procedure work correctly.
set.seed(1234)
```

```
x2 <- rnorm(100, 1e-4, 2e-4)
for(i in 0:6)
       cat(i, try(fitdist(x2*10^i, "cauchy", method="mle")$estimate, silent=TRUE), "\n")
# (15) Fit of a normal distribution on acute toxicity values of endosulfan in log10 for
# nonarthropod invertebrates, using maximum likelihood estimation
# to estimate what is called a species sensitivity distribution
# (SSD) in ecotoxicology, followed by estimation of the 5 percent quantile value of
# the fitted distribution (which is called the 5 percent hazardous concentration, HC5,
# in ecotoxicology) and estimation of other quantiles.
data(endosulfan)
ATV <- subset(endosulfan, group == "NonArthroInvert")$ATV
log10ATV <- log10(subset(endosulfan, group == "NonArthroInvert")$ATV)</pre>
fln <- fitdist(log10ATV, "norm")</pre>
quantile(fln, probs = 0.05)
quantile(fln, probs = c(0.05, 0.1, 0.2))
# (16) Fit of a triangular distribution using Cramer-von Mises or
# Kolmogorov-Smirnov distance
set.seed(1234)
require("mc2d")
t <- rtriang(100, min=5, mode=6, max=10)
fCvM <- fitdist(t, "triang", method="mge", start = list(min=4, mode=6,max=9), gof="CvM")
fKS <- fitdist(t, "triang", method="mge", start = list(min=4, mode=6,max=9), gof="KS")</pre>
cdfcomp(list(fCvM, fKS))
# (17) fit a non classical discrete distribution (the zero inflated Poisson distribution)
#
require("gamlss.dist")
set.seed(1234)
x < - rZIP(n = 30, mu = 5, sigma = 0.2)
plotdist(x, discrete = TRUE)
fitzip \leftarrow fitdist(x, "ZIP", start = list(mu = 4, sigma = 0.15), discrete = TRUE,
  optim.method = "L-BFGS-B", lower = c(0, 0), upper = c(Inf, 1))
summary(fitzip)
plot(fitzip)
fitp <- fitdist(x, "pois")</pre>
cdfcomp(list(fitzip, fitp))
gofstat(list(fitzip, fitp))
```

# (18) examples with distributions in actuar (predefined starting values)

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fitdistcens

Fitting of univariate distributions to censored data

### **Description**

Fits a univariate distribution to censored data by maximum likelihood.

#### Usage

```
fitdistcens(censdata, distr, start=NULL, fix.arg=NULL,
   keepdata = TRUE, keepdata.nb=100, calcvcov=TRUE, ...)

## S3 method for class 'fitdistcens'
print(x, ...)

## S3 method for class 'fitdistcens'
plot(x, ...)

## S3 method for class 'fitdistcens'
summary(object, ...)

## S3 method for class 'fitdistcens'
logLik(object, ...)

## S3 method for class 'fitdistcens'
AIC(object, ..., k = 2)

## S3 method for class 'fitdistcens'
BIC(object, ...)
```

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```
## $3 method for class 'fitdistcens'
vcov(object, ...)
## $3 method for class 'fitdistcens'
coef(object, ...)
```

#### Arguments

A dataframe of two columns respectively named left and right, describing each observed value as an interval. The left column contains either NA for left censored observations, the left bound of the interval for interval censored

observations, or the observed value for non-censored observations. The right column contains either NA for right censored observations, the right bound of the interval for interval censored observations, or the observed value for non-

censored observations.

distr A character string "name" naming a distribution, for which the corresponding

density function dname and the corresponding distribution function pname must

be defined, or directly the density function.

start A named list giving the initial values of parameters of the named distribution.

This argument may be omitted for some distributions for which reasonable start-

ing values are computed (see the 'details' section of mledist).

fix.arg An optional named list giving the values of parameters of the named distribution

that must be kept fixed rather than estimated by maximum likelihood.

x an object of class "fitdistcens".

object an object of class "fitdistcens".

keepdata a logical. If TRUE, dataset is returned, otherwise only a sample subset is returned.

keepdata.nb When keepdata=FALSE, the length of the subset returned.

calcvcov A logical indicating if (asymptotic) covariance matrix is required.

k penalty per parameter to be passed to the AIC generic function (2 by default).

... further arguments to be passed to generic functions, to the function plotdistcens

in order to control the type of ecdf-plot used for censored data, or to the function

mledist in order to control the optimization method.

#### Details

Maximum likelihood estimations of the distribution parameters are computed using the function mledist. By default direct optimization of the log-likelihood is performed using optim, with the "Nelder-Mead" method for distributions characterized by more than one parameter and the "BFGS" method for distributions characterized by only one parameter. The algorithm used in optim can be chosen or another optimization function can be specified using ... argument (see mledist for details). start may be omitted (i.e. NULL) for some classic distributions (see the 'details' section of mledist). Note that when errors are raised by optim, it's a good idea to start by adding traces during the optimization process by adding control=list(trace=1, REPORT=1) in ... argument.

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The function is not able to fit a uniform distribution. With the parameter estimates, the function returns the log-likelihood and the standard errors of the estimates calculated from the Hessian at the solution found by optim or by the user-supplied function passed to mledist.

By default (keepdata = TRUE), the object returned by fitdist contains the data vector given in input. When dealing with large datasets, we can remove the original dataset from the output by setting keepdata = FALSE. In such a case, only keepdata.nb points (at most) are kept by random subsampling keepdata.nb-4 points from the dataset and adding the component-wise minimum and maximum. If combined with bootdistcens, be aware that bootstrap is performed on the subset randomly selected in fitdistcens. Currently, the graphical comparisons of multiple fits is not available in this framework.

Weighted version of the estimation process is available for method = "mle" by using weights=.... See the corresponding man page for details. It is not yet possible to take into account weighths in functions plotdistcens, plot.fitdistcens and cdfcompcens (developments planned in the future).

Once the parameter(s) is(are) estimated, gofstat allows to compute goodness-of-fit statistics.

#### Value

fitdistcens returns an object of class "fitdistcens", a list with the following components:

estimate the parameter estimates.

method the character string coding for the fitting method : only "mle" for 'maximum

likelihood estimation'.

sd the estimated standard errors.

cor the estimated correlation matrix, NA if numerically not computable or NULL if

not available.

vcov the estimated variance-covariance matrix, NULL if not available.

loglik the log-likelihood.

aic the Akaike information criterion.

bic the the so-called BIC or SBC (Schwarz Bayesian criterion).

censdata the censored data set.
distname the name of the distribution.

fix.arg the named list giving the values of parameters of the named distribution that

must be kept fixed rather than estimated by maximum likelihood or NULL if there

are no such parameters.

fix.arg.fun the function used to set the value of fix.arg or NULL.

dots the list of further arguments passed in ... to be used in bootdistcens to control

the optimization method used in iterative calls to mledist or NULL if no such

arguments.

convergence an integer code for the convergence of optim/constrOptim defined as below

or defined by the user in the user-supplied optimization function. 0 indicates successful convergence. 1 indicates that the iteration limit of optim has been reached. 10 indicates degeneracy of the Nealder-Mead simplex. 100 indicates

that optim encountered an internal error.

discrete always FALSE.

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weights the vector of weights used in the estimation process or NULL.

Generic functions:

print The print of a "fitdist" object shows few traces about the fitting method and the fitted distribution.

summary The summary provides the parameter estimates of the fitted distribution, the log-likelihood, AIC and BIC statistics, the standard errors of the parameter estimates and the correlation matrix between parameter estimates.

plot The plot of an object of class "fitdistcens" returned by fitdistcens uses the function plotdistcens.

logLik Extracts the estimated log-likelihood from the "fitdistcens" object.

AIC Extracts the AIC from the "fitdistcens" object.

BIC Extracts the BIC from the "fitdistcens" object.

vcov Extracts the estimated var-covariance matrix from the "fitdistcens" object (only available When method = "mle").

coef Extracts the fitted coefficients from the "fitdistcens" object.

#### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

## References

Venables WN and Ripley BD (2002), *Modern applied statistics with S.* Springer, New York, pp. 435-446, doi:10.1007/9780387217062.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

### See Also

See Surv2fitdistcens to convert Surv outputs to a data frame appropriate for fitdistcens. See plotdistcens, optim and quantile.fitdistcens for generic functions. See gofstat for goodness-of-fit statistics. See fitdistrplus for an overview of the package.

Please visit the Frequently Asked Questions.

```
# (1) Fit of a lognormal distribution to bacterial contamination data
#
data(smokedfish)
fitsf <- fitdistcens(smokedfish,"lnorm")
summary(fitsf)
# default plot using the Wang technique (see ?plotdiscens for details)
plot(fitsf)
# plot using the Turnbull algorithm (see ?plotdiscens for details)
# with confidence intervals for the empirical distribution
plot(fitsf, NPMLE = TRUE, NPMLE.method = "Turnbull", Turnbull.confint = TRUE)</pre>
```

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```
# basic plot using intervals and points (see ?plotdiscens for details)
plot(fitsf, NPMLE = FALSE)
# plot of the same fit using the Turnbull algorithm in logscale
cdfcompcens(fitsf,main="bacterial contamination fits",
   xlab="bacterial concentration (CFU/g)",ylab="F",
    addlegend = FALSE, lines01 = TRUE, xlogscale = TRUE, xlim = c(1e-2, 1e2))
# zoom on large values of F
cdfcompcens(fitsf,main="bacterial contamination fits",
    xlab="bacterial concentration (CFU/g)",ylab="F",
    addlegend = FALSE,lines01 = TRUE, xlogscale = TRUE,
   xlim = c(1e-2, 1e2), ylim=c(0.4, 1))
# (2) Fit of a normal distribution on acute toxicity values
# of fluazinam (in decimal logarithm) for
# macroinvertebrates and zooplancton, using maximum likelihood estimation
# to estimate what is called a species sensitivity distribution
# (SSD) in ecotoxicology
data(fluazinam)
log10EC50 <-log10(fluazinam)</pre>
fln <- fitdistcens(log10EC50,"norm")</pre>
summary(fln)
plot(fln)
# (3) defining your own distribution functions, here for the Gumbel distribution
# for other distributions, see the CRAN task view dedicated to
# probability distributions
dgumbel <- function(x,a,b) 1/b*exp((a-x)/b)*exp(-exp((a-x)/b))
pgumbel <- function(q,a,b) exp(-exp((a-q)/b))
qgumbel <- function(p,a,b) a-b*log(-log(p))</pre>
fg <- fitdistcens(log10EC50, "gumbel", start=list(a=1,b=1))</pre>
summary(fg)
plot(fg)
# (4) comparison of fits of various distributions
fll <- fitdistcens(log10EC50,"logis")</pre>
summary(fll)
cdfcompcens(list(fln,fll,fg),legendtext=c("normal","logistic","gumbel"),
xlab = "log10(EC50)")
# (5) how to change the optimisation method?
fitdistcens(log10EC50, "logis", optim.method="Nelder-Mead")
fitdistcens(log10EC50,"logis",optim.method="BFGS")
fitdistcens(log10EC50, "logis", optim.method="SANN")
```

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```
# (6) custom optimisation function - example with the genetic algorithm
    #wrap genoud function rgenoud package
    mygenoud <- function(fn, par, ...)</pre>
        require("rgenoud")
        res <- genoud(fn, starting.values=par, ...)</pre>
        standardres <- c(res, convergence=0)</pre>
        return(standardres)
    }
    # call fitdistcens with a 'custom' optimization function
    fit.with.genoud <- fitdistcens(log10EC50,"logis", custom.optim=mygenoud, nvars=2,</pre>
        Domains=cbind(c(0,0), c(5, 5)), boundary.enforcement=1,
        print.level=1, hessian=TRUE)
    summary(fit.with.genoud)
# (7) estimation of the mean of a normal distribution
# by maximum likelihood with the standard deviation fixed at 1 using the argument fix.arg
flnb <- fitdistcens(log10EC50, "norm", start = list(mean = 1),fix.arg = list(sd = 1))</pre>
# (8) Fit of a lognormal distribution on acute toxicity values of fluazinam for
# macroinvertebrates and zooplancton, using maximum likelihood estimation
# to estimate what is called a species sensitivity distribution
# (SSD) in ecotoxicology, followed by estimation of the 5 percent quantile value of
# the fitted distribution (which is called the 5 percent hazardous concentration, HC5,
# in ecotoxicology) and estimation of other quantiles.
data(fluazinam)
log10EC50 <-log10(fluazinam)</pre>
fln <- fitdistcens(log10EC50,"norm")</pre>
quantile(fln, probs = 0.05)
quantile(fln, probs = c(0.05, 0.1, 0.2))
# (9) Fit of a lognormal distribution on 72-hour acute salinity tolerance (LC50 values)
# of riverine macro-invertebrates using maximum likelihood estimation
data(salinity)
log10LC50 <-log10(salinity)</pre>
fln <- fitdistcens(log10LC50,"norm")</pre>
plot(fln)
```

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fluazinam

Species-Sensitivity Distribution (SSD) for Fluazinam

# Description

48-hour acute toxicity values (EC50 values) for exposure of macroinvertebrates and zooplancton to fluazinam.

# Usage

```
data(fluazinam)
```

## **Format**

fluazinam is a data frame with 2 columns named left and right, describing each observed EC50 value (in micrograms per liter) as an interval. The left column contains either NA for left censored observations, the left bound of the interval for interval censored observations, or the observed value for non-censored observations. The right column contains either NA for right censored observations, the right bound of the interval for interval censored observations, or the observed value for noncensored observations.

