# Package 'mcca'

July 22, 2025

Type Package

Title Multi-Category Classification Accuracy

Version 0.7.0

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**Description** It contains six common multi-category classification accuracy evaluation measures.

All of these measures could be found in Li and Ming (2019) <doi:10.1002/sim.8103>. Specifically,

Hypervolume Under Manifold (HUM), described in

Li and Fine (2008) <doi:10.1093/biostatistics/kxm050>.

Correct Classification Percentage (CCP), Integrated Discrimination Improvement (IDI), Net Reclassification Improvement (NRI), R-Squared Value (RSQ), described in

Li, Jiang and Fine (2013) <doi:10.1093/biostatistics/kxs047>.

Polytomous Discrimination Index (PDI), described in

Van Calster et al. (2012) <doi:10.1007/s10654-012-9733-3>.

Li et al. (2018) <doi:10.1177/0962280217692830>.

We described all these above measures and our mcca package in

Li, Gao and D'Agostino (2019) <doi:10.1002/sim.8103>.

License GPL

**Encoding UTF-8** 

LazyData true

Imports nnet,rpart,e1071,MASS,stats,pROC,caret,rgl

URL https://github.com/gaoming96/mcca

BugReports https://github.com/gaoming96/mcca/issues

NeedsCompilation no

Repository CRAN

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2 mcca-package

# **Contents**

mcca-	-package	Diagnostic accuracy methods for classifiers
dex		30
	rsq	2
	print.mcca.rsq	
	print.mcca.pdi	25
	print.mcca.hum	
	print.mcca.ccp	
	pm	
	plot.mcca.hum	
	pdi	
	nri	
	idi	
	hum	
	ests	
	estp	
	сср	
	mcca-package	

# Description

Index

Six common multi-category classification accuracy evaluation measures are included i.e., Correct Classification Percentage (CCP), Hypervolume Under Manifold (HUM), Integrated Discrimination Improvement (IDI), Net Reclassification Improvement (NRI), Polytomous Discrimination Index (PDI) and R-squared (RSQ). It allows users to fit many popular classification procedures, such as multinomial logistic regression, support vector machine, classification tree, and user computed risk values.

# **Details**

Package: mcca Type: Package Version: 0.6

Date: 2019-08-05 License: GPL

mcca-package 3

## **Functions**

Calculate CCP Value
Calculate HUM Value
Plot 3D ROC curve
Calculate IDI Value
Calculate NRI Value
Calculate PDI Value
Calculate RSQ Value
Calculate Probability Matrix
Estimated Information for Single Model Evaluation Value
Estimated Information for Paired Model Evaluation Value

# Installing and using

To install this package, make sure you are connected to the internet and issue the following command in the R prompt:

```
install.packages("mcca")
```

To load the package in R:

```
library(mcca)
```

## Citation

Li J, Gao M, D'Agostino R. Evaluating classification accuracy for modern learning approaches. Statistics in Medicine. 2019;1-27. https://doi.org/10.1002/sim.8103

# Author(s)

Ming Gao, Jialiang Li

Maintainer: Ming Gao <gaoming@umich.edu>

## References

- Li, J., Gao, M., D'Agostino, R. (2019). Evaluating Classification Accuracy for Modern Learning Approaches. Statistics in Medicine (Tutorials in Biostatistics). 38(13): 2477-2503.
- Li, Ming G., D'Agostino. (2019). Evaluating Classification Accuracy for Modern Learning Approaches. Statistics in Medicine.
- Li, J. and Fine, J. P. (2008): ROC analysis with multiple tests and multiple classes: methodology and applications in microarray studies. Biostatistics. 9 (3): 566-576.

4 mcca-package

Li, J., Chow, Y., Wong, W.K., and Wong, T.Y. (2014). Sorting Multiple Classes in Multi-dimensional ROC Analysis: Parametric and Nonparametric Approaches. Biomarkers. 19(1): 1-8.

Li, J., Jiang, B. and Fine, J. P. (2013). Multicategory reclassification statistics for assessing Improvements in diagnostic accuracy. Biostatistics. 14(2): 382-394.

Li, J., Jiang, B., and Fine, J. P. (2013). Letter to Editor: Response. Biostatistics. 14(4): 809-810.

Van Calster B, Vergouwe Y, Looman CWN, Van Belle V, Timmerman D and Steyerberg EW. Assessing the discriminative ability of risk models for more than two outcome categories. European Journal of Epidemiology 2012; 27: 761 C 770.

Li, J., Feng, Q., Fine, J.P., Pencina, M.J., Van Calster, B. (2018). Nonparametric estimation and inference for polytomous discrimination index. Statistical Methods in Medical Research. 27(10): 3092—3103.

#### See Also

CRAN packages HUM for HUM.

CRAN packages **nnet**, **rpart**, **e1071**, **MASS** employed in this package.

```
str(iris)
data <- iris[, 1:4]
label <- iris[, 5]</pre>
ccp(y = label, d = data, method = "multinom", maxit = 1000, MaxNWts = 2000, trace=FALSE)
ccp(y = label, d = data, method = "multinom")
ccp(y = label, d = data, method = "svm")
ccp(y = label, d = data, method = "svm",kernel="sigmoid",cost=4,scale=TRUE,coef0=0.5)
ccp(y = label, d = data, method = "tree")
p = as.numeric(label)
ccp(y = label, d = p, method = "label")
hum(y = label, d = data, method = "multinom")
hum(y = label, d = data,method = "svm")
hum(y = label, d = data,method = "svm",kernel="linear",cost=4,scale=TRUE)
hum(y = label, d = data, method = "tree")
ests(y = label, d = data,acc="hum",level=0.95,method = "multinom",trace=FALSE)
## $value
## [1] 0.9972
## $sd
## [1] 0.002051529
## $interval
## [1] 0.9935662 1.0000000
```

ccp 5

Calculate CCP Value

## **Description**

compute the Correct Classification Percentage (CCP) value of two or three or four categories classifiers with an option to define the specific model or user-defined model.

