# Package 'missMethods'

July 22, 2025

Title Methods for Missing Data
Version 0.4.0
Description Supply functions for the creation and handling of missing data as well as tools to evaluate missing data methods. Nearly all possibilities of generating missing data discussed by Santos et al. (2019) <doi:10.1109 access.2019.2891360=""> and some additional are implemented. Functions are supplied to compare parameter estimates and imputed values to true values to evaluate missing data methods. Evaluations of these types are done, for example, by Cetin-Berber et al. (2019) <doi:10.1177 0013164418805532=""> and Kim et al. (2005) <doi:10.1093 bioinformatics="" bth499="">.</doi:10.1093></doi:10.1177></doi:10.1109>
License GPL-3
<pre>URL https://github.com/torockel/missMethods</pre>
BugReports https://github.com/torockel/missMethods/issues
Imports mytnorm, stats, utils
<b>Suggests</b> ggplot2, knitr, lpSolve, norm, rmarkdown, testthat (>= 2.1.0), tibble
VignetteBuilder knitr
Encoding UTF-8
RoxygenNote 7.2.1
NeedsCompilation no
Author Tobias Rockel [aut, cre]
Maintainer Tobias Rockel < Rockel . To@gmail . com>
Repository CRAN
<b>Date/Publication</b> 2022-09-16 15:16:10 UTC
Contents
apply_imputation

2 apply\_imputation

	delete_MAR_1_to_x	
	delete_MAR_censoring	8
	delete_MAR_one_group	11
	delete_MAR_rank	13
	delete_MCAR	15
	delete_MNAR_1_to_x	17
	delete_MNAR_censoring	19
	delete_MNAR_one_group	20
	delete_MNAR_rank	22
	evaluate_imputation_parameters	23
	evaluate_imputed_values	25
	evaluate_parameters	28
	impute_EM	29
	impute_expected_values	30
	impute_hot_deck_in_classes	31
	impute_in_classes	33
	impute_LS_adaptive	34
	impute_LS_array	36
	impute_LS_combined	38
	impute_LS_gene	39
	impute_mean	41
	impute_median	42
	impute_mode	43
	impute_sRHD	44
	median.factor	46
Index		48
appl	y_imputation	

Apply a function for imputation

# Description

Apply a function for imputation over rows, columns or combinations of both

```
apply_imputation(
 ds,
 FUN = mean,
 type = "columnwise",
 convert_tibble = TRUE,
)
```

apply\_imputation 3

#### **Arguments**

ds A data frame or matrix with missing values.

FUN The function to be applied for imputation.

type A string specifying the values used for imputation; one of: "columnwise", "rowwise", "total", "Two-Way" or "Winer" (see details).

convert\_tibble If ds is a tibble, should it be converted (see section A note for tibble users).

Further arguments passed to FUN.

#### **Details**

The functionality of apply\_imputation is inspired by the apply function. The function applies a function FUN to impute the missing values in ds. FUN must be a function, which takes a vector as input and returns exactly one value. The argument type is comparable to apply's MARGIN argument. It specifies the values that are used for the calculation of the imputation values. For example, type = "columnwise" and FUN = mean will impute the mean of the observed values in a column for all missing values in this column. In contrast, type = "rowwise" and FUN = mean will impute the mean of the observed values in a row for all missing values in this row.

List of all implemented types:

- "columnwise" (the default): imputes column by column; all observed values of a column are given to FUN and the returned value is used as the imputation value for all missing values of the column.
- "rowwise": imputes row by row; all observed values of a row are given to FUN and the returned value is used as the imputation value for all missing values of the row.
- "total": All observed values of ds are given to FUN and the returned value is used as the imputation value for all missing values of ds.
- "Winer": The mean value from "columnwise" and "rowwise" is used as the imputation value.
- "Two-Way": The sum of the values from "columnwise" and "rowwise" minus "total" is used as the imputation value.

If no value can be given to FUN (for example, if no value in a column is observed and type = "columnwise"), then a warning will be issued and no value will be imputed in the corresponding column or row.