#### Source

Hose, G.C., Van den Brink, P.J. 2004. The species sensitivity distribution approach compared to a microcosm study: A case study with the fungicide fluazinam. *Ecotoxicology and Environmental Safety*, **73**, 109-122.

```
# (1) load of data
#
data(fluazinam)

# (2) plot of data using Turnbull cdf plot
#
log10EC50 <- log10(fluazinam)
plotdistcens(log10EC50)

# (3) fit of a lognormal and a logistic distribution to data
# (classical distributions used for species sensitivity
# distributions, SSD, in ecotoxicology)
# and visual comparison of the fits using Turnbull cdf plot
#
fln <- fitdistcens(log10EC50, "norm")
summary(fln)

fll <- fitdistcens(log10EC50, "logis")
summary(fl1)</pre>
```

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```
cdfcompcens(list(fln,fll), legendtext = c("normal", "logistic"),
  xlab = "log10(EC50)")
# (4) estimation of the 5 percent quantile value of
# the normal fitted distribution (5 percent hazardous concentration : HC5)
# with its two-sided 95 percent confidence interval calculated by
# non parametric bootstrap
# with a small number of iterations to satisfy CRAN running times constraint.
# For practical applications, we recommend to use at least niter=501 or niter=1001.
# in log10(EC50)
bln <- bootdistcens(fln, niter = 101)</pre>
HC5ln <- quantile(bln, probs = 0.05)</pre>
10^(HC5ln$quantiles)
10^(HC5ln$quantCI)
# (5) estimation of the HC5 value
# with its one-sided 95 percent confidence interval (type "greater")
# in log10(EC50)
HC5lnb <- quantile(bln, probs = 0.05, CI.type = "greater")</pre>
# in LC50
10^(HC5lnb$quantiles)
10^(HC5lnb$quantCI)
```

fremale

Fictive survival dataset of a french Male population

# Description

100 male individuals randomly taken from frefictivetable in CASdatasets package

# Usage

```
data(fremale)
```

## Format

fremale is a data frame with 3 columns names AgeIn, AgeOut respectively for entry age and exit age; Death a binary dummy: 1 indicating the death of the individual; 0 a censored observation.

### References

See full dataset frefictivetable of CASdatasets at http://dutangc.perso.math.cnrs.fr/RRepository/

## **Examples**

```
# (1) load of data
#
data(fremale)
summary(fremale)
```

gofstat

Goodness-of-fit statistics

# Description

Computes goodness-of-fit statistics for parametric distributions fitted to a same censored or noncensored data set.

## Usage

```
gofstat(f, chisqbreaks, meancount, discrete, fitnames=NULL)
## S3 method for class 'gofstat.fitdist'
print(x, ...)
## S3 method for class 'gofstat.fitdistcens'
print(x, ...)
```

# **Arguments**

f

An object of class "fitdist" (or "fitdistcens"), output of the function fitdist() (resp. "fitdist()"), or a list of "fitdist" objects, or a list of "fitdistcens" objects.

chisqbreaks

Only usable for non censored data, a numeric vector defining the breaks of the cells used to compute the chi-squared statistic. If omitted, these breaks are automatically computed from the data in order to reach roughly the same number of observations per cell, roughly equal to the argument meancount, or sligthly more if there are some ties.

meancount

Only usable for non censored data, the mean number of observations per cell expected for the definition of the breaks of the cells used to compute the chi-squared statistic. This argument will not be taken into account if the breaks are directly defined in the argument chisqbreaks. If chisqbreaks and meancount are both omitted, meancount is fixed in order to obtain roughly  $(4n)^{2/5}$  cells with n the length of the dataset.

discrete

If TRUE, only the Chi-squared statistic and information criteria are computed. If missing, discrete is passed from the first object of class "fitdist" of the list f. For censored data this argument is ignored, as censored data are considered continuous.

fitnames

A vector defining the names of the fits.

Χ

An object of class "gofstat.fitdist" or "gofstat.fitdistcens".

. . .

Further arguments to be passed to generic functions.

#### **Details**

For any type of data (censored or not), information criteria are calculated. For non censored data, added Goodness-of-fit statistics are computed as described below.

The Chi-squared statistic is computed using cells defined by the argument chisqbreaks or cells automatically defined from data, in order to reach roughly the same number of observations per cell, roughly equal to the argument meancount, or sligthly more if there are some ties. The choice to define cells from the empirical distribution (data), and not from the theoretical distribution, was done to enable the comparison of Chi-squared values obtained with different distributions fitted on a same data set. If chisqbreaks and meancount are both omitted, meancount is fixed in order to obtain roughly  $(4n)^{2/5}$  cells, with n the length of the data set (Vose, 2000). The Chi-squared statistic is not computed if the program fails to define enough cells due to a too small dataset. When the Chi-squared statistic is computed, and if the degree of freedom (nb of cells - nb of parameters - 1) of the corresponding distribution is strictly positive, the p-value of the Chi-squared test is returned.

For continuous distributions, Kolmogorov-Smirnov, Cramer-von Mises and Anderson-Darling and statistics are also computed, as defined by Stephens (1986).

An approximate Kolmogorov-Smirnov test is performed by assuming the distribution parameters known. The critical value defined by Stephens (1986) for a completely specified distribution is used to reject or not the distribution at the significance level 0.05. Because of this approximation, the result of the test (decision of rejection of the distribution or not) is returned only for data sets with more than 30 observations. Note that this approximate test may be too conservative.

For data sets with more than 5 observations and for distributions for which the test is described by Stephens (1986) for maximum likelihood estimations ("exp", "cauchy", "gamma" and "weibull"), the Cramer-von Mises and Anderson-darling tests are performed as described by Stephens (1986). Those tests take into account the fact that the parameters are not known but estimated from the data by maximum likelihood. The result is the decision to reject or not the distribution at the significance level 0.05. Those tests are available only for maximum likelihood estimations.

Only recommended statistics are automatically printed, i.e. Cramer-von Mises, Anderson-Darling and Kolmogorov statistics for continuous distributions and Chi-squared statistics for discrete ones ("binom", "nbinom", "geom", "hyper" and "pois").

Results of the tests are not printed but stored in the output of the function.

#### Value

gofstat() returns an object of class "gofstat.fitdist" or "gofstat.fitdistcens" with following components or a sublist of them (only aic, bic and nbfit for censored data),

chisq	a named vector with the Chi-squared statistics or NULL if not computed
chisqbreaks	common breaks used to define cells in the Chi-squared statistic
chisqpvalue	a named vector with the p-values of the Chi-squared statistic or NULL if not computed
chisqdf	a named vector with the degrees of freedom of the Chi-squared distribution or $NULL$ if not computed
chisqtable	a table with observed and theoretical counts used for the Chi-squared calculations
CVM	a named vector of the Cramer-von Mises statistics or "not computed" if not computed

cvmtest	a named vector of the decisions of the Cramer-von Mises test or "not computed" if not computed
ad	a named vector with the Anderson-Darling statistics or "not computed" if not computed
adtest	a named vector with the decisions of the Anderson-Darling test or "not computed" if not computed
ks	a named vector with the Kolmogorov-Smirnov statistic or "not computed" if not computed
kstest	a named vector with the decisions of the Kolmogorov-Smirnov test or "not computed" if not computed
aic	a named vector with the values of the Akaike's Information Criterion.
bic	a named vector with the values of the Bayesian Information Criterion.
discrete	the input argument or the automatic definition by the function from the first object of class "fitdist" of the list in input.
nbfit	Number of fits in argument.

## Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

## References

Cullen AC and Frey HC (1999), *Probabilistic techniques in exposure assessment*. Plenum Press, USA, pp. 81-155.

Stephens MA (1986), *Tests based on edf statistics*. In Goodness-of-fit techniques (D'Agostino RB and Stephens MA, eds), Marcel Dekker, New York, pp. 97-194.

Venables WN and Ripley BD (2002), *Modern applied statistics with S.* Springer, New York, pp. 435-446, doi:10.1007/9780387217062.

Vose D (2000), *Risk analysis, a quantitative guide*. John Wiley & Sons Ltd, Chischester, England, pp. 99-143.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

## See Also

See fitdist.

Please visit the Frequently Asked Questions.

```
# (1) fit of two distributions to the serving size data
# by maximum likelihood estimation
# and comparison of goodness-of-fit statistics
#
data(groundbeef)
```

```
serving <- groundbeef$serving</pre>
(fitg <- fitdist(serving, "gamma"))</pre>
gofstat(fitg)
(fitln <- fitdist(serving, "lnorm"))</pre>
gofstat(fitln)
gofstat(list(fitg, fitln))
# (2) fit of two discrete distributions to toxocara data
# and comparison of goodness-of-fit statistics
data(toxocara)
number <- toxocara$number</pre>
fitp <- fitdist(number, "pois")</pre>
summary(fitp)
plot(fitp)
fitnb <- fitdist(number, "nbinom")</pre>
summary(fitnb)
plot(fitnb)
gofstat(list(fitp, fitnb),fitnames = c("Poisson","negbin"))
# (3) Get Chi-squared results in addition to
      recommended statistics for continuous distributions
set.seed(1234)
x4 <- rweibull(n=1000, shape=2, scale=1)</pre>
# fit of the good distribution
f4 <- fitdist(x4,"weibull")</pre>
plot(f4)
# fit of a bad distribution
f4b <- fitdist(x4,"cauchy")
plot(f4b)
(g <- gofstat(list(f4,f4b),fitnames=c("Weibull", "Cauchy")))</pre>
g$chisq
g$chisqdf
g$chisqpvalue
g$chisqtable
# and by defining the breaks
(g <- gofstat(list(f4,f4b),</pre>
 chisqbreaks = seq(from = min(x4), to = max(x4), length.out = 10), fitnames = c("Weibull", "Cauchy"))) \\
g$chisq
g$chisqdf
g$chisqpvalue
g$chisqtable
```

```
# (4) fit of two distributions on acute toxicity values
# of fluazinam (in decimal logarithm) for
# macroinvertebrates and zooplancton
# and comparison of goodness-of-fit statistics
#

data(fluazinam)
log10EC50 <-log10(fluazinam)
(fln <- fitdistcens(log10EC50, "norm"))
plot(fln)
gofstat(fln)
(fll <- fitdistcens(log10EC50, "logis"))
plot(fll)
gofstat(fll)
gofstat(fll)</pre>
```

graphcomp

Graphical comparison of multiple fitted distributions (for non-censored data)

## **Description**

cdfcomp plots the empirical cumulative distribution against fitted distribution functions, denscomp plots the histogram against fitted density functions, qqcomp plots theoretical quantiles against empirical ones, ppcomp plots theoretical probabilities against empirical ones. Only cdfcomp is able to plot fits of a discrete distribution.

## Usage

```
cdfcomp(ft, xlim, ylim, xlogscale = FALSE, ylogscale = FALSE, main, xlab, ylab,
    datapch, datacol, fitlty, fitcol, fitlwd, addlegend = TRUE, legendtext,
    xlegend = "bottomright", ylegend = NULL, horizontals = TRUE, verticals = FALSE,
    do.points = TRUE, use.ppoints = TRUE, a.ppoints = 0.5, name.points = NULL,
    lines01 = FALSE, discrete, add = FALSE, plotstyle = "graphics",
    fitnbpts = 101, ...)

denscomp(ft, xlim, ylim, probability = TRUE, main, xlab, ylab, datacol, fitlty,
    fitcol, fitlwd, addlegend = TRUE, legendtext, xlegend = "topright", ylegend = NULL,
    demp = FALSE, dempcol = "black", plotstyle = "graphics",
    discrete, fitnbpts = 101, fittype="l", ...)

qqcomp(ft, xlim, ylim, xlogscale = FALSE, ylogscale = FALSE, main, xlab, ylab,
    fitpch, fitcol, fitlwd, addlegend = TRUE, legendtext, xlegend = "bottomright",
    ylegend = NULL, use.ppoints = TRUE, a.ppoints = 0.5, line01 = TRUE,
```

```
line01col = "black", line01lty = 1, ynoise = TRUE, plotstyle = "graphics", ...)
ppcomp(ft, xlim, ylim, xlogscale = FALSE, ylogscale = FALSE, main, xlab, ylab,
   fitpch, fitcol, fitlwd, addlegend = TRUE, legendtext, xlegend = "bottomright",
   ylegend = NULL, use.ppoints = TRUE, a.ppoints = 0.5, line01 = TRUE,
   lineO1col = "black", lineO1lty = 1, ynoise = TRUE, plotstyle = "graphics", ...)
```

# **Arguments**

•	3	
	ft	One "fitdist" object or a list of objects of class "fitdist".
	xlim	The x-limits of the plot.
	ylim	The $y$ -limits of the plot.
	xlogscale	If TRUE, uses a logarithmic scale for the $x$ -axis.
	ylogscale	If TRUE, uses a logarithmic scale for the $y$ -axis.
	main	A main title for the plot. See also title.
	xlab	A label for the x-axis, defaults to a description of x.
	ylab	A label for the $y$ -axis, defaults to a description of y.
	datapch	An integer specifying a symbol to be used in plotting data points. See also par.
	datacol	A specification of the color to be used in plotting data points. See also par.
	fitcol	A (vector of) color(s) to plot fitted distributions. If there are fewer colors than fits they are recycled in the standard fashion. See also par.
	fitlty	A (vector of) line type(s) to plot fitted distributions/densities. If there are fewer values than fits they are recycled in the standard fashion. See also par.
	fitlwd	A (vector of) line size(s) to plot fitted distributions/densities. If there are fewer values than fits they are recycled in the standard fashion. See also par.
	fitpch	A (vector of) line type(s) to plot fitted quantiles/probabilities. If there are fewer values than fits they are recycled in the standard fashion. See also par.
	fittype	The type of plot for fitted probabilities in the case of discrete distributions: possible types are "p" for points, "1" for lines and "o" for both overplotted (as in plot.default). fittype is not used for non-discrete distributions.
	fitnbpts	A numeric for the number of points to compute fitted probabilities or cumulative probabilities. Default to 101.
	addlegend	If TRUE, a legend is added to the plot.
	legendtext	A character or expression vector of length $\geq 1$ to appear in the legend. See also legend.
	xlegend, ylegend	
		The mand a coordinates to be used to position the legand. They can be spec-

The x and y coordinates to be used to position the legend. They can be specified by keyword. If plotstyle = "graphics", see xy.coords and legend. If plotstyle = "ggplot", the xlegend keyword must be one of top, bottom, left, or right. See also guide\_legend in ggplot2

If TRUE, draws horizontal lines for the step empirical cumulative distribution horizontals

function (ecdf). See also plot.stepfun.

verticals If TRUE, draws vertical lines for the empirical cumulative distribution function (ecdf). Only taken into account if horizontals=TRUE. If TRUE (by default), draws points at the x-locations. For large dataset (n > 1e4), do.points do. points is ignored and no point is drawn. use.ppoints If TRUE, probability points of the empirical distribution are defined using function ppoints as (1:n - a.ppoints)/(n - 2a.ppoints + 1). If FALSE, probability points are simply defined as (1:n)/n. This argument is ignored for discrete data. a.ppoints If use.ppoints=TRUE, this is passed to the ppoints function. Label vector for points if they are drawn i.e. if do.points = TRUE (only for non name.points censored data). lines01 A logical to plot two horizontal lines at h=0 and h=1 for cdfcomp. line01 A logical to plot an horizontal line y = x for qqcomp and ppcomp. line01col, line01lty Color and line type for line01. See also par. demp A logical to add the empirical density on the plot, using the density function. dempcol A color for the empirical density in case it is added on the plot (demp=TRUE). ynoise A logical to add a small noise when plotting empirical quantiles/probabilities for qqcomp and ppcomp. A logical to use the probability scale for denscomp. See also hist. probability discrete If TRUE, the distributions are considered discrete. When missing, discrete is set to TRUE if at least one object of the list ft is discrete. add If TRUE, adds to an already existing plot. If FALSE, starts a new plot. This parameter is not available when plotstyle = "ggplot". "graphics" or "ggplot". If "graphics", the display is built with graphics plotstyle functions. If "ggplot", a graphic object output is created with ggplot2 functions (the ggplot2 package must be installed).

. . .

Further graphical arguments passed to graphical functions used in cdfcomp, denscomp, ppcomp and qqcomp when plotstyle = "graphics". When plotstyle = "ggplot", these arguments are only used by the histogram plot (hist) in the denscomp function. When plotstyle = "ggplot", the graphical output can be customized with relevant ggplot2 functions after you store your output.

## **Details**

cdfcomp provides a plot of the empirical distribution and each fitted distribution in cdf, by default using the Hazen's rule for the empirical distribution, with probability points defined as (1:n-0.5)/n. If discrete is TRUE, probability points are always defined as (1:n)/n. For large dataset (n > 1e4), no point is drawn but the line for ecdf is drawn instead. Note that when horizontals, verticals and do.points are FALSE, no empirical point is drawn, only the fitted cdf is shown.

denscomp provides a density plot of each fitted distribution with the histogram of the data for conyinuous data. When discrete=TRUE, distributions are considered as discrete, no histogram is plotted but demp is forced to TRUE and fitted and empirical probabilities are plotted either with vertical lines fittype="1", with single points fittype="p" or both lines and points fittype="o".

ppcomp provides a plot of the probabilities of each fitted distribution (x-axis) against the empirical probabilities (y-axis) by default defined as (1:n-0.5)/n (data are assumed continuous). For large dataset (n > 1e4), lines are drawn instead of pointss and customized with the fitpch parameter.

qqcomp provides a plot of the quantiles of each theoretical distribution (x-axis) against the empirical quantiles of the data (y-axis), by default defining probability points as (1:n-0.5)/n for theoretical quantile calculation (data are assumed continuous). For large dataset (n > 1e4), lines are drawn instead of points and customized with the fitpch parameter.

By default a legend is added to these plots. Many graphical arguments are optional, dedicated to personalize the plots, and fixed to default values if omitted.

## Value

\*comp returns a list of drawn points and/or lines when plotstyle == "graphics" or an object of class "ggplot" when plotstyle == "ggplot".

#### Author(s)

Christophe Dutang, Marie-Laure Delignette-Muller and Aurelie Siberchicot.

#### References

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

## See Also

See plot, legend, ppoints, plot.stepfun for classic plotting functions. See CIcdfplot and plotdist for other plot functions of fitdistrplus.

Please visit the Frequently Asked Questions.