## Usage

```
ccp(y, d, method="multinom", ...)
```

## **Arguments**

y The multinomial response vector with two, three or four categories.

d The set of candidate markers, including one or more columns. Can be a data

frame or a matrix; if the method is "label", then d should be the label vector.

method Specifies what method is used to construct the classifier based on the marker

set in d. Available option includes the following methods: "multinom": Multinomial Logistic Regression which is the default method, requiring R package nnet; "tree": Classification Tree method, requiring R package rpart; "svm": Support Vector Machine (C-classification and radial basis as default), requiring R package e1071; "lda": Linear Discriminant Analysis, requiring R package lda; "label": d is a label vector resulted from any external classification algorithm obtained by the user, should be encoded from 1; "prob": d is a probability matrix

resulted from any external classification algorithm obtained by the user.

. . . Additional arguments in the chosen method's function.

# **Details**

The function returns the CCP value for predictive markers based on a user-chosen machine learning method. Currently available methods include logistic regression (default), tree, lda, svm and user-computed risk values. This function is general since we can evaluate the accuracy for marker combinations resulted from complicated classification algorithms.

#### Value

Returns an object of class "mcca.ccp". The CCP value of the classification using a particular learning method on a set of marker(s).

An object of class "mcca.ccp" is a list containing at least the following components:

call the matched call.

measure the value of measure.

table the category-specific value of measure.

6 ccp

#### Note

Users are advised to change the operating settings of various classifiers since it is well known that machine learning methods require extensive tuning. Currently only some common and intuitive options are set as default and they are by no means the optimal parameterization for a particular data analysis. Users can put machine learning methods' parameters after tuning. A more flexible evaluation is to consider "method=label" in which case the input d should be a label vector.

## Author(s)

```
Ming Gao: gaoming@umich.edu
Jialiang Li: stalj@nus.edu.sg
```

#### References

Li, J., Gao, M., D'Agostino, R. (2019). Evaluating Classification Accuracy for Modern Learning Approaches. Statistics in Medicine (Tutorials in Biostatistics). 38(13): 2477-2503.

Li, J., Jiang, B. and Fine, J. P. (2013). Multicategory reclassification statistics for assessing Improvements in diagnostic accuracy. Biostatistics. 14(2): 382-394.

Li, J., Jiang, B., and Fine, J. P. (2013). Letter to Editor: Response. Biostatistics. 14(4): 809-810.

#### See Also

pdi

```
str(iris)
data <- iris[, 1:4]
label <- iris[, 5]</pre>
ccp(y = label, d = data, method = "multinom", maxit = 1000, MaxNWts = 2000, trace=FALSE)
## ccp(y = label, d = data, method = "multinom", maxit = 1000,
       MaxNWts = 2000, trace = FALSE)
## Overall Correct Classification Probability:
  0.9866667
## Category-specific Correct Classification Probability:
   CATEGORIES VALUES PREVALENCE
## 1
        setosa 1.00 0.3333333
## 2 versicolor
                 0.98 0.3333333
## 3 virginica 0.98 0.3333333
ccp(y = label, d = data, method = "multinom")
ccp(y = label, d = data, method = "svm")
ccp(y = label, d = data, method = "svm",kernel="sigmoid",cost=4,scale=TRUE,coef0=0.5)
ccp(y = label, d = data, method = "tree")
p = as.numeric(label)
```

estp 7

```
ccp(y = label, d = p, method = "label")
table(mtcars$carb)
for (i in (1:length(mtcars$carb))) {
 if (mtcars$carb[i] == 3 | mtcars$carb[i] == 6 | mtcars$carb[i] == 8) {
    mtcars$carb_new[i] = 9
 }else{
    mtcars$carb_new[i] = mtcars$carb[i]
 }
}
data <- data.matrix(mtcars[, c(1)])</pre>
mtcars$carb_new <- factor(mtcars$carb_new)</pre>
label <- mtcars$carb_new</pre>
str(mtcars)
ccp(y = as.numeric(label), d = data, method = "svm",kernel="radial",cost=1,scale=TRUE)
## ccp(y = as.numeric(label), d = data, method = "svm", kernel = "radial", cost = 1, scale = TRUE)
## Overall Correct Classification Probability:
   0.4375
## Category-specific Correct Classification Probability:
    CATEGORIES
                   VALUES PREVALENCE
##
## 1
              1 0.5714286
                              0.21875
## 2
              2 0.2000000
                              0.31250
## 3
              3 0.8000000
                              0.31250
## 4
              4 0.0000000
                              0.15625
```

estp

Inference for Accuracy Improvement Measures based on Bootstrap

# Description

compute the bootstrap standard error and confidence interval for the classification accuracy improvement for a pair of nested models.

## Usage

```
estp(y, m1, m2, acc="idi", level=0.95, method="multinom", B=250, balance=FALSE, ...)
```

#### **Arguments**

m1

y The multinomial response vector with two, three or four categories. It can be factor or integer-valued.

The set of marker(s) included in the baseline model, can be a data frame or a matrix; if the method is "prob", then m1 should be the prediction probablity matrix of the baseline model.

8 estp

m2 The set of additional marker(s) included in the improved model, can be a data

frame or a matrix; if the method is "prob", then m2 should be the prediction

probablity matrix of the improved model.

acc Accuracy measure to be evaluated. Allow two choices: "idi", "nri".

level The confidence level. Default value is 0.95.

method Specifies what method is used to construct the classifier based on the marker

set in m1 & m2. Available option includes the following methods: "multinom": Multinomial Logistic Regression which is the default method, requiring R package nnet; "tree": Classification Tree method, requiring R package rpart; "svm": Support Vector Machine (C-classification and radial basis as default), requiring R package e1071; "lda": Linear Discriminant Analysis, requiring R package lda; "prob": m1 & m2 are risk matrices resulted from any external classification

algorithm obtained by the user.