## Value

An object of the same class as ds with imputed missing values.

## A note for tibble users

If you use tibbles and convert\_tibble is TRUE the tibble is first converted to a data frame, then imputed and converted back. If convert\_tibble is FALSE no conversion is done. However, depending on the tibble and the package version of tibble you use, imputation may not be possible and some errors will be thrown.

4 count\_NA

## References

Beland, S., Pichette, F., & Jolani, S. (2016). Impact on Cronbach's  $\alpha$  of simple treatment methods for missing data. *The Quantitative Methods for Psychology*, 12(1), 57-73.

#### See Also

A convenient interface exists for common cases like mean imputation: impute\_mean, impute\_median, impute\_mode. All these functions call apply\_imputation.

## **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
ds_mis <- delete_MCAR(ds, 0.2)
ds_imp_app <- apply_imputation(ds_mis, FUN = mean, type = "total")
# the same result can be achieved via impute_mean():
ds_imp_mean <- impute_mean(ds_mis, type = "total")
all.equal(ds_imp_app, ds_imp_mean)</pre>
```

count\_NA

Count the number of NAs

## **Description**

Count the number of NA values in a vector, matrix or data frame

## Usage

```
count_NA(x, type = "default")
```

# **Arguments**

Χ

a vector, matrix or data frame, in which NA values are counted

type

How to count the NA values. Possible choices:

- "default": If x is a matrix or a data frame, the number of missing values per column is returned. If x is something else, the total number of missing values in x is returned.
- "all": The number of all missing values in x is returned.
- "cols": The number of missing values per column is returned.
- "rows": The number of missing values per row is returned.

#### Value

The number of missing values.

delete\_MAR\_1\_to\_x 5

## **Examples**

```
count_NA(c(1, NA, 3, NA, 5, NA))
test_df <- data.frame(X1 = rep(c(1, NA), 5), X2 = c(1:9, NA))
count_NA(test_df)
count_NA(test_df, "cols") # the default
count_NA(test_df, "rows")
count_NA(test_df, "all")</pre>
```

delete\_MAR\_1\_to\_x

Create MAR values using MAR1:x

## **Description**

Create missing at random (MAR) values using MAR1:x in a data frame or a matrix

## Usage

