

# Package ‘lddmm’

July 22, 2025

**Type** Package  
**Title** Longitudinal Drift-Diffusion Mixed Models (LDDMM)  
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**Description** Implementation of the drift-diffusion mixed model for category learning as described in Paulon et al. (2021) <[doi:10.1080/01621459.2020.1801448](https://doi.org/10.1080/01621459.2020.1801448)>.  
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|         |                               |
|---------|-------------------------------|
| B_basis | <i>Spline Basis Functions</i> |
|---------|-------------------------------|

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**Description**

Construct the J basis functions for the splines evaluated on a grid.

**Usage**

B\_basis(xgrid, knots)

**Arguments**

- xgrid            grid where we want to evaluate the spline functions (vector of length n)
- knots           vector of knots for the splines (vector of length K)

**Value**

n x (K+1) - matrix representing the value of each basis function evaluated on xgrid

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|              |                       |
|--------------|-----------------------|
| compute_WAIC | <i>Calculate WAIC</i> |
|--------------|-----------------------|

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**Description**

Function to compute the Watanabe-Akaike information criterion (Gelman, Hwang, Vehtari, 2014), which estimates the expected out-of-sample-prediction error using a bias-corrected adjustment of within-sample error.

**Usage**

compute\_WAIC(model\_fit)

**Arguments**

`model_fit` results of a model fit from the `lddmm` function

**Value**

A scalar indicating the WAIC (smaller WAIC denotes better fit)

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|                   |                        |
|-------------------|------------------------|
| <code>data</code> | <i>Example dataset</i> |
|-------------------|------------------------|

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**Description**

A toy dataset in the correct format for the LDDMM function call. This dataset has two possible response categories.

**Usage**

```
data
```

**Format**

A data frame with 24,254 rows and 6 columns

**Details**

- `subject`: vector of size `n` containing the participant labels
- `block`: vector of size `n` containing the training blocks (longitudinal units)
- `s`: vector of size `n` containing the stimuli
- `d`: vector of size `n` containing the decisions
- `r_time`: vector of size `n` containing the response times (log transformed)
- `cens`: vector of size `n` containing the censoring indicators (1 censored, 0 non censored)

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|                                 |                                  |
|---------------------------------|----------------------------------|
| <code>extract_post_draws</code> | <i>Parameter posterior draws</i> |
|---------------------------------|----------------------------------|

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**Description**

Function to extract the posterior draws of the parameters of interest from a `lddmm` fit object.

**Usage**

```
extract_post_draws(data, fit, par = c("drift", "boundary"))
```

**Arguments**

|                   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |
|-------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>data</code> | dataframe with the following columns: <ul style="list-style-type: none"> <li>• <code>subject</code>: vector of size <code>n</code> containing the participant labels</li> <li>• <code>block</code>: vector of size <code>n</code> containing the training blocks (longitudinal units)</li> <li>• <code>s</code>: vector of size <code>n</code> containing the stimuli</li> <li>• <code>d</code>: vector of size <code>n</code> containing the decisions</li> <li>• <code>r_time</code>: vector of size <code>n</code> containing the response times</li> <li>• <code>cens</code>: vector of size <code>n</code> containing the censoring indicators (1 censored, 0 non censored)</li> </ul> |
| <code>fit</code>  | fit from the <code>lddmm</code> function                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |
| <code>par</code>  | parameter to output ('drift', or 'boundary')                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |

**Value**

Matrix with the following columns:

- `subject`: participant labels
- `block`: training blocks
- `draw`: iteration of the MCMC estimates
- `par_s_d, ...`: posterior draws for the requested parameters

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|                                |                                  |
|--------------------------------|----------------------------------|
| <code>extract_post_mean</code> | <i>Parameter posterior means</i> |
|--------------------------------|----------------------------------|

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**Description**

Function to extract the posterior means of the parameters of interest from a `lddmm` fit object.