B Number of bootstrap resamples.

balance Logical, if TRUE, the class prevalence of the bootstrap sample is forced to be

identical to the class prevalence of the original sample. Otherwise the prevalence

of the bootstrap sample may be random.

... Additional arguments in the chosen method's function.

#### **Details**

The function returns the standard error and confidence interval for a paired model evaluation method. All the other arguments are the same as the function hum.

## Value

value The specific value of the classification using a particular learning method on a

set of marker(s).

se The standard error of the value.
interval The confidence interval of the value.

## Note

Users are advised to change the operating settings of various classifiers since it is well known that machine learning methods require extensive tuning. Currently only some common and intuitive options are set as default and they are by no means the optimal parameterization for a particular data analysis. Users can put machine learning methods' parameters after tuning. A more flexible evaluation is to consider "method=prob" in which case the input m1 & m2 should be a matrix of membership probabilities with k columns and each row of m1 & m2 should sum to one.

# Author(s)

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## See Also

ests

ests 9

## **Examples**

```
table(mtcars$carb)
for (i in (1:length(mtcars$carb))) {
  if (mtcars$carb[i] == 3 | mtcars$carb[i] == 6 | mtcars$carb[i] == 8) {
    mtcars$carb_new[i] = 9
    mtcars$carb_new[i] = mtcars$carb[i]
  }
}
data <- data.matrix(mtcars[, c(1,2)])</pre>
mtcars$carb_new <- factor(mtcars$carb_new)</pre>
label <- mtcars$carb_new</pre>
str(mtcars)
estp(y = label, m1 = data[, 1], m2 = data[, 2], acc="idi",method="lda", B=10)
## $value
## [1] 0.1235644
## $se
## [1] 0.07053541
## $interval
## [1] 0.05298885 0.21915088
estp(y = label, m1 = data[, 1], m2 = data[, 2], acc="nri",method="tree",B=5)
## $value
## [1] 0.05
## $se
## [1] 0.09249111
## $interval
## [1] 0.0000000 0.1458333
```

ests

Inference for Accuracy Measures based on Bootstrap

## **Description**

compute the bootstrap standard error and confidence interval for the classification accuracy for a single classification model.

# Usage

```
ests(y, d, acc="hum", level=0.95, method="multinom", B=250, balance=FALSE, ...)
```

10 ests

#### **Arguments**

y The multinomial response vector with two, three or four categories. It can be

factor or integer-valued.

d The set of candidate markers, including one or more columns. Can be a data

frame or a matrix; if the method is "prob", then d should be the probability

matrix.

acc Accuracy measure to be evaluated. Allow four choices: "hum", "pdi", "ccp" and

"rsq".

level The confidence level. Default value is 0.95.

method Specifies what method is used to construct the classifier based on the marker

set in d. Available option includes the following methods: "multinom": Multinomial Logistic Regression which is the default method, requiring R package nnet; "tree": Classification Tree method, requiring R package rpart; "svm": Support Vector Machine (C-classification and radial basis as default), requiring R package e1071; "lda": Linear Discriminant Analysis, requiring R package lda; "label": d is a label vector resulted from any external classification algorithm obtained by the user, should be encoded from 1; "prob": d is a probability matrix

resulted from any external classification algorithm obtained by the user.

B Number of bootstrap resamples.

balance Logical, if TRUE, the class prevalence of the bootstrap sample is forced to be

identical to the class prevalence of the original sample. Otherwise the prevalence

of the bootstrap sample may be random.

... Additional arguments in the chosen method's function.

## **Details**

The function returns the standard error and confidence interval for a single model evaluation method. All the other arguments are the same as the function hum.

#### Value

value The specific value of the classification using a particular learning method on a

set of marker(s).

se The standard error of the value.

interval The confidence interval of the value.

#### Note

Users are advised to change the operating settings of various classifiers since it is well known that machine learning methods require extensive tuning. Currently only some common and intuitive options are set as default and they are by no means the optimal parameterization for a particular data analysis. Users can put machine learning methods' parameters after tuning. A more flexible evaluation is to consider "method=prob" in which case the input d should be a matrix of membership probabilities with k columns and each row of d should sum to one.

ests 11

## Author(s)

Ming Gao: gaoming@umich.edu Jialiang Li: stalj@nus.edu.sg

# See Also

estp

```
str(iris)
data <- iris[, 1:4]
label <- iris[, 5]</pre>
ests(y = label, d = data,acc="hum",level=0.95,method = "multinom",B=10,trace=FALSE)
## $value
## [1] 0.9972
## $se
## [1] 0.002051529
## $interval
## [1] 0.9935662 1.0000000
ests(y = label, d = data,acc="pdi",level=0.85,method = "tree",B=10)
## $value
## [1] 0.9213333
## $se
## [1] 0.02148812
## $interval
## [1] 0.9019608 0.9629630
table(mtcars$carb)
for (i in (1:length(mtcars$carb))) {
  if (mtcars$carb[i] == 3 | mtcars$carb[i] == 6 | mtcars$carb[i] == 8) {
    mtcars$carb_new[i] = 9
  }else{
    mtcars$carb_new[i] = mtcars$carb[i]
  }
}
data <- data.matrix(mtcars[, c(1:2)])</pre>
mtcars$carb_new <- factor(mtcars$carb_new)</pre>
label <- mtcars$carb_new</pre>
str(mtcars)
ests(y = label, d = data,acc="hum",level=0.95,method = "multinom",trace=FALSE,B=5)
## $value
## [1] 0.2822857
```

12 hum

```
## $se
## [1] 0.170327
## $interval
## [1] 0.2662500 0.4494643
```

hum

Calculate HUM Value

# **Description**

compute the Hypervolume Under Manifold (HUM) value of two or three or four categories classifiers with an option to define the specific model or user-defined model.