```
# (1) Plot various distributions fitted to serving size data
data(groundbeef)
serving <- groundbeef$serving</pre>
fitW <- fitdist(serving, "weibull")</pre>
fitln <- fitdist(serving, "lnorm")</pre>
fitg <- fitdist(serving, "gamma")</pre>
cdfcomp(list(fitW, fitln, fitg), horizontals = FALSE)
cdfcomp(list(fitW, fitln, fitg), horizontals = TRUE)
cdfcomp(list(fitW, fitln, fitg), horizontals = TRUE, verticals = TRUE, datacol = "purple")
cdfcomp(list(fitW, fitln, fitg), legendtext = c("Weibull", "lognormal", "gamma"),
  main = "ground beef fits", xlab = "serving sizes (g)",
  ylab = "F", xlim = c(0, 250), xlegend = "center", lines01 = TRUE)
denscomp(list(fitW, fitln, fitg), legendtext = c("Weibull", "lognormal", "gamma"),
 main = "ground beef fits", xlab = "serving sizes (g)", xlim = c(0, 250), xlegend = "topright")
ppcomp(list(fitW, fitln, fitg), legendtext = c("Weibull", "lognormal", "gamma"),
  main = "ground beef fits", xlegend = "bottomright", line01 = TRUE)
```

```
qqcomp(list(fitW, fitln, fitg), legendtext = c("Weibull", "lognormal", "gamma"),
 main = "ground beef fits", xlegend = "bottomright", line01 = TRUE,
 xlim = c(0, 300), ylim = c(0, 300), fitpch = 16)
# (2) Plot lognormal distributions fitted by
# maximum goodness-of-fit estimation
# using various distances (data plotted in log scale)
data(endosulfan)
ATV <- subset(endosulfan, group == "NonArthroInvert")$ATV
taxaATV <- subset(endosulfan, group == "NonArthroInvert")$taxa</pre>
flnMGEKS <- fitdist(ATV, "lnorm", method = "mge", gof = "KS")
flnMGEAD <- fitdist(ATV, "lnorm", method = "mge", gof = "AD")</pre>
flnMGEADL <- fitdist(ATV, "lnorm", method = "mge", gof = "ADL")</pre>
flnMGEAD2L <- fitdist(ATV, "lnorm", method = "mge", gof = "AD2L")</pre>
cdfcomp(list(flnMGEKS, flnMGEAD, flnMGEADL, flnMGEAD2L),
 xlogscale = TRUE, main = "fits of a lognormal dist. using various GOF dist.",
 legendtext = c("MGE KS", "MGE AD", "MGE ADL", "MGE AD2L"),
 verticals = TRUE, xlim = c(1, 100000), name.points=taxaATV)
qqcomp(list(flnMGEKS, flnMGEAD, flnMGEADL, flnMGEAD2L),
 main = "fits of a lognormal dist. using various GOF dist.",
 legendtext = c("MGE KS", "MGE AD", "MGE ADL", "MGE AD2L"),
 xlogscale = TRUE, ylogscale = TRUE)
ppcomp(list(flnMGEKS, flnMGEAD, flnMGEADL, flnMGEAD2L),
 main = "fits of a lognormal dist. using various GOF dist.",
 legendtext = c("MGE KS", "MGE AD", "MGE ADL", "MGE AD2L"))
# (3) Plot normal and logistic distributions fitted by
# maximum likelihood estimation
# using various plotting positions in cdf plots
data(endosulfan)
log10ATV <-log10(subset(endosulfan, group == "NonArthroInvert")$ATV)</pre>
fln <- fitdist(log10ATV, "norm")</pre>
fll <- fitdist(log10ATV, "logis")</pre>
# default plot using Hazen plotting position: (1:n - 0.5)/n
cdfcomp(list(fln, fll), legendtext = c("normal", "logistic"), xlab = "log10ATV")
# plot using mean plotting position (named also Gumbel plotting position)
\# (1:n)/(n + 1)
cdfcomp(list(fln, fll),legendtext = c("normal", "logistic"), xlab = "log10ATV",
 use.ppoints = TRUE, a.ppoints = 0)
# plot using basic plotting position: (1:n)/n
cdfcomp(list(fln, fll),legendtext = c("normal", "logistic"), xlab = "log10ATV",
 use.ppoints = FALSE)
```

# (4) Comparison of fits of two distributions fitted to discrete data

```
data(toxocara)
number <- toxocara$number</pre>
fitp <- fitdist(number, "pois")</pre>
fitnb <- fitdist(number, "nbinom")</pre>
cdfcomp(list(fitp, fitnb), legendtext = c("Poisson", "negative binomial"))
denscomp(list(fitp, fitnb),demp = TRUE, legendtext = c("Poisson", "negative binomial"))
denscomp(list(fitp, fithb),demp = TRUE, fittype = "1", dempcol = "black",
 legendtext = c("Poisson", "negative binomial"))
denscomp(list(fitp, fitnb),demp = TRUE, fittype = "p", dempcol = "black",
 legendtext = c("Poisson", "negative binomial"))
denscomp(list(fitp, fitnb),demp = TRUE, fittype = "o", dempcol = "black",
 legendtext = c("Poisson", "negative binomial"))
# (5) Customizing of graphical output and use of ggplot2
#
data(groundbeef)
serving <- groundbeef$serving</pre>
fitW <- fitdist(serving, "weibull")</pre>
fitln <- fitdist(serving, "lnorm")</pre>
fitg <- fitdist(serving, "gamma")</pre>
if (requireNamespace ("ggplot2", quietly = TRUE)) {
 denscomp(list(fitW, fitln, fitg), plotstyle = "ggplot")
 cdfcomp(list(fitW, fitln, fitg), plotstyle = "ggplot")
 qqcomp(list(fitW, fitln, fitg), plotstyle = "ggplot")
 ppcomp(list(fitW, fitln, fitg), plotstyle = "ggplot")
}
# customizing graphical output with graphics
denscomp(list(fitW, fitln, fitg), legendtext = c("Weibull", "lognormal", "gamma"),
 main = "ground beef fits", xlab = "serving sizes (g)", xlim = c(0, 250),
 xlegend = "topright", addlegend = FALSE)
# customizing graphical output with ggplot2
if (requireNamespace ("ggplot2", quietly = TRUE)) {
 dcomp <- denscomp(list(fitW, fitln, fitg), legendtext = c("Weibull", "lognormal", "gamma"),</pre>
    xlab = "serving sizes (g)", xlim = c(0, 250),
    xlegend = "topright", plotstyle = "ggplot", breaks = 20, addlegend = FALSE)
 dcomp + ggplot2::theme_minimal() + ggplot2::ggtitle("Ground beef fits")
```

graphcompcens

Graphical comparison of multiple fitted distributions for censored data

# **Description**

cdfcompcens plots the empirical cumulative distribution against fitted distribution functions, qqcompcens

plots theoretical quantiles against empirical ones, ppcompcens plots theoretical probabilities against empirical ones.

## Usage

```
cdfcompcens(ft, xlim, ylim, xlogscale = FALSE, ylogscale = FALSE, main, xlab, ylab,
    datacol, fillrect, fitlty, fitcol, fitlwd, addlegend = TRUE, legendtext,
    xlegend = "bottomright", ylegend = NULL, lines01 = FALSE,
    Turnbull.confint = FALSE,
    NPMLE.method = "Wang",
    add = FALSE, plotstyle = "graphics", ...)

qqcompcens(ft, xlim, ylim, xlogscale = FALSE, ylogscale = FALSE, main, xlab, ylab,
    fillrect, fitcol, fitlwd, addlegend = TRUE, legendtext, xlegend = "bottomright",
    ylegend = NULL, line01 = TRUE, line01col = "black", line01lty = 1,
    ynoise = TRUE, NPMLE.method = "Wang", plotstyle = "graphics", ...)

ppcompcens(ft, xlim, ylim, xlogscale = FALSE, ylogscale = FALSE, main, xlab, ylab,
    fillrect, fitcol, fitlwd, addlegend = TRUE, legendtext, xlegend = "bottomright",
    ylegend = NULL, line01 = TRUE, line01col = "black", line01lty = 1,
    ynoise = TRUE, NPMLE.method = "Wang", plotstyle = "graphics", ...)
```

### **Arguments**

ft	One "fitdistcens" object or a list of objects of class "fitdistcens".
xlim	The $x$ -limits of the plot.
ylim	The <i>y</i> -limits of the plot.
xlogscale	If TRUE, uses a logarithmic scale for the x-axis.
ylogscale	If TRUE, uses a logarithmic scale for the $y$ -axis.
main	A main title for the plot, see also title.
xlab	A label for the $x$ -axis, defaults to a description of $x$ .
ylab	A label for the $y$ -axis, defaults to a description of y.
datacol	A specification of the color to be used in plotting data points.
fillrect	A specification of the color to be used for filling rectanges of non uniqueness of the empirical cumulative distribution (only used if NPMLE.method is equal to "Wang" in cdfcompcens). Fix it to NA if you do not want to fill the rectangles.
fitcol	A (vector of) color(s) to plot fitted distributions. If there are fewer colors than fits they are recycled in the standard fashion.
fitlty	A (vector of) line type(s) to plot fitted distributions. If there are fewer values than fits they are recycled in the standard fashion. See also par.
fitlwd	A (vector of) line size(s) to plot fitted distributions. If there are fewer values than fits they are recycled in the standard fashion. See also par.
addlegend	If TRUE, a legend is added to the plot.
legendtext	A character or expression vector of length $\geq 1$ to appear in the legend, see also legend.

xlegend, ylegend

The x and y coordinates to be used to position the legend. They can be specified by keyword. If plotstyle = "graphics", see xy.coords and legend. If plotstyle = "ggplot", the xlegend keyword must be one of top, bottom, left, or right. See also guide\_legend in ggplot2

lines01

A logical to plot two horizontal lines at h=0 and h=1 for cdfcompcens.

Turnbull.confint

if TRUE confidence intervals will be added to the Turnbull plot. In that case NPMLE.method is forced to "Turnbull"

NPMLE.method

Three NPMLE techniques are provided, "Wang", the default one, rewritten from the package npsurv using function constrOptim from the package stats for optimisation, "Turnbull.middlepoints", an older one which is implemented in the package survival and "Turnbull.intervals" that uses the same Turnbull algorithm from the package survival but associates an interval to each equivalence class instead of the middlepoint of this interval (see details). Only "Wang" and "Turnbull.intervals" enable the derivation of a Q-Q plot and a P-P plot.

add

If TRUE, adds to an already existing plot. If FALSE, starts a new plot. This parameter is not available when plotstyle = "ggplot".

line01

A logical to plot an horizontal line y = x for qqcompcens and ppcompcens.

line01col, line01lty

Color and line type for line01. See also par.

ynoise

A logical to add a small noise when plotting empirical quantiles/probabilities for qqcompcens and ppcompcens. ynoise is only used when various fits are plotted with the "graphics" plotstyle. Facets are used instead with the "ggplot" plotstyle.

plotstyle

"graphics" or "ggplot". If "graphics", the display is built with graphics functions. If "ggplot", a graphic object output is created with ggplot2 functions (the ggplot2 package must be installed). In "cdfcompcens", "ggplot" graphics are only available with "Wang" NPMLE technique.

. . .

Further graphical arguments passed to graphical functions used in cdfcompcens, ppcompcens and qqcompcens.

## **Details**

See details of plotdistcens for a detailed description of provided goddness-of-fit plots.

## Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

## References

Turnbull BW (1974), Nonparametric estimation of a survivorship function with doubly censored data. Journal of American Statistical Association, 69, 169-173.

Wang Y (2008), Dimension-reduced nonparametric maximum likelihood computation for intervalcensored data. Computational Statistics & Data Analysis, 52, 2388-2402.

Wang Y and Taylor SM (2013), Efficient computation of nonparametric survival functions via a hierarchical mixture formulation. Statistics and Computing, 23, 713-725.

Delignette-Muller ML and Dutang C (2015), *fitdistribus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34.

#### See Also

See plotdistcens, survfit. formula, legend and par.

Please visit the Frequently Asked Questions.

```
# (1) Plot various distributions fitted to bacterial contamination data
data(smokedfish)
Clog10 <- log10(smokedfish)</pre>
fitsfn <- fitdistcens(Clog10, "norm")</pre>
summary(fitsfn)
fitsfl <- fitdistcens(Clog10, "logis")</pre>
summary(fitsfl)
dgumbel <- function(x,a,b) 1/b*exp((a-x)/b)*exp(-exp((a-x)/b))
pgumbel <- function(q,a,b) exp(-exp((a-q)/b))
qgumbel \leftarrow function(p,a,b) a-b*log(-log(p))
fitsfg<-fitdistcens(Clog10, "gumbel", start=list(a=-3,b=3))</pre>
summary(fitsfg)
# CDF plot
cdfcompcens(list(fitsfn,fitsfl,fitsfg))
cdfcompcens(list(fitsfn,fitsfl,fitsfg),datacol="orange",fillrect = NA,
  legendtext=c("normal","logistic","Gumbel"),
  main="bacterial contamination fits",
  xlab="bacterial concentration (CFU/g)",ylab="F",
  xlegend = "bottom",lines01 = TRUE)
# alternative Turnbull plot for the empirical cumulative distribution
# (default plot of the previous versions of the package)
cdfcompcens(list(fitsfn,fitsfl,fitsfg), NPMLE.method = "Turnbull.middlepoints")
# customizing graphical output with ggplot2
if (requireNamespace ("ggplot2", quietly = TRUE)) {
  cdfcompcens <- cdfcompcens(list(fitsfn,fitsfl,fitsfg),datacol="orange",fillrect = NA,</pre>
    legendtext=c("normal","logistic","Gumbel"),
    xlab="bacterial concentration (CFU/g)",ylab="F",
    xlegend = "bottom",lines01 = TRUE, plotstyle = "ggplot")
 cdfcompcens + ggplot2::theme_minimal() + ggplot2::ggtitle("Bacterial contamination fits")
}
# PP plot
ppcompcens(list(fitsfn,fitsfl,fitsfg))
ppcompcens(list(fitsfn,fitsfl,fitsfg), ynoise = FALSE)
```

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```
par(mfrow = c(2,2))
ppcompcens(fitsfn)
ppcompcens(fitsfl)
ppcompcens(fitsfg)
par(mfrow = c(1,1))
if (requireNamespace ("ggplot2", quietly = TRUE)) {
 ppcompcens(list(fitsfn,fitsfl,fitsfg), plotstyle = "ggplot")
 ppcompcens(list(fitsfn,fitsfl,fitsfg), plotstyle = "ggplot",
    fillrect = c("lightpink", "lightblue", "lightgreen"),
    fitcol = c("red", "blue", "green"))
}
# QQ plot
qqcompcens(list(fitsfn,fitsfl,fitsfg))
qqcompcens(list(fitsfn,fitsfl,fitsfg), ynoise = FALSE)
par(mfrow = c(2,2))
qqcompcens(fitsfn)
qqcompcens(fitsfl)
qqcompcens(fitsfg)
par(mfrow = c(1,1))
if (requireNamespace ("ggplot2", quietly = TRUE)) {
 qqcompcens(list(fitsfn,fitsfl,fitsfg), ynoise = FALSE, plotstyle = "ggplot")
 qqcompcens(list(fitsfn,fitsfl,fitsfg), ynoise = FALSE, plotstyle = "ggplot",
    fillrect = c("lightpink", "lightblue", "lightgreen"),
    fitcol = c("red", "blue", "green"))
}
```

groundbeef

Ground beef serving size data set

# **Description**

Serving sizes collected in a French survey, for ground beef patties consumed by children under 5 years old.