```
delete_MAR_1_to_x(
  ds,
 p,
 cols_mis,
 cols_ctrl,
 Х,
  cutoff_fun = median,
 prop = 0.5,
  use_lpSolve = TRUE,
  ordered_as_unordered = FALSE,
  n_mis_stochastic = FALSE,
  x_stochastic = FALSE,
  add_realized_x = FALSE,
  . . . ,
 miss_cols,
 ctrl_cols,
  stochastic
)
```

## **Arguments**

ds	A data frame or matrix in which missing values will be created.
p	A numeric vector with length one or equal to length cols_mis; the probability that a value is missing.
cols_mis	A vector of column names or indices of columns in which missing values will be created.
cols_ctrl	A vector of column names or indices of columns, which controls the creation of missing values in cols_mis. Must be of the same length as cols_mis.

6 delete\_MAR\_1\_to\_x

Numeric with length one (0 < x < Inf); odds are 1 to x for the probability of a value to be missing in group 1 against the probability of a value to be missing in

group 2 (see details).

cutoff\_fun Function that calculates the cutoff values in the cols\_ctrl.

prop Numeric of length one; (minimum) proportion of rows in group 1 (only used for

unordered factors).

use\_lpSolve Logical; should lpSolve be used for the determination of groups, if cols\_ctrl[i]

is an unordered factor.

ordered\_as\_unordered

Logical; should ordered factors be treated as unordered factors.

n\_mis\_stochastic

Х

Logical, should the number of missing values be stochastic? If n\_mis\_stochastic = TRUE, the number of missing values for a column with missing values cols\_mis[i] is a random variable with expected value nrow(ds) \* p[i]. If n\_mis\_stochastic = FALSE, the number of missing values will be deterministic. Normally, the number of missing values for a column with missing values cols\_mis[i] is round(nrow(ds) \* p[i]). Possible deviations from this value, if any exists,

are documented in Details.

x\_stochastic Logical; should the odds be stochastic or deterministic.

add\_realized\_x Logical; if TRUE the realized odds for cols\_mis will be returned (as attribute).

... Further arguments passed to cutoff\_fun.

miss\_cols Deprecated, use cols\_mis instead.

ctrl\_cols Deprecated, use cols\_ctrl instead.

stochastic Deprecated, use n\_mis\_stochastic instead.

## **Details**

This function creates missing at random (MAR) values in the columns specified by the argument cols\_mis. The probability for missing values is controlled by p. If p is a single number, then the overall probability for a value to be missing will be p in all columns of cols\_mis. (Internally p will be replicated to a vector of the same length as cols\_mis. So, all p[i] in the following sections will be equal to the given single number p.) Otherwise, p must be of the same length as cols\_mis. In this case, the overall probability for a value to be missing will be p[i] in the column cols\_mis[i]. The position of the missing values in cols\_mis[i] is controlled by cols\_ctrl[i]. The following procedure is applied for each pair of cols\_ctrl[i] and cols\_mis[i] to determine the positions of missing values:

At first, the rows of ds are divided into two groups. Therefore, the cutoff\_fun calculates a cutoff value for cols\_ctrl[i] (via cutoff\_fun(ds[, cols\_ctrl[i]], ...)). The group 1 consists of the rows, whose values in cols\_ctrl[i] are below the calculated cutoff value. If the so defined group 1 is empty, the rows that have a value equal to the cutoff value will be added to this group (otherwise, these rows will belong to group 2). The group 2 consists of the remaining rows, which are not part of group 1. Now the probabilities for the rows in the two groups are set in the way that the odds are 1:x against a missing value in cols\_mis[i] for the rows in group 1 compared to the rows in group 2. That means, the probability for a value to be missing in group 1 divided by the probability for a value to be missing in group 2 equals 1 divided by x. For example, for two equal

 $delete\_MAR\_1\_to\_x$  7

sized groups 1 and 2, ideally the number of NAs in group 1 divided by the number of NAs in group 2 should equal 1 divided by x. But there are some restrictions, which can lead to some deviations from the odds 1:x (see below).

If x\_stochastic and n\_mis\_stochastic are false (the default), then exactly round(nrow(ds) \* p[i]) values will be set NA in column cols\_mis[i]. To achieve this, it is possible that the true odds differ from 1:x. The number of observations that are deleted in group 1 and group 2 are chosen to minimize the absolute difference between the realized odds and 1:x. Furthermore, if round(nrow(ds) \* p[i]) == 0, then no missing value will be created in cols\_mis[i].

If x\_stochastic is true, the rows from the two groups will get sampling weights proportional to 1 (group 1) and x (group 2). If n\_mis\_stochastic is false, these weights are given to sample via the argument prob and exactly round(nrow(ds) \* p[i]) values will be set NA. If n\_mis\_stochastic is true, the sampling weights will be scaled and compared to uniform random numbers. The scaling is done in such a way to get expected nrow(ds) \* p[i] missing values in cols\_mis[i].

If p is high and x is too high or too low, it is possible that the odds 1:x and the proportion of missing values p cannot be realized together. For example, if p[i] = 0.9, then a maximum of x = 1.25 is possible (assuming that exactly 50 % of the values are below and 50 % of the values are above the cutoff value in  $cols_ctrl[i]$ ). If a combination of p and x that cannot be realized together is given to  $delete_MAR_1_to_x$ , then a warning will be generated and x will be adjusted in such a way that p can be realized as given to the function. The warning can be silenced by setting the option missMethods.warn.too.high.p to false.

The argument add\_realized\_x controls whether the x of the realized odds are added to the return value or not. If add\_realized\_x = TRUE, then the realized x values for all cols\_mis will be added as an attribute to the returned object. For x\_stochastic = TRUE these realized x will differ from the given x most of the time and will change if the function is rerun without setting a seed. For  $x_stochastic = FALSE$ , it is also possible that the realized odds differ (see above). However, the realized odds will be constant over multiple runs.

## Value

An object of the same class as ds with missing values.

#### **Treatment of factors**

If ds[, cols\_ctrl[i]] is an unordered factor, then the concept of a cutoff value is not meaningful and cannot be applied. Instead, a combinations of the levels of the unordered factor is searched that

- guarantees at least a proportion of prop rows are in group 1
- minimize the difference between prop and the proportion of rows in group 1.

This can be seen as a binary search problem, which is solved by the solver from the package lpSolve, if use\_lpSolve = TRUE. If use\_lpSolve = FALSE, a very simple heuristic is applied. The heuristic only guarantees that at least a proportion of prop rows are in group 1. The choice use\_lpSolve = FALSE is not recommend and should only be considered, if the solver of lpSolve fails.

If ordered\_as\_unordered = TRUE, then ordered factors will be treated like unordered factors and the same binary search problem will be solved for both types of factors. If ordered\_as\_unordered = FALSE (the default), then ordered factors will be grouped via cutoff\_fun as described in Details.

## References

Santos, M. S., Pereira, R. C., Costa, A. F., Soares, J. P., Santos, J., & Abreu, P. H. (2019). Generating Synthetic Missing Data: A Review by Missing Mechanism. *IEEE Access*, 7, 11651-11667

## See Also