## Usage

```
hum(y, d, method="multinom", ...)
```

## Arguments

y The multinomial response vector with two, three or four categories. It can be

factor or integer-valued.

d The set of candidate markers, including one or more columns. Can be a data

frame or a matrix; if the method is "prob", then d should be the probablity ma-

trix.

method Specifies what method is used to construct the classifier based on the marker

set in d. Available option includes the following methods:"multinom": Multinomial Logistic Regression which is the default method, requiring R package nnet;"tree": Classification Tree method, requiring R package rpart; "svm": Support Vector Machine (C-classification and radial basis as default), requiring R package e1071;"lda": Linear Discriminant Analysis, requiring R package lda; "prob": d is a risk matrix resulted from any external classification algorithm

obtained by the user.

... Additional arguments in the chosen method's function.

## Details

The function returns the HUM value for predictive markers based on a user-chosen machine learning method. Currently available methods include logistic regression (default), tree, lda, svm and user-computed risk values. For binary outcome, one can use AUC value (HUM reduces to AUC in such case). This function is more general than the package HUM, since we can evaluate the accuracy for marker combinations resulted from complicated classification algorithms.

## Value

The HUM value of the classification using a particular learning method on a set of marker(s).

hum 13

#### Note

Users are advised to change the operating settings of various classifiers since it is well known that machine learning methods require extensive tuning. Currently only some common and intuitive options are set as default and they are by no means the optimal parameterization for a particular data analysis. Users can put machine learning methods' parameters after tuning. A more flexible evaluation is to consider "method=prob" in which case the input d should be a matrix of membership probabilities with k columns and each row of d should sum to one.

## Author(s)

Ming Gao: gaoming@umich.edu Jialiang Li: stalj@nus.edu.sg

#### References

Li, J., Gao, M., D'Agostino, R. (2019). Evaluating Classification Accuracy for Modern Learning Approaches. Statistics in Medicine (Tutorials in Biostatistics). 38(13): 2477-2503.

Li, J. and Fine, J. P. (2008): ROC analysis with multiple tests and multiple classes: methodology and applications in microarray studies. Biostatistics. 9 (3): 566-576.

Li, J., Chow, Y., Wong, W.K., and Wong, T.Y. (2014). Sorting Multiple Classes in Multi-dimensional ROC Analysis: Parametric and Nonparametric Approaches. Biomarkers. 19(1): 1-8.

## See Also

pdi

```
str(iris)
data <- iris[, 1:4]
label <- iris[, 5]</pre>
hum(y = label, d = data,method = "multinom")
## [1] 0.9972
hum(y = label, d = data,method = "svm")
## [1] 0.9964
hum(y = label, d = data,method = "svm",type="C",kernel="linear",cost=4,scale=TRUE)
## [1] 0.9972
hum(y = label, d = data, method = "tree")
## [1] 0.998
data <- data.matrix(iris[, 1:4])</pre>
label <- as.numeric(iris[, 5])</pre>
# multinomial
require(nnet)
# model
fit <- multinom(label ~ data, maxit = 1000, MaxNWts = 2000)
predict.probs <- predict(fit, type = "probs")</pre>
pp<- data.frame(predict.probs)</pre>
# extract the probablity assessment vector
head(pp)
```

14 idi

```
hum(y = label, d = pp, method = "prob")
## [1] 0.9972
table(mtcars$carb)
for (i in (1:length(mtcars$carb))) {
  if (mtcars$carb[i] == 3 | mtcars$carb[i] == 6 | mtcars$carb[i] == 8) {
    mtcars$carb_new[i] = 9
    mtcars$carb_new[i] = mtcars$carb[i]
  }
}
data <- data.matrix(mtcars[, c(1:10)])</pre>
mtcars$carb_new <- factor(mtcars$carb_new)</pre>
label <- mtcars$carb_new</pre>
str(mtcars)
hum(y = label, d = data, method = "tree",control = rpart::rpart.control(minsplit = 5))
## [1] 1
hum(y = label, d = data, method = "svm",kernel="linear",cost=0.7,scale=TRUE)
hum(y = label, d = data, method = "svm", kernel ="radial",cost=0.7,scale=TRUE)
## [1] 0.53
```

idi

Calculate IDI Value

## **Description**

compute the integrated discrimination improvement (IDI) value of two or three or four categories classifiers with an option to define the specific model or user-defined model.

# Usage

```
idi(y, m1, m2, method="multinom", ...)
```

## Arguments

У	The multinomial response vector with two, three or four categories. It can be factor or integer-valued.
m1	The set of marker(s) included in the baseline model, can be a data frame or a matrix; if the method is "prob", then m1 should be the prediction probablity matrix of the baseline model.
m2	The set of additional marker(s) included in the improved model, can be a data frame or a matrix; if the method is "prob", then m2 should be the prediction probablity matrix of the improved model.
method	Specifies what method is used to construct the classifier based on the marker set in m1 & m2. Available option includes the following methods:"multinom":

idi 15

Multinomial Logistic Regression which is the default method, requiring R package nnet;"tree": Classification Tree method, requiring R package rpart; "svm": Support Vector Machine (C-classification and radial basis as default), requiring R package e1071;"lda": Linear Discriminant Analysis, requiring R package lda; "prob": m1 & m2 are risk matrices resulted from any external classification algorithm obtained by the user.

. . . Additional arguments in the chosen method's function.