## Usage

```
data(groundbeef)
```

#### **Format**

groundbeef is a data frame with 1 column (serving: serving sizes in grams)

## **Source**

Delignette-Muller, M.L., Cornu, M. 2008. Quantitative risk assessment for *Escherichia coli* O157:H7 in frozen ground beef patties consumed by young children in French households. *International Journal of Food Microbiology*, **128**, 158-164.

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## **Examples**

```
# (1) load of data
#
data(groundbeef)

# (2) description and plot of data
#
serving <- groundbeef$serving
descdist(serving)
plotdist(serving)

# (3) fit of a Weibull distribution to data
#
fitW <- fitdist(serving, "weibull")
summary(fitW)
plot(fitW)
gofstat(fitW)</pre>
```

logLikplot

(Log)likelihood plot for a fit using maximum likelihood

# Description

11plot plots the (log)likelihood around the estimation for distributions fitted by maximum likelihood.

# Usage

# Arguments

mlefit	An object of class "fitdist" of "fitdistcens" obtained by maximum likelihood (with method = "mle")
loglik	a logical to plot log-likelihood or likelihood function.
expansion	a expansion factor to enlarge the default range of values explored for each parameter.
lseq	length of sequences of parameters.
back.col	logical (for llsurface only). Contours are plotted with a background gradient of colors if TRUE.
nlev	number of contour levels to plot.
pal.col	Palette of colors. Colors to be used as back (for llsurface only).
fit.show	a logical to plot the mle estimate.
fit.pch	the type of point used to plot the mle estimate.
	Further graphical arguments passed to graphical functions.

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#### **Details**

llplot plots the (log)likelihood surface(s) (or curve if there there is only one estimated parameter) around the maximum likelihood estimation. It internally calls function llsurface and llcurve. When there is more than two estimated parameters, the (log)likehood surface is plotted for each combination of two parameters, fixing the other ones to their estimated value. For each (log)likelihood surface, when back.col image (2D-plot) is used and when nlev > 0 contour (2D-plot) is used to add nlev contours. By default the range of values explored for each estimated parameter is of 2 standard error around the mle estimate but this range can be expanded (or contracted) using the argument expansion.

# Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

#### References

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

#### See Also

See llsurface and llcurve for manual (log)likelihood plots (surface ou curve) and plot, contour, image for classic plotting functions.

Please visit the Frequently Asked Questions.

```
# (1) a distribution with one parameter
#

x <- rexp(50)
fite <- fitdist(x, "exp")
llplot(fite)
llplot(fite, col = "red", fit.show = TRUE)
llplot(fite, col = "red", fit.show = TRUE, loglik = FALSE)

# (2) a distribution with two parameters
#

data(groundbeef)
serving <- groundbeef$serving
fitg <- fitdist(serving, "gamma")
llplot(fitg)

llplot(fitg, expansion = 2)
llplot(fitg, pal.col = heat.colors(100), fit.show = TRUE)
llplot(fitg, back.col = FALSE, nlev = 25, fit.show = TRUE)</pre>
```

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```
# (3) a distribution with two parameters with one fixed
fitg2 <- fitdist(serving, "gamma", fix.arg = list(rate = 0.5))</pre>
llplot(fitg2, fit.show = TRUE)
# (4) a distribution with three parameters
 data(endosulfan)
 ATV <-endosulfan$ATV
 require("actuar")
 fBurr <- fitdist(ATV, "burr", start = list(shape1 = 0.3, shape2 = 1, rate = 1))</pre>
 llplot(fBurr)
 llplot(fBurr, back.col = FALSE, fit.show = TRUE, fit.pch = 16)
 llplot(fBurr, nlev = 0, pal.col = rainbow(100), lseq = 100)
# (5) a distribution with two parameters fitted on censored data
data(salinity)
fsal <- fitdistcens(salinity, "lnorm")</pre>
llplot(fsal, fit.show = TRUE)
llplot(fsal, fit.show = TRUE, loglik = FALSE)
```

logLiksurface

(Log)likelihood surfaces or (log)likelihood curves

## **Description**

llsurface plots the likelihood surface for distributions with two or more parameters, llcurve plots the likelihood curve for distributions with one or more parameters.

## Usage

```
llsurface(data, distr, plot.arg, min.arg, max.arg, lseq = 50, fix.arg = NULL,
    loglik = TRUE, back.col = TRUE, nlev = 10, pal.col = terrain.colors(100),
    weights = NULL, ...)

llcurve(data, distr, plot.arg, min.arg, max.arg, lseq = 50, fix.arg = NULL,
    loglik = TRUE, weights = NULL, ...)
```

## **Arguments**

data

A numeric vector for non censored data or a dataframe of two columns respectively named left and right, describing each observed value as an interval for

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	censored data. In that case the left column contains either NA for left censored observations, the left bound of the interval for interval censored observations, or the observed value for non-censored observations. The right column contains either NA for right censored observations, the right bound of the interval for interval censored observations, or the observed value for non-censored observations.
distr	A character string "name" naming a distribution for which the corresponding density function dname and the corresponding distribution function pname must be classically defined.
plot.arg	a two-element vector with the names of the two parameters that will vary for llsurface, only one element for llcurve.
min.arg	a two-element vector with lower plotting bounds for llsurface, only one element for llcurve.
max.arg	a two-element vector with upper plotting bounds for llsurface, only one element for llcurve.
lseq	length of sequences of parameters.
fix.arg	a named list with fixed value of other parameters.
loglik	a logical to plot log-likelihood or likelihood function.
back.col	logical (for llsurface only). Contours are plotted with a background gradient of colors if TRUE.
nlev	number of contour levels to plot (for llsurface only).
pal.col	Palette of colors. Colors to be used as back (for llsurface only).
weights	an optional vector of weights to be used in the fitting process. Should be NULL or a numeric vector with strictly positive values (classically the number of occurences of each observation).

# **Details**

. . .

These two function are not intended to be called directly but is internally called in llplot.

llsurface plots the likelihood surface for distributions with two varying parameters and other parameters fixed. When back.col, image (2D-plot) is used. When nlev > 0, contour (2D-plot) is used to add nlev contours.

Further graphical arguments passed to graphical functions.

11curve plots the likelihood curve for distributions with one varying parameter and other parameters fixed.

# Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

# References

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

## See Also

See llplot for an automatic (log)likelihood plots (surface ou curve) of an object of class "fitdist" or "fitdistcens" and plot, contour, image for classic plotting functions.

Please visit the Frequently Asked Questions.

```
# (1) loglikelihood or likelihood curve
#
n <- 100
set.seed(1234)
x \leftarrow rexp(n)
llcurve(data = x, distr = "exp", plot.arg = "rate", min.arg = 0, max.arg = 4)
llcurve(data = x, distr = "exp", plot.arg = "rate", min.arg = 0, max.arg = 4,
loglik = FALSE)
llcurve(data = x, distr = "exp", plot.arg = "rate", min.arg = 0, max.arg = 4,
  main = "log-likelihood for exponential distribution", col = "red")
abline(v = 1, lty = 2)
# (2) loglikelihood surface
x \leftarrow rnorm(n, 0, 1)
llsurface(data =x, distr="norm", plot.arg=c("mean", "sd"),
          min.arg=c(-1, 0.5), max.arg=c(1, 3/2), back.col = FALSE,
          main="log-likelihood for normal distribution")
llsurface(data =x, distr="norm", plot.arg=c("mean", "sd"),
          min.arg=c(-1, 0.5), max.arg=c(1, 3/2),
          main="log-likelihood for normal distribution",
          nlev = 20, pal.col = heat.colors(100),)
points(0, 1, pch="+", col="red")
llsurface(data =x, distr="norm", plot.arg=c("mean", "sd"),
          min.arg=c(-1, 0.5), max.arg=c(1, 3/2),
          main="log-likelihood for normal distribution",
          nlev = 0, back.col = TRUE, pal.col = rainbow(100, s = 0.5, end = 0.8))
points(0, 1, pch="+", col="black")
```

# Description

Fit of univariate continuous distribution by maximizing goodness-of-fit (or minimizing distance) for non censored data.

# Usage

```
mgedist(data, distr, gof = "CvM", start = NULL, fix.arg = NULL, optim.method = "default",
  lower = -Inf, upper = Inf, custom.optim = NULL, silent = TRUE, gradient = NULL,
  checkstartfix=FALSE, calcvcov=FALSE, ...)
```

# **Arguments**

data	A numeric vector for non censored data.
distr	A character string "name" naming a distribution for which the corresponding quantile function qname and the corresponding density distribution dname must be classically defined.
gof	A character string coding for the name of the goodness-of-fit distance used: "CvM" for Cramer-von Mises distance, "KS" for Kolmogorov-Smirnov distance, "AD" for Anderson-Darling distance, "ADR", "ADL", "AD2R", "AD2L" and "AD2" for variants of Anderson-Darling distance described by Luceno (2006).
start	A named list giving the initial values of parameters of the named distribution or a function of data computing initial values and returning a named list. This argument may be omitted (default) for some distributions for which reasonable starting values are computed (see the 'details' section of mledist).
fix.arg	An optional named list giving the values of fixed parameters of the named distribution or a function of data computing (fixed) parameter values and returning a named list. Parameters with fixed value are thus NOT estimated.
optim.method	"default" or optimization method to pass to optim.
lower	Left bounds on the parameters for the "L-BFGS-B" method (see optim).
upper	Right bounds on the parameters for the "L-BFGS-B" method (see optim).
custom.optim	a function carrying the optimization.
silent	A logical to remove or show warnings when bootstraping.
gradient	A function to return the gradient of the gof distance for the "BFGS", "CG" and "L-BFGS-B" methods. If it is NULL, a finite-difference approximation will be used.
checkstartfix	A logical to test starting and fixed values. Do not change it.
calcvcov	A logical indicating if (asymptotic) covariance matrix is required. (currently ignored)
• • •	further arguments passed to the $\ensuremath{optim}$ , $\ensuremath{constrOptim}$ or $\ensuremath{custom.optim}$ function.

#### **Details**

The mgedist function numerically maximizes goodness-of-fit, or minimizes a goodness-of-fit distance coded by the argument gof. One may use one of the classical distances defined in Stephens (1986), the Cramer-von Mises distance ("CVM"), the Kolmogorov-Smirnov distance ("KS") or the Anderson-Darling distance ("AD") which gives more weight to the tails of the distribution, or one of the variants of this last distance proposed by Luceno (2006). The right-tail AD ("ADR") gives more weight only to the right tail, the left-tail AD ("ADL") gives more weight only to the left tail. Either of the tails, or both of them, can receive even larger weights by using second order Anderson-Darling Statistics (using "AD2R", "AD2L" or "AD2").

The optimization process is the same as mledist, see the 'details' section of that function.

This function is not intended to be called directly but is internally called in fitdist and bootdist.

This function is intended to be used only with continuous distributions and weighted maximum goodness-of-fit estimation is not allowed.

NB: if your data values are particularly small or large, a scaling may be needed before the optimization process. See example (4).

#### Value

mgedist returns a list with following components,

estimate the parameter estimates.

convergence an integer code for the convergence of optim defined as below or defined by the

user in the user-supplied optimization function. 0 indicates successful convergence. 1 indicates that the iteration limit of optim has been reached. 10 indicates degeneracy of the Nealder-Mead simplex. 100 indicates that optim encountered

an internal error.

value the minimal value reached for the criterion to minimize.

hessian a symmetric matrix computed by optim as an estimate of the Hessian at the

solution found or computed in the user-supplied optimization function.

optim. function the name of the optimization function used for maximum likelihood.

optim.method when optim is used, the name of the algorithm used, the field method of the

custom.optim function otherwise.

fix.arg the named list giving the values of parameters of the named distribution that

must kept fixed rather than estimated by maximum likelihood or NULL if there

are no such parameters.

fix.arg.fun the function used to set the value of fix.arg or NULL.

weights the vector of weights used in the estimation process or NULL.

counts A two-element integer vector giving the number of calls to the log-likelihood

function and its gradient respectively. This excludes those calls needed to compute the Hessian, if requested, and any calls to log-likelihood function to compute a finite-difference approximation to the gradient. counts is returned by

optim or the user-supplied function or set to NULL.

optim.message A character string giving any additional information returned by the optimizer,

or NULL. To understand exactly the message, see the source code.

loglik the log-likelihood value.

gof the code of the goodness-of-fit distance maximized.

#### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

#### References

Luceno A (2006), Fitting the generalized Pareto distribution to data using maximum goodness-of-fit estimators. Computational Statistics and Data Analysis, 51, 904-917, doi:10.1016/j.csda.2005.09.011.

Stephens MA (1986), *Tests based on edf statistics*. In Goodness-of-fit techniques (D'Agostino RB and Stephens MA, eds), Marcel Dekker, New York, pp. 97-194.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

#### See Also

See mmedist, mledist, qmedist, fitdist for other estimation methods.

Please visit the Frequently Asked Questions.