**Usage**

```
extract_post_mean(data, fit, par = c("drift", "boundary"))
```

**Arguments**

|                   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |
|-------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>data</code> | dataframe with the following columns: <ul style="list-style-type: none"> <li>• <code>subject</code>: vector of size <code>n</code> containing the participant labels</li> <li>• <code>block</code>: vector of size <code>n</code> containing the training blocks (longitudinal units)</li> <li>• <code>s</code>: vector of size <code>n</code> containing the stimuli</li> <li>• <code>d</code>: vector of size <code>n</code> containing the decisions</li> <li>• <code>r_time</code>: vector of size <code>n</code> containing the response times</li> <li>• <code>cens</code>: vector of size <code>n</code> containing the censoring indicators (1 censored, 0 non censored)</li> </ul> |
| <code>fit</code>  | fit from the <code>lddmm</code> function                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |
| <code>par</code>  | parameter to output ('drift', or 'boundary')                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |

**Value**

Matrix with the following columns:

- subject: participant labels
- block: training blocks
- par\_s\_d, ...: posterior means for the requested parameters

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|        |                     |
|--------|---------------------|
| H_ball | <i>Hamming Ball</i> |
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**Description**

Computes the Hamming Ball centered at x with radius r.

**Usage**

```
H_ball(x, S, r)
```

**Arguments**

|   |                            |
|---|----------------------------|
| x | center of the Hamming Ball |
| S | number of states           |
| r | radius of the Hamming Ball |

**Value**

Hamming Ball

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|       |                                  |
|-------|----------------------------------|
| LDDMM | <i>Drift Diffusion Model Fit</i> |
|-------|----------------------------------|

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**Description**

Main function for the Gibbs sampler for the drift-diffusion model. Note that priors are noninformative and calibrated so that, for the most stable performance, the response times (variable r\_time in the data dataframe) should lie between 0 and 10.

**Usage**

```
LDDMM(
  data,
  hypers,
  cluster = TRUE,
  boundaries = "flexible",
  Niter = 5000,
  burnin = 2000,
  thin = 5
)
```

**Arguments**

|            |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |
|------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| data       | dataframe with the following columns: <ul style="list-style-type: none"> <li>• subject: vector of size n containing the participant labels</li> <li>• block: vector of size n containing the training blocks (longitudinal units)</li> <li>• s: vector of size n containing the stimuli</li> <li>• d: vector of size n containing the decisions</li> <li>• r_time: vector of size n containing the response times. To avoid numerical issues, the unit of measurement should be such that the numerical values of most response times should lie between 0 and 10</li> <li>• cens: vector of size n containing the censoring indicators (1 censored, 0 non censored)</li> </ul> |
| hypers     | hyperparameters of the MCMC: list containing "s_sigma_mu" and "s_sigma_b", which are the smoothness parameters for drifts and boundaries, respectively)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |
| cluster    | should clustering be used? (default = TRUE)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
| boundaries | whether to fit the unrestricted model (flexible), assume constant boundaries over time (constant) or fix the boundaries to the same level across predictors (fixed)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |
| Niter      | total number of iterations                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |
| burnin     | burnin of the chain                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |
| thin       | thinning factor                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |

**Value**

List with the following MCMC posterior samples:

- post\_mean\_delta: posterior samples for the population offset parameters
- post\_mean\_mu: posterior samples for the population drift parameters
- post\_mean\_b: posterior samples for the population boundary parameters
- post\_ind\_delta: posterior samples for the individual offset parameters
- post\_ind\_mu: posterior samples for the individual drift parameters
- post\_ind\_b: posterior samples for the individual boundary parameters
- sigma2\_mu\_us: posterior samples for the random effects drift smoothness parameters
- sigma2\_mu\_ua: posterior samples for the random effects drift variance parameters
- sigma2\_b\_us: posterior samples for the random effects boundary smoothness parameters
- sigma2\_b\_ua: posterior samples for the random effects boundary variance parameters
- sigma2\_1\_mu: posterior samples for the drift smoothness parameters
- sigma2\_1\_b: posterior samples for the boundary smoothness parameters
- pred\_ans: predicted population-level categories
- pred\_time: predicted population-level response times
- pred\_ans\_ind: predicted individual-level categories
- pred\_time\_ind: predicted individual-level response times

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|                |                                   |
|----------------|-----------------------------------|
| log_likelihood | <i>Log-likelihood computation</i> |
|----------------|-----------------------------------|

---

**Description**

Compute the log-likelihood for the drift-diffusion model, including the censored data contribution.