#### **Details**

The function returns the IDI value for predictive markers based on a user-chosen machine learning method. Currently available methods include logistic regression (default), tree, lda, svm and user-computed risk values. This function is general since we can evaluate the accuracy for marker combinations resulted from complicated classification algorithms.

#### Value

The IDI value of the classification using a particular learning method on a set of marker(s).

#### Note

Users are advised to change the operating settings of various classifiers since it is well known that machine learning methods require extensive tuning. Currently only some common and intuitive options are set as default and they are by no means the optimal parameterization for a particular data analysis. Users can put machine learning methods' parameters after tuning. A more flexible evaluation is to consider "method=prob" in which case the input m1 & m2 should be a matrix of membership probabilities with k columns and each row of m1 & m2 should sum to one.

## Author(s)

Ming Gao: gaoming@umich.edu Jialiang Li: stalj@nus.edu.sg

## References

Li, J., Gao, M., D'Agostino, R. (2019). Evaluating Classification Accuracy for Modern Learning Approaches. Statistics in Medicine (Tutorials in Biostatistics). 38(13): 2477-2503.

Li, J., Jiang, B. and Fine, J. P. (2013). Multicategory reclassification statistics for assessing Improvements in diagnostic accuracy. Biostatistics. 14(2): 382—394.

Li, J., Jiang, B., and Fine, J. P. (2013). Letter to Editor: Response. Biostatistics. 14(4): 809-810.

#### See Also

nri

nri

## **Examples**

```
table(mtcars$carb)
for (i in (1:length(mtcars$carb))) {
    if (mtcars$carb[i] == 3 | mtcars$carb[i] == 6 | mtcars$carb[i] == 8) {
        mtcars$carb_new[i] = 9
    }else{
        mtcars$carb_new[i] = mtcars$carb[i]
    }
}
data <- data.matrix(mtcars[, c(1,5)])
mtcars$carb_new <- factor(mtcars$carb_new)
label <- mtcars$carb_new
str(mtcars)

idi(y = label, m1 = data[, 1], m2 = data[, 2], "tree")
## [1] 0.09979413
idi(y = label, m1 = data[, 1], m2 = data[, 2], "tree",control=rpart::rpart.control(minsplit=4))
## [1] 0.2216707</pre>
```

nri

Calculate NRI Value

## **Description**

compute the net reclassification improvement (NRI) value of two or three or four categories classifiers with an option to define the specific model or user-defined model.

## Usage

```
nri(y, m1, m2, method="multinom", ...)
```

## **Arguments**

m1

m2

method

y The multinomial response vector with two, three or four categories. It can be factor or integer-valued.

The set of marker(s) included in the baseline model, can be a data frame or a matrix; if the method is "prob", then m1 should be the prediction probablity matrix of the baseline model.

The set of additional marker(s) included in the improved model, can be a data frame or a matrix; if the method is "prob", then m2 should be the prediction probablity matrix of the improved model.

Specifies what method is used to construct the classifier based on the marker set in m1 & m2. Available option includes the following methods: "multinom": Multinomial Logistic Regression which is the default method, requiring R package nnet; "tree": Classification Tree method, requiring R package rpart; "svm": Support Vector Machine (C-classification and radial basis as default), requiring R package e1071; "lda": Linear Discriminant Analysis, requiring R package

nri 17

lda;"label": m1 & m2 are label vectors resulted from any external classification algorithm obtained by the user;"prob": m1 & m2 are probability matrices resulted from any external classification algorithm obtained by the user.

Additional arguments in the chosen method's function.

#### **Details**

The function returns the NRI value for predictive markers based on a user-chosen machine learning method. Currently available methods include logistic regression (default), tree, lda, svm and user-computed risk values. This function is general since we can evaluate the accuracy for marker combinations resulted from complicated classification algorithms.

#### Value

The NRI value of the classification using a particular learning method on a set of marker(s).

#### Note

Users are advised to change the operating settings of various classifiers since it is well known that machine learning methods require extensive tuning. Currently only some common and intuitive options are set as default and they are by no means the optimal parameterization for a particular data analysis. Users can put machine learning methods' parameters after tuning. A more flexible evaluation is to consider "method=prob" in which case the input m1 & m2 should be a matrix of membership probabilities with k columns and each row of m1 & m2 should sum to one.

#### Author(s)

```
Ming Gao: gaoming@umich.edu
Jialiang Li: stalj@nus.edu.sg
```

#### References

Li, J., Gao, M., D'Agostino, R. (2019). Evaluating Classification Accuracy for Modern Learning Approaches. Statistics in Medicine (Tutorials in Biostatistics). 38(13): 2477-2503.

Li, J., Jiang, B. and Fine, J. P. (2013). Multicategory reclassification statistics for assessing Improvements in diagnostic accuracy. Biostatistics. 14(2): 382—394.

Li, J., Jiang, B., and Fine, J. P. (2013). Letter to Editor: Response. Biostatistics. 14(4): 809-810.

#### See Also

idi

```
table(mtcars$carb)
for (i in (1:length(mtcars$carb))) {
  if (mtcars$carb[i] == 3 | mtcars$carb[i] == 6 | mtcars$carb[i] == 8) {
    mtcars$carb_new[i] = 9
  }else{
```

18 pdi

```
mtcars$carb_new[i] = mtcars$carb[i]
}

data <- data.matrix(mtcars[, c(1,5)])
mtcars$carb_new <- factor(mtcars$carb_new)
label <- mtcars$carb_new
str(mtcars)

nri(y = label, m1 = data[, 1], m2 = data[, 2], "lda")
## [1] 0.09375
nri(y = label, m1 = data[, 1], m2 = data[, 2], "tree")
## [1] 0.0625
nri(y = label, m1 = data[, 1], m2 = data[, 2], "tree",control=rpart::rpart.control(minsplit=4))
## [1] 0.1875</pre>
```

pdi

Calculate PDI Value

## **Description**

compute the Polytomous Discrimination Index (PDI) value of two or three or four categories classifiers with an option to define the specific model or user-defined model.