```
# (1) Fit of a Weibull distribution to serving size data by maximum
# goodness-of-fit estimation using all the distances available
data(groundbeef)
serving <- groundbeef$serving</pre>
mgedist(serving, "weibull", gof="CvM")
mgedist(serving, "weibull", gof="KS")
mgedist(serving, "weibull", gof="AD")
mgedist(serving, "weibull", gof="ADR")
mgedist(serving, "weibull", gof="ADL")
mgedist(serving, "weibull", gof="AD2R")
mgedist(serving, "weibull", gof="AD2L")
mgedist(serving, "weibull", gof="AD2")
# (2) Fit of a uniform distribution using Cramer-von Mises or
# Kolmogorov-Smirnov distance
set.seed(1234)
u <- runif(100,min=5,max=10)</pre>
mgedist(u,"unif",gof="CvM")
mgedist(u,"unif",gof="KS")
# (3) Fit of a triangular distribution using Cramer-von Mises or
# Kolmogorov-Smirnov distance
require("mc2d")
```

```
set.seed(1234)
t <- rtriang(100,min=5,mode=6,max=10)
mgedist(t,"triang",start = list(min=4, mode=6,max=9),gof="CvM")
mgedist(t,"triang",start = list(min=4, mode=6,max=9),gof="KS")
# (4) scaling problem
# the simulated dataset (below) has particularly small values, hence without scaling (10^0),
# the optimization raises an error. The for loop shows how scaling by 10^i
# for i=1,...,6 makes the fitting procedure work correctly.
set.seed(1234)
x2 <- rnorm(100, 1e-4, 2e-4)
for(i in 6:0)
    cat(i, try(mgedist(x*10^i, "cauchy")$estimate, silent=TRUE), "\n")
```

mledist

Maximum likelihood fit of univariate distributions

## **Description**

Fit of univariate distributions using maximum likelihood for censored or non censored data.

## **Usage**

```
mledist(data, distr, start = NULL, fix.arg = NULL, optim.method = "default",
   lower = -Inf, upper = Inf, custom.optim = NULL, weights = NULL, silent = TRUE,
   gradient = NULL, checkstartfix=FALSE, calcvcov=FALSE, ...)
```

## **Arguments**

data

A numeric vector for non censored data or a dataframe of two columns respectively named left and right, describing each observed value as an interval for censored data. In that case the left column contains either NA for left censored observations, the left bound of the interval for interval censored observations, or the observed value for non-censored observations. The right column contains either NA for right censored observations, the right bound of the interval for interval censored observations, or the observed value for non-censored observa-

distr

A character string "name" naming a distribution for which the corresponding density function dname and the corresponding distribution function pname must be classically defined.

start

A named list giving the initial values of parameters of the named distribution or a function of data computing initial values and returning a named list. This argument may be omitted (default) for some distributions for which reasonable starting values are computed (see details).

fix.arg An optional named list giving the values of fixed parameters of the named dis-

tribution or a function of data computing (fixed) parameter values and returning a named list. Parameters with fixed value are thus NOT estimated by this maxi-

mum likelihood procedure.

optim.method "default" (see details) or an optimization method to pass to optim.

lower Left bounds on the parameters for the "L-BFGS-B" method (see optim).

upper Right bounds on the parameters for the "L-BFGS-B" method (see optim).

custom.optim a function carrying the MLE optimisation (see details).

weights an optional vector of weights to be used in the fitting process. Should be NULL

or a numeric vector with strictly positive integers (typically the number of occurences of each observation). If non-NULL, weighted MLE is used, otherwise

ordinary MLE.

silent A logical to remove or show warnings when bootstraping.

gradient A function to return the gradient of the log-likelihood for the "BFGS", "CG" and

"L-BFGS-B" methods. If it is NULL, a finite-difference approximation will be

used, see details.

checkstartfix A logical to test starting and fixed values. Do not change it.

calcvcov A logical indicating if (asymptotic) covariance matrix is required.

... further arguments passed to the optim, constrOptim or custom.optim func-

tion.

# Details

This function is not intended to be called directly but is internally called in fitdist and bootdist when used with the maximum likelihood method and fitdistcens and bootdistcens.

It is assumed that the distr argument specifies the distribution by the probability density function and the cumulative distribution function (d, p). The quantile function and the random generator function (q, r) may be needed by other function such as mmedist, qmedist, mgedist, fitdist, fitdistcens, bootdistcens and bootdist.

For the following named distributions, reasonable starting values will be computed if start is omitted (i.e. NULL): "norm", "lnorm", "exp" and "pois", "cauchy", "gamma", "logis", "nbinom" (parametrized by mu and size), "geom", "beta", "weibull" from the stats package; all distributions (except phase-type distributions) from the actuar package. Note that these starting values may not be good enough if the fit is poor. The function uses a closed-form formula to fit the uniform distribution. If start is a list, then it should be a named list with the same names as in the d,p,q,r functions of the chosen distribution. If start is a function of data, then the function should return a named list with the same names as in the d,p,q,r functions of the chosen distribution.

The mledist function allows user to set a fixed values for some parameters. As for start, if fix.arg is a list, then it should be a named list with the same names as in the d,p,q,r functions of the chosen distribution. If fix.arg is a function of data, then the function should return a named list with the same names as in the d,p,q,r functions of the chosen distribution.

When custom.optim=NULL (the default), maximum likelihood estimations of the distribution parameters are computed with the R base optim or constrOptim. If no finite bounds (lower=-Inf and upper=Inf) are supplied, optim is used with the method specified by optim.method. Note

that optim.method="default" means optim.method="Nelder-Mead" for distributions with at least two parameters and optim.method="BFGS" for distributions with only one parameter. If finite bounds are supplied (among lower and upper) and gradient != NULL, constrOptim is used. If finite bounds are supplied (among lower and upper) and gradient == NULL, constrOptim is used when optim.method="Nelder-Mead"; optim is used when optim.method="L-BFGS-B" or "Brent"; in other case, an error is raised (same behavior as constrOptim).

When errors are raised by optim, it's a good idea to start by adding traces during the optimization process by adding control=list(trace=1, REPORT=1).

If custom.optim is not NULL, then the user-supplied function is used instead of the R base optim. The custom.optim must have (at least) the following arguments fn for the function to be optimized, par for the initialized parameters. Internally the function to be optimized will also have other arguments, such as obs with observations and ddistname with distribution name for non censored data (Beware of potential conflicts with optional arguments of custom.optim). It is assumed that custom.optim should carry out a MINIMIZATION. Finally, it should return at least the following components par for the estimate, convergence for the convergence code, value for fn(par), hessian, counts for the number of calls (function and gradient) and message (default to NULL) for the error message when custom.optim raises an error, see the returned value of optim. See examples in fitdist and fitdistcens.

Optionally, a vector of weights can be used in the fitting process. By default (when weigths=NULL), ordinary MLE is carried out, otherwise the specified weights are used to balance the log-likelihood contributions. It is not yet possible to take into account weights in functions plotdist, plotdistcens, plot.fitdist, plot.fitdistcens, cdfcomp, cdfcompcens, denscomp, ppcomp, qqcomp, gofstat, descdist, bootdist, bootdistcens and mgedist. (developments planned in the future).

NB: if your data values are particularly small or large, a scaling may be needed before the optimization process. See Example (7).

## Value

mledist returns a list with following components,

estimate the parameter estimates.

convergence an integer code for the convergence of optim/constrOptim defined as below

or defined by the user in the user-supplied optimization function. 0 indicates successful convergence. 1 indicates that the iteration limit of optim has been reached. 10 indicates degeneracy of the Nealder-Mead simplex. 100 indicates

that optim encountered an internal error.

value the minimal value reached for the criterion to minimize.

hessian a symmetric matrix computed by optim as an estimate of the Hessian at the

solution found or computed in the user-supplied optimization function. It is

used in fitdist to estimate standard errors.

optim.function the name of the optimization function used for maximum likelihood.

optim.method when optim is used, the name of the algorithm used, the field method of the

custom.optim function otherwise.

fix.arg the named list giving the values of parameters of the named distribution that

must kept fixed rather than estimated by maximum likelihood or NULL if there

are no such parameters.

fix.arg.fun the function used to set the value of fix.arg or NULL.

weights the vector of weights used in the estimation process or NULL.

counts A two-element integer vector giving the number of calls to the log-likelihood

function and its gradient respectively. This excludes those calls needed to compute the Hessian, if requested, and any calls to log-likelihood function to compute a finite-difference approximation to the gradient. counts is returned by

optim or the user-supplied function or set to NULL.

optim.message A character string giving any additional information returned by the optimizer,

or NULL. To understand exactly the message, see the source code.

loglik the log-likelihood value.

method "closed formula" if appropriate otherwise NULL.

### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

#### References

Venables WN and Ripley BD (2002), *Modern applied statistics with S.* Springer, New York, pp. 435-446, doi:10.1007/9780387217062.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

## See Also

See mmedist, qmedist, mgedist, fitdist, fitdistcens for other estimation methods, optim, constrOptim for optimization routines, bootdistcens and bootdist for bootstrap, and llplot for plotting the (log)likelihood.

Please visit the Frequently Asked Questions.

```
# (1) basic fit of a normal distribution with maximum likelihood estimation
#
set.seed(1234)
x1 <- rnorm(n=100)
mledist(x1,"norm")
# (2) defining your own distribution functions, here for the Gumbel distribution
# for other distributions, see the CRAN task view dedicated to probability distributions
dgumbel <- function(x,a,b) 1/b*exp((a-x)/b)*exp(-exp((a-x)/b))
mledist(x1,"gumbel",start=list(a=10,b=5))
# (3) fit of a discrete distribution (Poisson)
# set.seed(1234)</pre>
```

```
x2 \leftarrow rpois(n=30, lambda = 2)
mledist(x2,"pois")
# (4) fit a finite-support distribution (beta)
set.seed(1234)
x3 <- rbeta(n=100, shape1=5, shape2=10)
mledist(x3,"beta")
# (5) fit frequency distributions on USArrests dataset.
#
x4 <- USArrests$Assault
mledist(x4, "pois")
mledist(x4, "nbinom")
# (6) fit a continuous distribution (Gumbel) to censored data.
data(fluazinam)
log10EC50 <-log10(fluazinam)</pre>
# definition of the Gumbel distribution
dgumbel <- function(x,a,b) 1/b*exp((a-x)/b)*exp(-exp((a-x)/b))
pgumbel <- function(q,a,b) exp(-exp((a-q)/b))
qgumbel <- function(p,a,b) a-b*log(-log(p))</pre>
mledist(log10EC50, "gumbel", start=list(a=0, b=2), optim.method="Nelder-Mead")
# (7) scaling problem
# the simulated dataset (below) has particularly small values,
# hence without scaling (10^0),
# the optimization raises an error. The for loop shows how scaling by 10^i
# for i=1,...,6 makes the fitting procedure work correctly.
set.seed(1234)
x2 <- rnorm(100, 1e-4, 2e-4)
for(i in 6:0)
    cat(i, try(mledist(x*10^i, "cauchy")$estimate, silent=TRUE), "\n")
# (17) small example for the zero-modified geometric distribution
dzmgeom \leftarrow function(x, p1, p2) p1 * (x == 0) + (1-p1)*dgeom(x-1, p2) #pdf
x2 < -c(2, 4, 0, 40, 4, 21, 0, 0, 0, 2, 5, 0, 0, 13, 2) #simulated dataset
initp1 \leftarrow function(x) list(p1=mean(x == 0)) #init as MLE
mledist(x2, "zmgeom", fix.arg=initp1, start=list(p2=1/2))
```

# **Description**

Fit of univariate distributions by matching moments (raw or centered) for non censored data.

# Usage

```
mmedist(data, distr, order, memp, start = NULL, fix.arg = NULL, optim.method = "default",
   lower = -Inf, upper = Inf, custom.optim = NULL, weights = NULL, silent = TRUE,
   gradient = NULL, checkstartfix=FALSE, calcvcov=FALSE, ...)
```

# Arguments

data	A numeric vector for non censored data.
distr	A character string "name" naming a distribution (see 'details').
order	A numeric vector for the moment order(s). The length of this vector must be equal to the number of parameters to estimate.
memp	A function implementing empirical moments, raw or centered but has to be consistent with distr argument (and weights argument). See details below.
start	A named list giving the initial values of parameters of the named distribution or a function of data computing initial values and returning a named list. This argument may be omitted (default) for some distributions for which reasonable starting values are computed (see the 'details' section of mledist).
fix.arg	An optional named list giving the values of fixed parameters of the named distribution or a function of data computing (fixed) parameter values and returning a named list. Parameters with fixed value are thus NOT estimated.
optim.method	"default" or optimization method to pass to optim.
lower	Left bounds on the parameters for the "L-BFGS-B" method (see optim).
upper	Right bounds on the parameters for the "L-BFGS-B" method (see optim).
custom.optim	a function carrying the optimization .
weights	an optional vector of weights to be used in the fitting process. Should be NULL or a numeric vector with strictly positive integers (typically the number of occurences of each observation). If non-NULL, weighted MME is used, otherwise ordinary MME.
silent	A logical to remove or show warnings when bootstraping.
gradient	A function to return the gradient of the squared difference for the "BFGS", "CG" and "L-BFGS-B" methods. If it is NULL, a finite-difference approximation will be used, see details.
checkstartfix	A logical to test starting and fixed values. Do not change it.
calcvcov	A logical indicating if (asymptotic) covariance matrix is required.
	further arguments passed to the ${\tt optim}, {\tt constrOptim}$ or ${\tt custom.optim}$ function.

#### **Details**

The argument distr can be one of the base R distributions: "norm", "lnorm", "exp" and "pois", "gamma", "logis", "nbinom", "geom", "beta" and "unif". In that case, no other arguments than data and distr are required, because the estimate is computed by a closed-form formula. For distributions characterized by one parameter ("geom", "pois" and "exp"), this parameter is simply estimated by matching theoretical and observed means, and for distributions characterized by two parameters, these parameters are estimated by matching theoretical and observed means and variances (Vose, 2000). Note that for these closed-form formula, fix.arg cannot be used and start is ignored.

The argument distr can also be the distribution name as long as a corresponding mdistr function exists, e.g. "pareto" if "mpareto" exists. In that case arguments arguments order and memp have to be supplied in order to carry out the matching numerically, by minimization of the sum of squared differences between observed and theoretical moments. Optionnally other arguments can be supplied to control optimization (see the 'details' section of mledist for details about arguments for the control of optimization). In that case, fix.arg can be used and start is taken into account.

For non closed-form estimators, memp must be provided to compute empirical moments. When weights=NULL, this function must have two arguments x, order: x the numeric vector of the data and order the order of the moment. When weights!=NULL, this function must have three arguments x, order, weights: x the numeric vector of the data, order the order of the moment, weights the numeric vector of weights. See examples below.

Optionally, a vector of weights can be used in the fitting process. By default (when weigths=NULL), ordinary MME is carried out, otherwise the specified weights are used to compute (raw or centered) weighted moments. For closed-form estimators, weighted mean and variance are computed by wtdmean and wtdvar from the Hmisc package. When a numerical minimization is used, weighted are expected to be computed by the memp function. It is not yet possible to take into account weighths in functions plotdist, plotdistcens, plot.fitdist, plot.fitdistcens, cdfcomp, cdfcompcens, denscomp, ppcomp, qqcomp, gofstat and descdist (developments planned in the future).

This function is not intended to be called directly but is internally called in fitdist and bootdist when used with the matching moments method.

Since Version 1.2-0, mmedist automatically computes the asymptotic covariance matrix using I. Ibragimov and R. Has'minskii (1981), hence the theoretical moments mdist should be defined up to an order which equals to twice the maximal order given order. For instance, the normal distribution, we fit against the expectation and the variance and we need to have mnorm up to order  $2\times 2=4$ .

## Value

mmedist returns a list with following components,

estimate the parameter estimates.

convergence an integer code for the convergence of optim defined as below or defined by the

user in the user-supplied optimization function. 0 indicates successful convergence. 1 indicates that the iteration limit of optim has been reached. 10 indicates degeneracy of the Nealder-Mead simplex. 100 indicates that optim encountered

an internal error.

value the minimal value reached for the criterion to minimize.

hessian a symmetric matrix computed by optim as an estimate of the Hessian at the

solution found or computed in the user-supplied optimization function.

optim. function (if appropriate) the name of the optimization function used for maximum likeli-

nood.

optim.method (if appropriate) when optim is used, the name of the algorithm used, the field

method of the custom.optim function otherwise.

fix.arg the named list giving the values of parameters of the named distribution that

must kept fixed rather than estimated by maximum likelihood or NULL if there

are no such parameters.

fix.arg.fun the function used to set the value of fix.arg or NULL.

weights the vector of weights used in the estimation process or NULL.

counts A two-element integer vector giving the number of calls to the log-likelihood

function and its gradient respectively. This excludes those calls needed to compute the Hessian, if requested, and any calls to log-likelihood function to compute a finite-difference approximation to the gradient. counts is returned by

optim or the user-supplied function or set to NULL.

optim.message A character string giving any additional information returned by the optimizer,

or NULL. To understand exactly the message, see the source code.

loglik the log-likelihood value.

method either "closed formula" or the name of the optimization method.

order the order of the moment(s) matched.

memp the empirical moment function.

## Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

### References

I. Ibragimov and R. Has'minskii (1981), *Statistical Estimation - Asymptotic Theory*, Springer-Verlag, doi:10.1007/9781489900272

Evans M, Hastings N and Peacock B (2000), *Statistical distributions*. John Wiley and Sons Inc, doi:10.1002/9780470627242.

Vose D (2000), *Risk analysis, a quantitative guide*. John Wiley & Sons Ltd, Chischester, England, pp. 99-143.

Delignette-Muller ML and Dutang C (2015), *fitdistriplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

#### See Also

See mledist, qmedist, mgedist, fitdist, fitdistcens, optim, bootdistcens and bootdist.

Please visit the Frequently Asked Questions.