```
delete_MNAR_1_to_x
```

Other functions to create MAR: delete\_MAR\_censoring(), delete\_MAR\_one\_group(), delete\_MAR\_rank()

## **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
delete_MAR_1_to_x(ds, 0.2, "X", "Y", 3)
# beware of small datasets and x_stochastic = FALSE
attr(delete_MAR_1_to_x(ds, 0.4, "X", "Y", 3, add_realized_x = TRUE), "realized_x")
attr(delete_MAR_1_to_x(ds, 0.4, "X", "Y", 4, add_realized_x = TRUE), "realized_x")
attr(delete_MAR_1_to_x(ds, 0.4, "X", "Y", 5, add_realized_x = TRUE), "realized_x")
attr(delete_MAR_1_to_x(ds, 0.4, "X", "Y", 7, add_realized_x = TRUE), "realized_x")
# p = 0.4 and 20 values -> 8 missing values, possible combinations:
# either 6 above 2 below (x = 3) or
# 7 above and 1 below (x = 7)
# Too high combination of p and x:
tryCatch(delete_MAR_1_to_x(ds, 0.9, "X", "Y", 3), warning = function(w) w)
```

delete\_MAR\_censoring Create MAR values using a censoring mechanism

## **Description**

Create missing at random (MAR) values using a censoring mechanism in a data frame or a matrix

```
delete_MAR_censoring(
   ds,
   p,
   cols_mis,
   cols_ctrl,
   n_mis_stochastic = FALSE,
   where = "lower",
   sorting = TRUE,
   miss_cols,
   ctrl_cols
)
```

#### **Arguments**

ds A data frame or matrix in which missing values will be created.

p A numeric vector with length one or equal to length cols\_mis; the probability

that a value is missing.

cols\_mis A vector of column names or indices of columns in which missing values will

be created.

cols\_ctrl A vector of column names or indices of columns, which controls the creation of

missing values in cols\_mis. Must be of the same length as cols\_mis.

n\_mis\_stochastic

Logical, should the number of missing values be stochastic? If n\_mis\_stochastic = TRUE, the number of missing values for a column with missing values cols\_mis[i] is a random variable with expected value nrow(ds) \* p[i]. If n\_mis\_stochastic = FALSE, the number of missing values will be deterministic. Normally, the number of missing values for a column with missing values cols\_mis[i] is round(nrow(ds) \* p[i]). Possible deviations from this value, if any exists,

are documented in Details.

where Controls where missing values are created; one of "lower", "upper" or "both"

(see details).

sorting Logical; should sorting be used or a quantile as a threshold.

miss\_cols Deprecated, use cols\_mis instead.

ctrl\_cols Deprecated, use cols\_ctrl instead.