# Usage

```
pdi(y, d, method="multinom", ...)
```

#### **Arguments**

d

y The multinomial response vector with two, three or four categories. It can be factor or integer-valued.

The set of candidate markers, including one or more columns. Can be a data

trix.

method Specifies what method is used to construct the classifier based on the marker

set in d. Available option includes the following methods: "multinom": Multinomial Logistic Regression which is the default method, requiring R package nnet; "tree": Classification Tree method, requiring R package rpart; "svm": Support Vector Machine (C-classification and radial basis as default), requiring R package e1071; "Ida": Linear Discriminant Analysis, requiring R package lda; "prob": d is a risk matrix resulted from any external classification algorithm

frame or a matrix; if the method is "prob", then d should be the probablity ma-

obtained by the user.

. Additional arguments in the chosen method's function.

pdi 19

#### **Details**

The function returns the PDI value for predictive markers based on a user-chosen machine learning method. Currently available methods include logistic regression (default), tree, lda, svm and user-computed risk values. This function is general since we can evaluate the accuracy for marker combinations resulted from complicated classification algorithms.

#### Value

Returns an object of class "mcca.pdi". The PDI value of the classification using a particular learning method on a set of marker(s).

An object of class "mcca.pdi" is a list containing at least the following components:

call the matched call.

measure the value of measure.

table the category-specific value of measure.

#### Note

Users are advised to change the operating settings of various classifiers since it is well known that machine learning methods require extensive tuning. Currently only some common and intuitive options are set as default and they are by no means the optimal parameterization for a particular data analysis. Users can put machine learning methods' parameters after tuning. A more flexible evaluation is to consider "method=prob" in which case the input d should be a matrix of membership probabilities with k columns and each row of d should sum to one.

## Author(s)

Ming Gao: gaoming@umich.edu

Jialiang Li: stalj@nus.edu.sg

#### References

Li, J., Gao, M., D'Agostino, R. (2019). Evaluating Classification Accuracy for Modern Learning Approaches. Statistics in Medicine (Tutorials in Biostatistics). 38(13): 2477-2503.

Van Calster B, Vergouwe Y, Looman CWN, Van Belle V, Timmerman D and Steyerberg EW. Assessing the discriminative ability of risk models for more than two outcome categories. European Journal of Epidemiology 2012; 27: 761 C 770.

Li, J., Feng, Q., Fine, J.P., Pencina, M.J., Van Calster, B. (2018). Nonparametric estimation and inference for polytomous discrimination index. Statistical Methods in Medical Research. 27(10): 3092—3103.

#### See Also

hum

20 plot.mcca.hum

## **Examples**

```
str(iris)
data <- iris[, 3]</pre>
label <- iris[, 5]</pre>
pdi(y = label, d = data,method = "multinom")
## Call:
## pdi(y = label, d = data, method = "multinom")
## Overall Polytomous Discrimination Index:
## 0.9845333
## Category-specific Polytomous Discrimination Index:
##
   CATEGORIES VALUES
## 1
              1 1.0000
              2 0.9768
## 2
## 3
              3 0.9768
pdi(y = label, d = data,method = "tree")
pdi(y = label, d = data,method = "tree",control = rpart::rpart.control(minsplit = 200))
data <- data.matrix(iris[, 3])</pre>
label <- as.numeric(iris[, 5])</pre>
# multinomial
require(nnet)
# model
fit <- multinom(label ~ data, maxit = 1000, MaxNWts = 2000)</pre>
predict.probs <- predict(fit, type = "probs")</pre>
pp<- data.frame(predict.probs)</pre>
# extract the probablity assessment vector
head(pp)
pdi(y = label, d = pp, method = "prob")
```

plot.mcca.hum

Plot 3D ROC surface

# **Description**

plot the 3D ROC surface for a three-category classifier using the 3-dimensional point coordinates, computed by obj which is a mcca.hum class.

## Usage

```
## S3 method for class 'mcca.hum'
plot(x,labs=levels(x$y),coords=1:3,nticks=5,filename='fig.png',cex=0.7, ...)
```

plot.mcca.hum 21

# **Arguments**

X	An mcca.hum class object, containing probability matrix and labels.
labs	The label names of three coordinates. Default is 'levels(x\$y)'.
coords	The coordinates markers. Default is ' $c(1,2,3)$ ', which means labs[1] is the x-axis (class 1), labs[2] is the z-axis (class 3) and labs[3] is the y-axis (class 2).
nticks	Suggested number of ticks.
filename	Filename to save snapshot.
cex	Size for text.
	further arguments to 'plot.default'.

#### **Details**

This function is to plot the 3D ROC surface according to the correct classification probabilities for the three categories, resulted from any statistical or machine learning methods. This function complements the HUM package which can only plot 3D ROC surface for a single diagnostic test or biomarker for three classes.

#### Value

The function doesn't return any value.

## Author(s)

```
Ming Gao: gaoming@umich.edu
Jialiang Li: stalj@nus.edu.sg
```

## References

Li, J., and Zhou, X. H. (2009). Nonparametric and semiparametric estimation of the three way receiver operating characteristic surface. Journal of Statistical Planning and Inference. 139: 4133—4142.

Li, J., Gao, M., D'Agostino, R. (2019). Evaluating Classification Accuracy for Modern Learning Approaches. Statistics in Medicine (Tutorials in Biostatistics). 38(13): 2477-2503.

```
data <- iris[, 1]
label <- iris[, 5]
a=hum(y = label, d = data,method = "multinom")
#plot(a,filename='fig.png')</pre>
```

22 pm

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Calculate Probability Matrix

#### **Description**

compute the probability matrix of two or three or four categories classifiers with an option to define the specific model or user-defined model.