```
# (1) basic fit of a normal distribution with moment matching estimation
set.seed(1234)
n <- 100
x1 <- rnorm(n=n)</pre>
mmedist(x1, "norm")
#weighted
w \leftarrow c(rep(1, n/2), rep(10, n/2))
mmedist(x1, "norm", weights=w)$estimate
# (2) fit a discrete distribution (Poisson)
set.seed(1234)
x2 \leftarrow rpois(n=30, lambda = 2)
mmedist(x2, "pois")
# (3) fit a finite-support distribution (beta)
set.seed(1234)
x3 <- rbeta(n=100, shape1=5, shape2=10)
mmedist(x3, "beta")
# (4) fit a Pareto distribution
  require("actuar")
  #simulate a sample
  x4 <- rpareto(1000, 6, 2)
  #empirical raw moment
  memp <- function(x, order) mean(x^order)</pre>
  memp2 <- function(x, order, weights) sum(x^order * weights)/sum(weights)</pre>
  #fit by MME
  mmedist(x4, "pareto", order=c(1, 2), memp=memp,
    start=list(shape=10, scale=10), lower=1, upper=Inf)
  #fit by weighted MME
  w \leftarrow rep(1, length(x4))
  w[x4 < 1] < -2
  mmedist(x4, "pareto", order=c(1, 2), memp=memp2, weights=w,
    start=list(shape=10, scale=10), lower=1, upper=Inf)
```

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msedist	Maximum spacing estimation of univariate distributions
msed1st	Maximum spacing estimation of univariate distributions

# Description

Fit of univariate distribution by maximizing (log) spacings for non censored data.

# Usage

```
msedist(data, distr, phidiv="KL", power.phidiv=NULL, start = NULL, fix.arg = NULL,
  optim.method = "default", lower = -Inf, upper = Inf, custom.optim = NULL,
  weights=NULL, silent = TRUE, gradient = NULL, checkstartfix=FALSE, calcvcov=FALSE, ...)
```

# Arguments

data	A numeric vector for non censored data.
distr	A character string "name" naming a distribution for which the corresponding quantile function qname and the corresponding density distribution dname must be classically defined.
phidiv	A character string coding for the name of the phi-divergence used: "KL" for Kullback-Leibler information (corresponds to classic maximum spacing estimation), "J" for Jeffreys' divergence, "R" for Renyi's divergence, "H" for Hellinger distance, "V" for Vajda's measure of information, see details.
power.phidiv	If relevant, a numeric for the power used in some phi-divergence: should be NULL when phidiv="KL" or phidiv="J", should be positive and different from 1 when phidiv="R", should be greater or equal to 1 when phidiv="H" or phidiv="V", see details.
start	A named list giving the initial values of parameters of the named distribution or a function of data computing initial values and returning a named list. This argument may be omitted (default) for some distributions for which reasonable starting values are computed (see the 'details' section of mledist).
fix.arg	An optional named list giving the values of fixed parameters of the named distribution or a function of data computing (fixed) parameter values and returning a named list. Parameters with fixed value are thus NOT estimated.
optim.method	"default" or optimization method to pass to optim.
lower	Left bounds on the parameters for the "L-BFGS-B" method (see optim).
upper	Right bounds on the parameters for the "L-BFGS-B" method (see optim).
custom.optim	a function carrying the optimization.
weights	an optional vector of weights to be used in the fitting process. Should be NULL or a numeric vector with strictly positive integers (typically the number of occurences of each observation). If non-NULL, weighted MSE is used, otherwise ordinary MSE.
silent	A logical to remove or show warnings when bootstraping.

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gradient A function to return the gradient of the gof distance for the "BFGS", "CG" and

"L-BFGS-B" methods. If it is NULL, a finite-difference approximation will be

used.

checkstartfix A logical to test starting and fixed values. Do not change it.

calcvcov A logical indicating if (asymptotic) covariance matrix is required. (currently

ignored)

further arguments passed to the optim, constrOptim or custom.optim func-

tion.

#### **Details**

The msedist function numerically maximizes a phi-divergence function of spacings, where spacings are the differences of the cumulative distribution function evaluated at the sorted dataset. The classical maximum spacing estimation (MSE) was introduced by Cheng and Amin (1986) and Ranneby (1984) independently where the phi-diverence is the logarithm, see Anatolyev and Kosenok (2005) for a link between MSE and maximum likelihood estimation.

MSE was generalized by Ranneby and Ekstrom (1997) by allowing different phi-divergence function. Generalized MSE maximizes

$$S_n(\theta) = \frac{1}{n+1} \sum_{i=1}^{n+1} \phi \left( F(x_{(i)}; \theta) - F(x_{(i-1)}; \theta) \right),$$

where  $F(;\theta)$  is the parametric distribution function to be fitted,  $\phi$  is the phi-divergence function,  $x_{(1)} < \cdots < x_{(n)}$  is the sorted sample,  $x_{(0)} = -\infty$  and  $x_{(n+1)} = +\infty$ . The possible phi-divergence function is

• Kullback-Leibler information (when phidiv="KL" and corresponds to classical MSE)

$$\phi(x) = \log(x)$$

• Jeffreys' divergence (when phidiv="J")

$$\phi(x) = (1 - x)\log(x)$$

• Renyi's divergence (when phidiv="R" and power.phidiv=alpha)

$$\phi(x) = x^{\alpha} \times \text{sign}(1-\alpha) \text{ with } \alpha > 0, \alpha \neq 1$$

• Hellinger distance (when phidiv="H" and power.phidiv=p)

$$\phi(x) = -|1 - x^{1/p}|^p$$
 with  $p \ge 1$ 

• Vajda's measure of information (when phidiv="V" and power.phidiv=beta)

$$\phi(x) = -|1-x|^{\beta}$$
 with  $\beta > 1$ 

The optimization process is the same as mledist, see the 'details' section of that function.

This function is not intended to be called directly but is internally called in fitdist and bootdist.

This function is intended to be used only with non-censored data.

NB: if your data values are particularly small or large, a scaling may be needed before the optimization process, see mledist's examples.

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#### Value

msedist returns a list with following components,

estimate the parameter estimates.

convergence an integer code for the convergence of optim defined as below or defined by the

user in the user-supplied optimization function. 0 indicates successful convergence. 1 indicates that the iteration limit of optim has been reached. 10 indicates degeneracy of the Nealder-Mead simplex. 100 indicates that optim encountered

an internal error.

value the minimal value reached for the criterion to minimize.

hessian a symmetric matrix computed by optim as an estimate of the Hessian at the

solution found or computed in the user-supplied optimization function.

optim. function the name of the optimization function used for maximum likelihood.

optim.method when optim is used, the name of the algorithm used, the field method of the

custom.optim function otherwise.

fix.arg the named list giving the values of parameters of the named distribution that

must kept fixed rather than estimated by maximum likelihood or NULL if there

are no such parameters.

fix.arg.fun the function used to set the value of fix.arg or NULL.

weights the vector of weights used in the estimation process or NULL.

counts A two-element integer vector giving the number of calls to the log-likelihood

function and its gradient respectively. This excludes those calls needed to compute the Hessian, if requested, and any calls to log-likelihood function to compute a finite-difference approximation to the gradient. counts is returned by

optim or the user-supplied function or set to NULL.

optim.message A character string giving any additional information returned by the optimizer,

or NULL. To understand exactly the message, see the source code.

loglik the log-likelihood value.

phidiv The character string coding for the name of the phi-divergence used either "KL",

"J", "R", "H" or "V".

power . phidiv Either NULL or a numeric for the power used in the phi-divergence.

#### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

## References

Anatolyev, S., and Kosenok, G. (2005). *An alternative to maximum likelihood based on spacings*. Econometric Theory, 21(2), 472-476, doi:10.1017/S026646605050255.

Cheng, R.C.H. and N.A.K. Amin (1983) Estimating parameters in continuous univariate distributions with a shifted origin. Journal of the Royal Statistical Society Series B 45, 394-403, doi:10.1111/j.25176161.1983.tb01268.x.

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Ranneby, B. (1984) *The maximum spacing method: An estimation method related to the maximum likelihood method.* Scandinavian Journal of Statistics 11, 93-112.

Ranneby, B. and Ekstroem, M. (1997). *Maximum spacing estimates based on different metrics*. Umea universitet.

#### See Also

See mmedist, mledist, qmedist, mgedist, fitdist for other estimation methods.

Please visit the Frequently Asked Questions.

## **Examples**

```
# (1) Fit of a Weibull distribution to serving size data by maximum
# spacing estimation
#

data(groundbeef)
serving <- groundbeef$serving
msedist(serving, "weibull")

# (2) Fit of an exponential distribution
#

set.seed(123)
x1 <- rexp(1e3)
#the convergence is quick
msedist(x1, "exp", control=list(trace=0, REPORT=1))</pre>
```

plotdist

Plot of empirical and theoretical distributions for non-censored data

## **Description**

Plots an empirical distribution (non-censored data) with a theoretical one if specified.

## Usage

```
plotdist(data, distr, para, histo = TRUE, breaks = "default",
  demp = FALSE, discrete, ...)
```

## **Arguments**

data

A numeric vector.

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distr A character string "name" naming a distribution for which the corresponding density function dname, the corresponding distribution function pname and the corresponding quantile function gname must be defined, or directly the density function. This argument may be omitted only if para is omitted. A named list giving the parameters of the named distribution. This argument para may be omitted only if distr is omitted. histo A logical to plot the histogram using the hist function. breaks If "default" the histogram is plotted with the function hist with its default breaks definition. Else breaks is passed to the function hist. This argument is not taken into account if discrete is TRUE. A logical to plot the empirical density on the first plot (alone or superimposed on demp the histogram depending of the value of the argument histo) using the density function. discrete If TRUE, the distribution is considered as discrete. If both distr and discrete are missing, discrete is set to FALSE. If discrete is missing but not distr, discrete is set to TRUE when distr belongs to "binom", "nbinom", "geom", "hyper" or "pois". further graphical arguments passed to graphical functions used in plotdist.

#### **Details**

Empirical and, if specified, theoretical distributions are plotted in density and in cdf. For the plot in density, the user can use the arguments histo and demp to specify if he wants the histogram using the function hist, the density plot using the function density, or both (at least one of the two arguments must be put to "TRUE"). For continuous distributions, the function hist is used with its default breaks definition if breaks is "default" or passing breaks as an argument if it differs from "default". For continuous distribution and when a theoretical distribution is specified by both arguments distname and para, Q-Q plot (plot of the quantiles of the theoretical fitted distribution (x-axis) against the empirical quantiles of the data) and P-P plot (i.e. for each value of the data set, plot of the cumulative density function of the fitted distribution (x-axis) against the empirical cumulative density function (y-axis)) are also given (Cullen and Frey, 1999). The function ppoints (with default parameter for argument a) is used for the Q-Q plot, to generate the set of probabilities at which to evaluate the inverse distribution. NOTE THAT FROM VERSION 0.4-3, ppoints is also used for P-P plot and cdf plot for continuous data. To personalize the four plots proposed for continuous data, for example to change the plotting position, we recommend the use of functions cdfcomp, denscomp, qqcomp and ppcomp.

#### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

## References

Cullen AC and Frey HC (1999), *Probabilistic techniques in exposure assessment*. Plenum Press, USA, pp. 81-155.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

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## See Also

See graphcomp, descdist, hist, plot, plotdistcens and ppoints. Please visit the Frequently Asked Questions.