**Usage**

```
log_likelihood(tau, mu, b, delta, cens, D, log)
```

**Arguments**

|       |                                                                                                                                |
|-------|--------------------------------------------------------------------------------------------------------------------------------|
| tau   | vector of size n containing the response times                                                                                 |
| mu    | matrix of size (n x d1) containing the drift parameters corresponding to the n response times for each possible d1 decision    |
| b     | matrix of size (n x d1) containing the boundary parameters corresponding to the n response times for each possible d1 decision |
| delta | vector of size n containing the offset parameters corresponding to the n response times                                        |
| cens  | vector of size n containing censoring indicators (1 censored, 0 not censored) corresponding to the n response times            |
| D     | (n x 2) matrix whose first column has the n input stimuli, and whose second column has the n decision categories               |
| log   | should the results be returned on the log scale?                                                                               |

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|                    |                                                            |
|--------------------|------------------------------------------------------------|
| log_likelihood_ind | <i>Log-likelihood computation for a single observation</i> |
|--------------------|------------------------------------------------------------|

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**Description**

Compute the log-likelihood for the drift-diffusion model, including the censored data contribution, for a single observation.

**Usage**

```
log_likelihood_ind(tau, mu, b, delta, cens, D)
```

Arguments

|       |                                                                                                                                |
|-------|--------------------------------------------------------------------------------------------------------------------------------|
| tau   | vector of size n containing the response times                                                                                 |
| mu    | matrix of size (n x d1) containing the drift parameters corresponding to the n response times for each possible d1 decision    |
| b     | matrix of size (n x d1) containing the boundary parameters corresponding to the n response times for each possible d1 decision |
| delta | vector of size n containing the offset parameters corresponding to the n response times                                        |
| cens  | vector of size n containing censoring indicators (1 censored, 0 not censored) corresponding to the n response times            |
| D     | (n x 2) matrix whose first column has the n input stimuli, and whose second column has the n decision categories               |

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|               |                          |
|---------------|--------------------------|
| plot_accuracy | <i>Descriptive plots</i> |
|---------------|--------------------------|

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Description

Plot the accuracy of the raw data.

Usage

plot\_accuracy(data)

Arguments

|      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |
|------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| data | dataframe with the following columns: <ul style="list-style-type: none"><li>• subject: vector of size n containing the participant labels</li><li>• block: vector of size n containing the training blocks (longitudinal units)</li><li>• s: vector of size n containing the stimuli</li><li>• d: vector of size n containing the decisions</li><li>• r_time: vector of size n containing the response times</li><li>• cens: vector of size n containing the censoring indicators (1 censored, 0 non censored)</li></ul> |
|------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

Value

Individual and population level raw accuracies

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|                |                                 |
|----------------|---------------------------------|
| plot_post_pars | <i>Plot posterior estimates</i> |
|----------------|---------------------------------|

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**Description**

Function to plot the posterior mean and credible intervals of the parameters of interest from a lddmm fit object.

**Usage**

```
plot_post_pars(data, fit, par = c("drift", "boundary"))
```

**Arguments**

|      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |
|------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| data | <p>dataframe with the following columns:</p> <ul style="list-style-type: none"> <li>• subject: vector of size n containing the participant labels</li> <li>• block: vector of size n containing the training blocks (longitudinal units)</li> <li>• s: vector of size n containing the stimuli</li> <li>• d: vector of size n containing the decisions</li> <li>• r_time: vector of size n containing the response times</li> <li>• cens: vector of size n containing the censoring indicators (1 censored, 0 non censored)</li> </ul> |
| fit  | fit from the lddmm function                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
| par  | parameter to output ('drift', or 'boundary')                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |

**Value**

Posterior mean and 95% CI

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|         |                          |
|---------|--------------------------|
| plot_RT | <i>Descriptive plots</i> |
|---------|--------------------------|

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**Description**

Plot the mean response times of the raw data.

**Usage**

```
plot_RT(data)
```

**Arguments**

data                      dataframe with the following columns:

- subject: vector of size n containing the participant labels
- block: vector of size n containing the training blocks (longitudinal units)
- s: vector of size n containing the stimuli
- d: vector of size n containing the decisions
- r\_time: vector of size n containing the response times
- cens: vector of size n containing the censoring indicators (1 censored, 0 non censored)

**Value**

Population level raw response times

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|           |                              |
|-----------|------------------------------|
| P_smooth1 | <i>Spline Penalty Matrix</i> |
|-----------|------------------------------|

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**Description**

Construct the covariance matrix P of the smoothness inducing prior for the spline coefficients

**Usage**

P\_smooth1(K)

**Arguments**

K                      Number of spline knots

**Value**

Covariance of the smoothness inducing prior (penalizing first differences in the spline coefficients)

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