# Usage

```
pm(y, d, method="multinom", ...)
```

## **Arguments**

C	
У	The multinomial response vector with two, three or four categories. It can be factor or integer-valued.
d	The set of candidate markers, including one or more columns. Can be a data frame or a matrix.
method	Specifies what method is used to construct the classifier based on the marker set in d. Available option includes the following methods:"multinom": Multinomial Logistic Regression which is the default method, requiring R package nnet; "tree": Classification Tree method, requiring R package rpart; "svm": Support Vector Machine (C-classification and radial basis as default), requiring R package e1071; "lda": Linear Discriminant Analysis, requiring R package lda.
	Additional arguments in the chosen method's function.

# **Details**

The function returns the probability matrix for predictive markers based on a user-chosen machine learning method. Currently available methods include logistic regression (default), tree, lda, svm and user-computed risk values.

## Value

The probability matrix of the classification using a particular learning method on a set of marker(s).

# Author(s)

```
Ming Gao: gaoming@umich.edu
Jialiang Li: stalj@nus.edu.sg
```

## References

Li, J. and Fine, J. P. (2008): ROC analysis with multiple tests and multiple classes: methodology and applications in microarray studies. Biostatistics. 9 (3): 566-576.

Li, J., Chow, Y., Wong, W.K., and Wong, T.Y. (2014). Sorting Multiple Classes in Multi-dimensional ROC Analysis: Parametric and Nonparametric Approaches. Biomarkers. 19(1): 1-8.

print.mcca.ccp 23

## See Also

pdi

## **Examples**

```
str(iris)
data <- iris[, 1:4]
label <- iris[, 5]
pm(y = label, d = data,method = "multinom")</pre>
```

print.mcca.ccp

Print Method for mcca ccp class

# Description

An S3 method for the print generic. It is designed for a quick look at CCP values.

## Usage

```
## S3 method for class 'mcca.ccp'
print(x, ...)
```

## **Arguments**

x object of class 'mcca.ccp'.

... further arguments to 'print.default'.

## Value

An object of class "mcca.ccp" is a list containing at least the following components:

call the matched call.
measure the value of measure.

table the category-specific value of measure.

# Author(s)

Ming Gao: gaoming@umich.edu Jialiang Li: stalj@nus.edu.sg

## References

Li, J., Jiang, B. and Fine, J. P. (2013). Multicategory reclassification statistics for assessing Improvements in diagnostic accuracy. Biostatistics. 14(2): 382-394.

24 print.mcca.hum

## **Examples**

```
data = iris[, 1:4]
label = iris[, 5]
ccp_object=ccp(y = label, d = data, method = "multinom", maxit = 1000, MaxNWts = 2000, trace=FALSE)
print(ccp_object)
```

print.mcca.hum

Print Method for mcca hum class

## **Description**

An S3 method for the print generic. It is designed for a quick look at hum values.

## Usage

```
## S3 method for class 'mcca.hum'
print(x, ...)
```

# Arguments

x object of class 'mcca.hum'.

... further arguments to 'print.default'.

## Value

An object of class "mcca.hum" is a list containing at least the following components:

call the matched call.

measure the value of measure.

table the category-specific value of measure.

## Author(s)

Ming Gao: gaoming@umich.edu Jialiang Li: stalj@nus.edu.sg

## References

Li, J., Jiang, B. and Fine, J. P. (2013). Multicategory reclassification statistics for assessing Improvements in diagnostic accuracy. Biostatistics. 14(2): 382-394.

print.mcca.pdi 25

## **Examples**

```
data = iris[, 1:4]
label = iris[, 5]
hum_object=hum(y = label, d = data, method = "multinom", maxit = 1000, MaxNWts = 2000, trace=FALSE)
print(hum_object)
```

print.mcca.pdi

Print Method for mcca pdi class

## **Description**

An S3 method for the print generic. It is designed for a quick look at pdi values.

# Usage

```
## S3 method for class 'mcca.pdi'
print(x, ...)
```

## **Arguments**

x object of class 'mcca.pdi'.

... further arguments to 'print.default'.

## Value

An object of class "mcca.pdi" is a list containing at least the following components:

call the matched call.

measure the value of measure.

table the category-specific value of measure.

# Author(s)

Ming Gao: gaoming@umich.edu Jialiang Li: stalj@nus.edu.sg

## References

Li, J., Jiang, B. and Fine, J. P. (2013). Multicategory reclassification statistics for assessing Improvements in diagnostic accuracy. Biostatistics. 14(2): 382-394.

print.mcca.rsq

## **Examples**

```
data = iris[, 1:4]
label = iris[, 5]
pdi_object=pdi(y = label, d = data, method = "multinom", maxit = 1000, MaxNWts = 2000, trace=FALSE)
print(pdi_object)
```

print.mcca.rsq

Print Method for mcca rsq class

## **Description**

An S3 method for the print generic. It is designed for a quick look at rsq values.

# Usage

```
## S3 method for class 'mcca.rsq'
print(x, ...)
```

## **Arguments**

x object of class 'mcca.rsq'.

... further arguments to 'print.default'.

## Value

An object of class "mcca.rsq" is a list containing at least the following components:

call the matched call.

measure the value of measure.

table the category-specific value of measure.

## Author(s)

```
Ming Gao: gaoming@umich.edu
Jialiang Li: stalj@nus.edu.sg
```

## References

Li, J., Jiang, B. and Fine, J. P. (2013). Multicategory reclassification statistics for assessing Improvements in diagnostic accuracy. Biostatistics. 14(2): 382-394.