```
# (1) Plot of an empirical distribution with changing
# of default line types for CDF and colors
# and optionally adding a density line
set.seed(1234)
x1 <- rnorm(n=30)
plotdist(x1)
plotdist(x1, demp = TRUE)
plotdist(x1,histo = FALSE, demp = TRUE)
plotdist(x1, col="blue", type="b", pch=16)
plotdist(x1, type="s")
# (2) Plot of a discrete distribution against data
set.seed(1234)
x2 \leftarrow rpois(n=30, lambda = 2)
plotdist(x2, discrete=TRUE)
plotdist(x2, "pois", para=list(lambda = mean(x2)))
plotdist(x2, "pois", para=list(lambda = mean(x2)), lwd="2")
# (3) Plot of a continuous distribution against data
xn <- rnorm(n=100, mean=10, sd=5)</pre>
plotdist(xn, "norm", para=list(mean=mean(xn), sd=sd(xn)))
plotdist(xn, "norm", para=list(mean=mean(xn), sd=sd(xn)), pch=16)
plotdist(xn, "norm", para=list(mean=mean(xn), sd=sd(xn)), demp = TRUE)
plotdist(xn, "norm", para=list(mean=mean(xn), sd=sd(xn)),
histo = FALSE, demp = TRUE)
# (4) Plot of serving size data
data(groundbeef)
plotdist(groundbeef$serving, type="s")
# (5) Plot of numbers of parasites with a Poisson distribution
data(toxocara)
number <- toxocara$number</pre>
plotdist(number, discrete = TRUE)
plotdist(number, "pois", para=list(lambda=mean(number)))
```

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#### **Description**

Plots an empirical distribution for censored data with a theoretical one if specified.

#### Usage

#### **Arguments**

censdata A dataframe of two columns respectively named left and right, describing

each observed value as an interval. The left column contains either NA for left censored observations, the left bound of the interval for interval censored observations, or the observed value for non-censored observations. The right column contains either NA for right censored observations, the right bound of the interval for interval censored observations, or the observed value for non-

censored observations.

distr A character string "name" naming a distribution, for which the corresponding

density function dname and the corresponding distribution function pname must

be defined, or directly the density function.

para A named list giving the parameters of the named distribution. This argument

may be omitted only if distr is omitted.

leftNA the real value of the left bound of left censored observations: -Inf or a finite

value such as 0 for positive data for example.

rightNA the real value of the right bound of right censored observations: Inf or a finite

value such as a realistic maximum value.

NPMLE if TRUE an NPMLE (nonparametric maximum likelihood estimate) technique

is used to estimate the cdf curve of the censored data and previous arguments

leftNA and rightNA are not used (see details)

Turnbull.confint

if TRUE confidence intervals will be added to the Turnbull plot. In that case

NPMLE.method is forced to "Turnbull.middlepoints"

NPMLE.method Three NPMLE techniques are provided, "Wang", the default one, rewritten from

the package npsurv using function constrOptim from the package stats for optimisation, "Turnbull.middlepoints", an older one which is implemented in the package survival and "Turnbull.intervals" that uses the same Turnbull algorithm from the package survival but associates an interval to each equivalence class instead of the middlepoint of this interval (see details). Only "Wang" and "Turnbull.intervals" enable the derivation of a Q-Q plot and a P-P plot.

.. further graphical arguments passed to other methods. The title of the plot can be

modified using the argument main only for the CDF plot.

#### **Details**

If NPMLE is TRUE, and NPMLE.method is "Wang", empirical distributions are plotted in cdf using either the constrained Newton method (Wang, 2008) or the hierarchical constrained Newton method

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(Wang, 2013) to compute the overall empirical cdf curve. If NPMLE is TRUE, and NPMLE.method is "Turnbull.intervals", empirical are plotted in cdf using the EM approach of Turnbull (Turnbull, 1974). In those two cases, grey rectangles represent areas where the empirical distribution function is not unique. In cases where a theoretical distribution is specified, two goodness-of-fit plots are also provided, a Q-Q plot (plot of the quantiles of the theoretical fitted distribution (x-axis) against the empirical quantiles of the data) and a P-P plot (i.e. for each value of the data set, plot of the cumulative density function of the fitted distribution (x-axis) against the empirical cumulative density function (y-axis)). Grey rectangles in a Q-Q plot or a P-P plot also represent areas of non uniqueness of empirical quantiles or probabilities, directly derived from non uniqueness areas of the empirical cumulative distribution.

If NPMLE is TRUE, and NPMLE.method is "Turnbull.middlepoints", empirical and, if specified, theoretical distributions are plotted in cdf using the EM approach of Turnbull (Turnbull, 1974) to compute the overall empirical cdf curve, with confidence intervals if Turnbull.confint is TRUE, by calls to functions survfit and plot.survfit from the survival package.

If NPMLE is FALSE empirical and, if specified, theoretical distributions are plotted in cdf, with data directly reported as segments for interval, left and right censored data, and as points for non-censored data. Before plotting, observations are ordered and a rank r is associated to each of them. Left censored observations are ordered first, by their right bounds. Interval censored and non censored observations are then ordered by their mid-points and, at last, right censored observations are ordered by their left bounds. If leftNA (resp. rightNA) is finite, left censored (resp. right censored) observations are considered as interval censored observations and ordered by mid-points with noncensored and interval censored data. It is sometimes necessary to fix rightNA or leftNA to a realistic extreme value, even if not exactly known, to obtain a reasonable global ranking of observations. After ranking, each of the n observations is plotted as a point (one x-value) or a segment (an interval of possible x-values), with an y-value equal to r/n, r being the rank of each observation in the global ordering previously described. This second method may be interesting but is certainly less rigorous than the other methods that should be prefered.

## Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

## References

Turnbull BW (1974), *Nonparametric estimation of a survivorship function with doubly censored data*. Journal of American Statistical Association, 69, 169-173, doi:10.2307/2285518.

Wang Y (2008), Dimension-reduced nonparametric maximum likelihood computation for interval-censored data. Computational Statistics & Data Analysis, 52, 2388-2402, doi:10.1016/j.csda.2007.10.018.

Wang Y and Taylor SM (2013), *Efficient computation of nonparametric survival functions via a hierarchical mixture formulation*. Statistics and Computing, 23, 713-725, doi:10.1007/s11222012-93419.

Wang, Y., & Fani, S. (2018), *Nonparametric maximum likelihood computation of a U-shaped haz-ard function*. Statistics and Computing, 28(1), 187-200, doi:10.1007/s112220179724z.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

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## See Also

```
See plotdist, survfit.formula.

Please visit the Frequently Asked Questions.
```

## **Examples**

```
# (1) Plot of an empirical censored distribution (censored data) as a CDF
# using the default Wang method
data(smokedfish)
d1 <- as.data.frame(log10(smokedfish))</pre>
plotdistcens(d1)
# (2) Add the CDF of a normal distribution
plotdistcens(d1, "norm", para=list(mean = -1.6, sd = 1.5))
# (3) Various plots of the same empirical distribution
# default Wang plot with representation of equivalence classess
plotdistcens(d1, NPMLE = TRUE, NPMLE.method = "Wang")
# same plot but using the Turnbull alorithm from the package survival
plotdistcens(d1, NPMLE = TRUE, NPMLE.method = "Wang")
# Turnbull plot with middlepoints (as in the package survival)
plotdistcens(d1, NPMLE = TRUE, NPMLE.method = "Turnbull.middlepoints")
# Turnbull plot with middlepoints and confidence intervals
plotdistcens(d1, NPMLE = TRUE, NPMLE.method = "Turnbull.middlepoints", Turnbull.confint = TRUE)
# with intervals and points
plotdistcens(d1,rightNA=3, NPMLE = FALSE)
# with intervals and points
# defining a minimum value for left censored values
plotdistcens(d1,leftNA=-3, NPMLE = FALSE)
```

prefit

Pre-fitting procedure

#### **Description**

Search good starting values

# Usage

```
prefit(data, distr, method = c("mle", "mme", "qme", "mge"),
  feasible.par, memp=NULL, order=NULL,
  probs=NULL, qtype=7, gof=NULL, fix.arg=NULL, lower,
  upper, weights=NULL, silent=TRUE, ...)
```

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#### **Arguments**

data A numeric vector.

distr A character string "name" naming a distribution for which the corresponding

> density function dname, the corresponding distribution function pname and the corresponding quantile function gname must be defined, or directly the density

function.

method A character string coding for the fitting method: "mle" for 'maximum likeli-

> hood estimation', "mme" for 'moment matching estimation', "qme" for 'quantile matching estimation' and "mge" for 'maximum goodness-of-fit estimation'.

feasible.par A named list giving the initial values of parameters of the named distribution

> or a function of data computing initial values and returning a named list. This argument may be omitted (default) for some distributions for which reasonable starting values are computed (see the 'details' section of mledist). It may not

be into account for closed-form formulas.

order A numeric vector for the moment order(s). The length of this vector must be

equal to the number of parameters to estimate.

A function implementing empirical moments, raw or centered but has to be conmemp

sistent with distr argument (and weights argument).

A numeric vector of the probabilities for which the quantile matching is done. probs

The length of this vector must be equal to the number of parameters to estimate.

The quantile type used by the R quantile function to compute the empirical qtype

quantiles, (default 7 corresponds to the default quantile method in R).

gof A character string coding for the name of the goodness-of-fit distance used:

> "CvM" for Cramer-von Mises distance, "KS" for Kolmogorov-Smirnov distance, "AD" for Anderson-Darling distance, "ADR", "ADL", "AD2R", "AD2L" and

> "AD2" for variants of Anderson-Darling distance described by Luceno (2006).

An optional named list giving the values of fixed parameters of the named disfix.arg

> tribution or a function of data computing (fixed) parameter values and returning a named list. Parameters with fixed value are thus NOT estimated by this maximum likelihood procedure. The use of this argument is not possible if

method="mme" and a closed-form formula is used.

weights an optional vector of weights to be used in the fitting process. Should be NULL

or a numeric vector. If non-NULL, weighted MLE is used, otherwise ordinary

MLE.

silent A logical to remove or show warnings.

lower Lower bounds on the parameters.

Upper bounds on the parameters. upper

Further arguments to be passed to generic functions, or to one of the functions

"mledist", "mmedist", "qmedist" or "mgedist" depending of the chosen method. See mledist, mmedist, qmedist, mgedist for details on parameter

estimation.

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#### **Details**

Searching good starting values is achieved by transforming the parameters (from their constraint interval to the real line) of the probability distribution. Indeed,

- positive parameters in (0, Inf) are transformed using the logarithm (typically the scale parameter sd of a normal distribution, see Normal),
- parameters in (1, Inf) are transformed using the function log(x-1),
- probability parameters in (0,1) are transformed using the logit function log(x/(1-x)) (typically the parameter prob of a geometric distribution, see Geometric),
- negative probability parameters in (-1,0) are transformed using the function log(-x/(1+x)),
- real parameters are of course not transformed at all, typically the mean of a normal distribution, see Normal.

Once parameters are transformed, an optimization is carried out by a quasi-Newton algorithm (typically BFGS) and then we transform them back to original parameter value.

#### Value

A named list.

## Author(s)

Christophe Dutang and Marie-Laure Delignette-Muller.

#### References

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

## See Also

See mledist, mmedist, qmedist, mgedist for details on parameter estimation. See fitdist for the main procedure.

```
# (1) fit of a gamma distribution by maximum likelihood estimation
#
x <- rgamma(1e3, 5/2, 7/2)
prefit(x, "gamma", "mle", list(shape=3, scale=3), lower=-Inf, upper=Inf)</pre>
```

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Quantile matching fit of univariate distributions

# Description

Fit of univariate distribution by matching quantiles for non censored data.

# Usage

```
qmedist(data, distr, probs, start = NULL, fix.arg = NULL, qtype = 7,
    optim.method = "default", lower = -Inf, upper = Inf,
    custom.optim = NULL, weights = NULL, silent = TRUE, gradient = NULL,
    checkstartfix=FALSE, calcvcov=FALSE, ...)
```

# Arguments

data	A numeric vector for non censored data.
distr	A character string "name" naming a distribution for which the corresponding quantile function qname and the corresponding density distribution dname must be classically defined.
probs	A numeric vector of the probabilities for which the quantile matching is done. The length of this vector must be equal to the number of parameters to estimate.
start	A named list giving the initial values of parameters of the named distribution or a function of data computing initial values and returning a named list. This argument may be omitted (default) for some distributions for which reasonable starting values are computed (see the 'details' section of mledist).
fix.arg	An optional named list giving the values of fixed parameters of the named distribution or a function of data computing (fixed) parameter values and returning a named list. Parameters with fixed value are thus NOT estimated.
qtype	The quantile type used by the R quantile function to compute the empirical quantiles, (default 7 corresponds to the default quantile method in R).
optim.method	"default" or optimization method to pass to optim.
lower	Left bounds on the parameters for the "L-BFGS-B" method (see optim).
upper	Right bounds on the parameters for the "L-BFGS-B" method (see optim).
custom.optim	a function carrying the optimization.
weights	an optional vector of weights to be used in the fitting process. Should be NULL or a numeric vector with strictly positive integers (typically the number of occurences of each observation). If non-NULL, weighted QME is used, otherwise ordinary QME.
silent	A logical to remove or show warnings when bootstraping.
gradient	A function to return the gradient of the squared difference for the "BFGS", "CG" and "L-BFGS-B" methods. If it is NULL, a finite-difference approximation will

be used, see details.

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checkstartfix A logical to test starting and fixed values. Do not change it.

calcvcov A logical indicating if (asymptotic) covariance matrix is required. (currently

ignored)

... further arguments passed to the optim, constrOptim or custom.optim func-

tion.

#### **Details**

The qmedist function carries out the quantile matching numerically, by minimization of the sum of squared differences between observed and theoretical quantiles. Note that for discrete distribution, the sum of squared differences is a step function and consequently, the optimum is not unique, see the FAQ.

The optimization process is the same as mledist, see the 'details' section of that function.

Optionally, a vector of weights can be used in the fitting process. By default (when weigths=NULL), ordinary QME is carried out, otherwise the specified weights are used to compute weighted quantiles used in the squared differences. Weighted quantiles are computed by wtdquantile from the Hmisc package. It is not yet possible to take into account weighths in functions plotdist, plotdistcens, plot.fitdist, plot.fitdistcens, cdfcomp, cdfcompcens, denscomp, ppcomp, qqcomp, gofstat and descdist (developments planned in the future).

This function is not intended to be called directly but is internally called in fitdist and bootdist.

#### Value

qmedist returns a list with following components,

estimate the parameter estimates.

convergence an integer code for the convergence of optim defined as below or defined by the

user in the user-supplied optimization function. 0 indicates successful convergence. 1 indicates that the iteration limit of optim has been reached. 10 indicates degeneracy of the Nealder-Mead simplex. 100 indicates that optim encountered

an internal error.

value the minimal value reached for the criterion to minimize.

hessian a symmetric matrix computed by optim as an estimate of the Hessian at the

solution found or computed in the user-supplied optimization function.

optim. function the name of the optimization function used for maximum likelihood.

optim.method when optim is used, the name of the algorithm used, the field method of the

custom.optim function otherwise.

fix.arg the named list giving the values of parameters of the named distribution that

must kept fixed rather than estimated by maximum likelihood or NULL if there

are no such parameters.

fix.arg.fun the function used to set the value of fix.arg or NULL.

weights the vector of weights used in the estimation process or NULL.

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counts A two-element integer vector giving the number of calls to the log-likelihood

function and its gradient respectively. This excludes those calls needed to compute the Hessian, if requested, and any calls to log-likelihood function to compute a finite-difference approximation to the gradient. counts is returned by

optim or the user-supplied function or set to NULL.

optim.message A character string giving any additional information returned by the optimizer,

or NULL. To understand exactly the message, see the source code.

loglik the log-likelihood value.

probs the probability vector on which quantiles are matched.

## Author(s)

Christophe Dutang and Marie Laure Delignette-Muller.

#### References

Klugman SA, Panjer HH and Willmot GE (2012), *Loss Models: From Data to Decissions*, 4th edition. Wiley Series in Statistics for Finance, Business and Economics, p. 253, doi:10.1198/tech.2006.s409.

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

## See Also

See mmedist, mledist, mgedist, fitdist for other estimation methods and quantile for empirical quantile estimation in R.

Please visit the Frequently Asked Questions.

```
# (1) basic fit of a normal distribution
#
set.seed(1234)
x1 <- rnorm(n=100)
qmedist(x1, "norm", probs=c(1/3, 2/3))

# (2) defining your own distribution functions, here for the Gumbel
# distribution for other distributions, see the CRAN task view dedicated
# to probability distributions

dgumbel <- function(x, a, b) 1/b*exp((a-x)/b)*exp(-exp((a-x)/b))
qgumbel <- function(p, a, b) a - b*log(-log(p))
qmedist(x1, "gumbel", probs=c(1/3, 2/3), start=list(a=10,b=5))
# (3) fit a discrete distribution (Poisson)
#</pre>
```

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```
set.seed(1234)
x2 <- rpois(n=30,lambda = 2)
qmedist(x2, "pois", probs=1/2)

# (4) fit a finite-support distribution (beta)
#
set.seed(1234)
x3 <- rbeta(n=100,shape1=5, shape2=10)
qmedist(x3, "beta", probs=c(1/3, 2/3))

# (5) fit frequency distributions on USArrests dataset.
#
x4 <- USArrests$Assault
qmedist(x4, "pois", probs=1/2)
qmedist(x4, "nbinom", probs=c(1/3, 2/3))</pre>
```

quantile

Quantile estimation from a fitted distribution

## Description

Quantile estimation from a fitted distribution, optionally with confidence intervals calculated from the bootstrap result.

#### Usage

```
## S3 method for class 'fitdist'
quantile(x, probs = seq(0.1, 0.9, by=0.1), ...)
## S3 method for class 'fitdistcens'
quantile(x, probs = seq(0.1, 0.9, by=0.1), ...)
## S3 method for class 'bootdist'
quantile(x, probs = seq(0.1, 0.9, by=0.1),CI.type = "two.sided",
 CI.level = 0.95, ...)
## S3 method for class 'bootdistcens'
quantile(x, probs = seq(0.1, 0.9, by=0.1),CI.type = "two.sided",
  CI.level = 0.95, ...)
## S3 method for class 'quantile.fitdist'
print(x, ...)
## S3 method for class 'quantile.fitdistcens'
print(x, ...)
## S3 method for class 'quantile.bootdist'
print(x, ...)
## S3 method for class 'quantile.bootdistcens'
print(x, ...)
```

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## **Arguments**

An object of class "fitdist", "fitdistcens", "bootdist", "bootdistcens" or "quantile.fitdist", "quantile.fitdistens", "quantile.bootdist", "quantile.bootdistens" for the print generic function.

probs

A numeric vector of probabilities with values in [0, 1] at which quantiles must be calculated.