27 rsq

## **Examples**

```
data = iris[, 1:4]
label = iris[, 5]
rsq_object=rsq(y = label, d = data, method = "multinom", maxit = 1000, MaxNWts = 2000, trace=FALSE)
print(rsq_object)
```

rsq

Calculate RSQ Value

## **Description**

compute the R-squared (RSQ) value of two or three or four categories classifiers with an option to define the specific model or user-defined model.

## Usage

```
rsq(y, d, method="multinom", ...)
```

## **Arguments**

The multinomial response vector with two, three or four categories. It can be у

factor or integer-valued.

d The set of candidate markers, including one or more columns. Can be a data

frame or a matrix; if the method is "prob", then d should be the probablity ma-

trix.

method Specifies what method is used to construct the classifier based on the marker

> set in d. Available option includes the following methods:"multinom": Multinomial Logistic Regression which is the default method, requiring R package nnet;"tree": Classification Tree method, requiring R package rpart;"svm": Support Vector Machine (C-classification and radial basis as default), requiring R package e1071;"lda": Linear Discriminant Analysis, requiring R package lda; "prob": d is a risk matrix resulted from any external classification algorithm

obtained by the user.

Additional arguments in the chosen method's function.

# **Details**

The function returns the RSQ value for predictive markers based on a user-chosen machine learning method. Currently available methods include logistic regression (default), tree, lda, svm and usercomputed risk values. This function is general since we can evaluate the accuracy for marker combinations resulted from complicated classification algorithms.

28 rsq

#### Value

Returns an object of class "mcca.rsq". The RSQ value of the classification using a particular learning method on a set of marker(s).

An object of class "mcca.rsq" is a list containing at least the following components:

call the matched call.
measure the value of measure.

table the category-specific value of measure.

## Note

Users are advised to change the operating settings of various classifiers since it is well known that machine learning methods require extensive tuning. Currently only some common and intuitive options are set as default and they are by no means the optimal parameterization for a particular data analysis. Users can put machine learning methods' parameters after tuning. A more flexible evaluation is to consider "method=prob" in which case the input d should be a matrix of membership probabilities with k columns and each row of d should sum to one.

## Author(s)

Ming Gao: gaoming@umich.edu Jialiang Li: stalj@nus.edu.sg

#### References

Li, J., Gao, M., D'Agostino, R. (2019). Evaluating Classification Accuracy for Modern Learning Approaches. Statistics in Medicine (Tutorials in Biostatistics). 38(13): 2477-2503.

Li, J., Jiang, B. and Fine, J. P. (2013). Multicategory reclassification statistics for assessing Improvements in diagnostic accuracy. Biostatistics. 14(2): 382-394.

Li, J., Jiang, B., and Fine, J. P. (2013). Letter to Editor: Response. Biostatistics. 14(4): 809-810.

## See Also

сср

```
str(iris)
data <- iris[, 1:4]
label <- iris[, 5]
rsq(y = label, d = data, method="multinom")
## Call:
## rsq(y = label, d = data, method = "multinom")
## Overall R-squared value:
## 0.9637932</pre>
```

rsq 29

```
## Category-specific R-squared value:
## CATEGORIES
                  VALUES
## 1
         setosa 0.9999824
## 2 versicolor 0.9456770
## 3 virginica 0.9457203
rsq(y = label, d = data, method = "tree")
data <- data.matrix(iris[, 1:4])</pre>
label <- as.numeric(iris[, 5])</pre>
# multinomial
require(nnet)
# model
fit <- multinom(label ~ data, maxit = 1000, MaxNWts = 2000)</pre>
predict.probs <- predict(fit, type = "probs")</pre>
pp<- data.frame(predict.probs)</pre>
# extract the probablity assessment vector
head(pp)
rsq(y = label, d = pp, method = "prob")
table(mtcars$carb)
for (i in (1:length(mtcars$carb))) {
  if (mtcars$carb[i] == 3 | mtcars$carb[i] == 6 | mtcars$carb[i] == 8) {
    mtcars$carb_new[i] = 9
  }else{
    mtcars$carb_new[i] = mtcars$carb[i]
  }
}
data <- data.matrix(mtcars[, c(1)])</pre>
mtcars$carb_new <- factor(mtcars$carb_new)</pre>
label <- mtcars$carb_new</pre>
str(mtcars)
rsq(y = label, d = data, method="tree")
rsq(y = label, d = data, method="lda")
rsq(y = label, d = data, method="lda", prior = c(100,1,1,1)/103)
```

# **Index**

* CCP	nri, <i>3</i> , <i>15</i> , 16
ccp, 5	111 1, 5, 15, 16
mcca-package, 2	pdi, 3, 6, 13, 18, 23
print.mcca.ccp, 23	plot.mcca.hum, $3$ , $20$
* CCR	pm, 3, 22
ests, 9	print.mcca.ccp, 23
* HUM	print.mcca.hum, 24
hum, 12	print.mcca.pdi, 25
mcca-package, 2	print.mcca.rsq, 26
* IDI	2.27
estp, 7	rsq, 3, 27
idi, 14	
mcca-package, 2	
* NRI	
nri, 16	
* PDI	
pdi, 18	
* <b>PM</b>	
pm, 22	
* Plot	
plot.mcca.hum, 20	
* RSQ	
rsq, 27	
* hum	
print.mcca.hum, 24	
* pdi	
print.mcca.pdi,25	
* rsq	
print.mcca.rsq,26	
ccp, 3, 5, 28	
estp, 3, 7, 11	
ests, 3, 8, 9	
6363, 3, 6, 7	
hum, 3, 8, 10, 12, 19	
idi, 3, 14, <i>17</i>	
mcca (mcca-package), 2	
mcca-package, 2	