CI.type

Type of confidence intervals: either "two.sided" or one-sided intervals ("less" or "greater").

CI.level

The confidence level.

Further arguments to be passed to generic functions.

## **Details**

Quantiles of the parametric distribution are calculated for each probability specified in probs, using the estimated parameters. When used with an object of class "bootdist" or "bootdistcens", percentile confidence intervals and medians etimates are also calculated from the bootstrap result. If CI. type is two.sided, the CI.level two-sided confidence intervals of quantiles are calculated. If CI.type is less or greater, the CI.level one-sided confidence intervals of quantiles are calculated. The print functions show the estimated quantiles with percentile confidence intervals and median estimates when a bootstrap resampling has been done previously, and the number of bootstrap iterations for which the estimation converges if it is inferior to the whole number of bootstrap iterations.

#### Value

quantile returns a list with 2 components (the first two described below) when called with an object of class "fitdist" or "fitdistcens" and 8 components (described below) when called with an object of class "bootdist" or "bootdistcens":

quantiles a dataframe containing the estimated quantiles for each probability value speci-

fied in the argument probs (one row, and as many columns as values in probs).

probs the numeric vector of probabilities at which quantiles are calculated.

bootguant A data frame containing the bootstraped values for each quantile (many rows, as

specified in the call to bootdist in the argument niter, and as many columns

as values in probs)

quantCI If CI.type is two.sided, the two bounds of the CI.level percent two.sided

confidence interval for each quantile (two rows and as many columns as values in probs). If CI.type is less, right bound of the CI.level percent one.sided confidence interval for each quantile (one row). If CI.type is greater, left bound of the CI.level percent one.sided confidence interval for each quantile

(one row).

quantmedian Median of bootstrap estimates (per probability).

CI. type Type of confidence interval: either "two.sided" or one-sided intervals ("less"

or "greater").

CI.level The confidence level.

nbboot The number of samples drawn by bootstrap.

nbconverg The number of iterations for which the optimization algorithm converges.

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#### Author(s)

Marie-Laure Delignette-Muller and Christophe Dutang.

#### References

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

#### See Also

See fitdist, bootdist, fitdistcens, bootdistcens and CIcdfplot.

Please visit the Frequently Asked Questions.

```
\# (1) Fit of a normal distribution on acute toxicity log-transformed values of
# endosulfan for nonarthropod invertebrates, using maximum likelihood estimation
# to estimate what is called a species sensitivity distribution
# (SSD) in ecotoxicology, followed by estimation of the 5, 10 and 20 percent quantile
# values of the fitted distribution, which are called the 5, 10, 20 percent hazardous
# concentrations (HC5, HC10, HC20) in ecotoxicology, followed with calculations of their
# confidence intervals with various definitions, from a small number of bootstrap
# iterations to satisfy CRAN running times constraint.
# For practical applications, we recommend to use at least niter=501 or niter=1001.
data(endosulfan)
ATV <- subset(endosulfan, group == "NonArthroInvert")$ATV
log10ATV <- log10(subset(endosulfan, group == "NonArthroInvert")$ATV)</pre>
fln <- fitdist(log10ATV, "norm")</pre>
quantile(fln, probs = c(0.05, 0.1, 0.2))
bln <- bootdist(fln, bootmethod="param", niter=101)</pre>
quantile(bln, probs = c(0.05, 0.1, 0.2))
quantile(bln, probs = c(0.05, 0.1, 0.2), CI.type = "greater")
quantile(bln, probs = c(0.05, 0.1, 0.2), CI.level = 0.9)
# (2) Draw of 95 percent confidence intervals on quantiles of the
# previously fitted distribution
cdfcomp(fln)
q1 <- quantile(bln, probs = seq(0,1,length=101))
points(q1$quantCI[1,],q1$probs,type="1")
points(q1$quantCI[2,],q1$probs,type="1")
# (2b) Draw of 95 percent confidence intervals on quantiles of the
# previously fitted distribution
# using the NEW function CIcdfplot
CIcdfplot(bln, CI.output = "quantile", CI.fill = "pink")
# (3) Fit of a distribution on acute salinity log-transformed tolerance
# for riverine macro-invertebrates, using maximum likelihood estimation
```

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```
# to estimate what is called a species sensitivity distribution
# (SSD) in ecotoxicology, followed by estimation of the 5, 10 and 20 percent quantile
# values of the fitted distribution, which are called the 5, 10, 20 percent hazardous
# concentrations (HC5, HC10, HC20) in ecotoxicology, followed with calculations of
# their confidence intervals with various definitions.
# from a small number of bootstrap iterations to satisfy CRAN running times constraint.
# For practical applications, we recommend to use at least niter=501 or niter=1001.
#
data(salinity)
log10LC50 <-log10(salinity)
flncens <- fitdistcens(log10LC50,"norm")
quantile(flncens, probs = c(0.05, 0.1, 0.2))
blncens <- bootdistcens(flncens, niter = 101)
quantile(blncens, probs = c(0.05, 0.1, 0.2))
quantile(blncens, probs = c(0.05, 0.1, 0.2), CI.type = "greater")
quantile(blncens, probs = c(0.05, 0.1, 0.2), CI.type = "greater")
quantile(blncens, probs = c(0.05, 0.1, 0.2), CI.type = "greater")</pre>
```

salinity

Species-Sensitivity Distribution (SSD) for salinity tolerance

## **Description**

72-hour acute salinity tolerance (LC50 values) of riverine macro-invertebrates.

#### **Usage**

```
data(salinity)
```

## Format

salinity is a data frame with 2 columns named left and right, describing each observed LC50 value (in electrical condutivity, millisiemens per centimeter) as an interval. The left column contains either NA for left censored observations, the left bound of the interval for interval censored observations, or the observed value for non-censored observations. The right column contains either NA for right censored observations, the right bound of the interval for interval censored observations, or the observed value for noncensored observations.

## Source

Kefford, B.J., Nugegoda, D., Metzeling, L., Fields, E. 2006. Validating species sensitivity distributions using salinity tolerance of riverine macroinvertebrates in the southern Murray-darling Basin (Vitoria, Australia). *Canadian Journal of Fisheries and Aquatic Science*, **63**, 1865-1877.

```
# (1) load of data
#
data(salinity)
```

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```
# (2) plot of data using Turnbull cdf plot
log10LC50 <- log10(salinity)</pre>
plotdistcens(log10LC50)
# (3) fit of a normal and a logistic distribution to data in log10
# (classical distributions used for species sensitivity
# distributions, SSD, in ecotoxicology))
# and visual comparison of the fits using Turnbull cdf plot
fln <- fitdistcens(log10LC50, "norm")</pre>
summary(fln)
fll <- fitdistcens(log10LC50, "logis")
summary(fll)
cdfcompcens(list(fln, fll),legendtext = c("normal", "logistic"),
    xlab = "log10(LC50)", xlim = c(0.5, 2), lines01 = TRUE)
# (4) estimation of the 5 percent quantile value of
# the normal fitted distribution (5 percent hazardous concentration : HC5)
# with its two-sided 95 percent confidence interval calculated by
# non parametric bootstrap
# from a small number of bootstrap iterations to satisfy CRAN running times constraint.
# For practical applications, we recommend to use at least niter=501 or niter=1001.
# in log10(LC50)
bln <- bootdistcens(fln, niter = 101)</pre>
HC5ln <- quantile(bln, probs = 0.05)</pre>
# in LC50
10^(HC5ln$quantiles)
10^(HC5ln$quantCI)
# (5) estimation of the HC5 value
# with its one-sided 95 percent confidence interval (type "greater")
# in log10(LC50)
HC5lnb <- quantile(bln, probs = 0.05, CI.type = "greater")</pre>
# in LC50
10^(HC5lnb$quantiles)
10^(HC5lnb$quantCI)
```

smokedfish

Contamination data of Listeria monocytogenes in smoked fish

## **Description**

Contamination data of *Listeria monocytogenes* in smoked fish on the Belgian market in the period 2005 to 2007.

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#### Usage

```
data(smokedfish)
```

#### **Format**

smokedfish is a data frame with 2 columns named left and right, describing each observed value of *Listeria monocytogenes* concentration (in CFU/g) as an interval. The left column contains either NA for left censored observations, the left bound of the interval for interval censored observations, or the observed value for non-censored observations. The right column contains either NA for right censored observations, the right bound of the interval for interval censored observations, or the observed value for non-censored observations.

#### Source

Busschaert, P., Geereard, A.H., Uyttendaele, M., Van Impe, J.F., 2010. Estimating distributions out of qualitative and (semi) quantitative microbiological contamination data for use in risk assessment. *International Journal of Food Microbiology.* **138**, 260-269.

## **Examples**

```
# (1) load of data
#
data(smokedfish)

# (2) plot of data in CFU/g
#
plotdistcens(smokedfish)

# (3) plot of transformed data in log10[CFU/g]
#
Clog10 <- log10(smokedfish)
plotdistcens(Clog10)

# (4) Fit of a normal distribution to data in log10[CFU/g]
#
fitlog10 <- fitdistcens(Clog10, "norm")
summary(fitlog10)
plot(fitlog10)</pre>
```

Surv2fitdistcens

Handling of data formated as in the survival package for use in fitdistcens()

## **Description**

Provide a function to prepare a data frame needed by fitdistcens() from data classically coded when using the Surv() function of the survival package

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## Usage

## **Arguments**

time	for right censored data, this is the follow up time. For interval data, the first argument is the starting time for the interval.
event	The status indicator, normally $\emptyset$ =alive, 1=dead. Other choices are TRUE/FALSE (TRUE = death) or 1/2 (2=death). For interval censored data, the status indicator is $\emptyset$ =right censored, 1=event at time, 2=left censored, 3=interval censored. For factor data, assume that it has only two levels with the second level coding death.
time2	ending time of the interval for interval censored. Intervals are assumed to be open on the left and closed on the right, (start, end].
type	character string specifying the type of censoring. Possible values are "right", "left", "interval", "interval".

## **Details**

Surv2fitdistcens makes a data.frame with two columns respectively named left and right, describing each observed value as an interval as required in fitdistcens(): the left column contains either NA for left-censored observations, the left bound of the interval for interval-censored observations, or the observed value for non-censored observations. The right column contains either NA for right-censored observations, the right bound of the interval for interval censored observations, or the observed value for non-censored observations.

## Value

Surv2fitdistcens returns a data.frame with two columns respectively named left and right.

# Author(s)

Christophe Dutang and Marie-Laure Delignette-Muller.

## References

Delignette-Muller ML and Dutang C (2015), *fitdistrplus: An R Package for Fitting Distributions*. Journal of Statistical Software, 64(4), 1-34, doi:10.18637/jss.v064.i04.

## See Also

See fitdistrplus for an overview of the package. See fitdistcens for fitting of univariate distributions to censored data and fremale for the full dataset used in examples below. See Surv for survival objects which use the same arguments.

Please visit the Frequently Asked Questions.

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```
# (1) randomized fictive survival data - right-censored
origdata <- data.frame(rbind(</pre>
c( 43.01, 55.00,
c( 36.37, 47.17,
                        0),
c( 33.10, 34.51,
c( 71.00, 81.15,
                        0),
                        1),
c( 80.89, 81.91,
                       1),
c( 67.81, 78.48,
                       1),
c( 73.98, 76.92,
                       1),
c( 53.19, 54.80,
                       1)))
colnames(origdata) <- c("AgeIn", "AgeOut", "Death")</pre>
# add of follow-up time (for type = "right" in Surv())
origdata$followuptime <- origdata$AgeOut - origdata$AgeIn</pre>
origdata
### use of default survival type "right"
# in Surv()
survival::Surv(time = origdata$followuptime, event = origdata$Death, type = "right")
# for fitdistcens()
Surv2fitdistcens(origdata$followuptime, event = origdata$Death, type = "right")
# use of survival type "interval"
# in Surv()
survival::Surv(time = origdata$followuptime, time2 = origdata$followuptime,
          event = origdata$Death, type = "interval")
# for fitdistcens()
Surv2fitdistcens(time = origdata$followuptime, time2 = origdata$followuptime,
          event = origdata$Death, type = "interval")
# use of survival type "interval2"
origdata$survivalt1 <- origdata$followuptime
origdata$survivalt2 <- origdata$survivalt1</pre>
origdata$survivalt2[1:3] <- Inf</pre>
origdata
survival::Surv(time = origdata$survivalt1, time2 = origdata$survivalt2,
type = "interval2")
Surv2fitdistcens(origdata$survivalt1, time2 = origdata$survivalt2,
                type = "interval2")
# (2) Other examples with various left, right and interval censored values
# with left censored data
(d1 \leftarrow data.frame(time = c(2, 5, 3, 7), ind = c(0, 1, 1, 1)))
survival::Surv(time = d1$time, event = d1$ind, type = "left")
Surv2fitdistcens(time = d1$time, event = d1$ind, type = "left")
(d1bis \leftarrow data.frame(t1 = c(2, 5, 3, 7), t2 = c(2, 5, 3, 7),
  censtype = c(2, 1, 1, 1))
```

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```
survival::Surv(time = d1bis$t1, time2 = d1bis$t2,
  event = d1bis$censtype, type = "interval")
Surv2fitdistcens(time = d1bis$t1, time2 = d1bis$t2,
  event = d1bis$censtype, type = "interval")

# with interval, left and right censored data
(d2 <- data.frame(t1 = c(-Inf, 2, 3, 4, 3, 7), t2 = c(2, 5, 3, 7, 8, Inf)))
survival::Surv(time = d2$t1, time2 = d2$t2, type = "interval2")
Surv2fitdistcens(time = d2$t1, time2 = d2$t2, type = "interval2")

(d2bis <- data.frame(t1 = c(2, 2, 3, 4, 3, 7), t2 = c(2, 5, 3, 7, 8, 7),
  censtype = c(2,3,1,3,3,0)))
survival::Surv(time = d2bis$t1, time2 = d2bis$t2,
  event = d2bis$censtype, type = "interval")
Surv2fitdistcens(time = d2bis$t1, time2 = d2bis$t2,
  event = d2bis$censtype, type = "interval")</pre>
```

toxocara

Parasite abundance in insular feral cats

## **Description**

Toxocara cati abundance in feral cats living on Kerguelen island.

#### **Usage**

```
data(toxocara)
```

## Format

toxocara is a data frame with 1 column (number: number of parasites in digestive tract)

#### **Source**

Fromont, E., Morvilliers, L., Artois, M., Pontier, D. 2001. Parasite richness and abundance in insular and mainland feral cats. *Parasitology*, **123**, 143-151.

```
# (1) load of data
#
data(toxocara)

# (2) description and plot of data
#
number <- toxocara$number
descdist(number, discrete = TRUE, boot = 11)
plotdist(number, discrete = TRUE)

# (3) fit of a Poisson distribution to data</pre>
```

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```
#
fitp <- fitdist(number, "pois")
summary(fitp)
plot(fitp)

# (4) fit of a negative binomial distribution to data
#
fitnb <- fitdist(number, "nbinom")
summary(fitnb)
plot(fitnb)</pre>
```

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