## **Details**

This function creates missing at random (MAR) values in the columns specified by the argument cols\_mis. The probability for missing values is controlled by p. If p is a single number, then the overall probability for a value to be missing will be p in all columns of cols\_mis. (Internally p will be replicated to a vector of the same length as cols\_mis. So, all p[i] in the following sections will be equal to the given single number p.) Otherwise, p must be of the same length as cols\_mis. In this case, the overall probability for a value to be missing will be p[i] in the column cols\_mis[i]. The position of the missing values in cols\_mis[i] is controlled by cols\_ctrl[i]. The following procedure is applied for each pair of cols\_ctrl[i] and cols\_mis[i] to determine the positions of missing values:

The default behavior (sorting = TRUE) of this function is to first sort the column cols\_ctrl[i]. Then missing values in cols\_mis[i] are created in the rows with the round(nrow(ds) \* p[i]) smallest values. This censors approximately the proportion of p[i] rows of smallest values in cols\_ctrl[i] in cols\_mis[i]. Hence, the name of the function.

If where = "upper", instead of the rows with the smallest values, the rows with the highest values will be selected. For where = "both", the one half of the round(nrow(ds) \* p[i]) rows with missing values will be the rows with the smallest values and the other half will be the rows with the highest values. So the censoring rows are dived to the highest and smallest values of cols\_ctrl[i]. For odd round(nrow(ds) \* p[i]) one more value is set NA among the smallest values.

If  $n_mis_stochastic = TRUE$  and sorting = TRUE the procedure is lightly altered. In this case, at first the floor(nrow(ds) \* p[i]) rows with the smallest values (where = "lower") are set NA. If nrow(ds) \* p[i] > floor(nrow(ds) \* p[i]), the row with the next greater value will be set

NA with a probability to get expected nrow(ds) \* p[i] missing values. For where = "upper" this "random" missing value will be the next smallest. For where = "both" this "random" missing value will be the next greatest of the smallest values.

If sorting = FALSE, the rows of ds will not be sorted. Instead, a quantile will be calculated (using quantile). If where = "lower", the quantile(ds[, cols\_ctrl[i]], p[i]) will be calculated and all rows with values in ds[, cols\_ctrl[i]] below this quantile will have missing values in cols\_mis[i]. For where = "upper", the quantile(ds[, cols\_ctrl[i]], 1 - p[i]) will be calculated and all rows with values above this quantile will have missing values. For where = "both", the quantile(ds[, cols\_ctrl[i]],p[i] / 2) and quantile(ds[, cols\_ctrl[i]], 1 - p[i] / 2) will be calculated. All rows with values in cols\_ctrl[i] below the first quantile or above the second quantile will have missing values in cols\_mis[i].

For sorting = FALSE only n\_mis\_stochastic = FALSE is implemented at the moment.

The option sorting = TRUE with n\_mis\_stochastic = FALSE will always create exactly round(nrow(ds) \* p[i]) missing values in cols\_mis[i]. With n\_mis\_stochastic = TRUE) sorting will result in floor(nrow(ds) \* p[i]) or ceiling(nrow(ds) \* p[i]) missing values in cols\_mis[i]. For sorting = FALSE, the number of missing values will normally be close to nrow(ds) \* p[i]. But for cols\_ctrl with many duplicates the choice sorting = FALSE can be problematic, because of the calculation of quantile(ds[,cols\_ctrl[i]], p[i]) and setting values NA below this threshold (see examples). So, in most cases sorting = TRUE is recommended.

#### Value

An object of the same class as ds with missing values.

#### References

Santos, M. S., Pereira, R. C., Costa, A. F., Soares, J. P., Santos, J., & Abreu, P. H. (2019). Generating Synthetic Missing Data: A Review by Missing Mechanism. *IEEE Access*, 7, 11651-11667

#### See Also

```
delete_MNAR_censoring
```

Other functions to create MAR: delete\_MAR\_1\_to\_x(), delete\_MAR\_one\_group(), delete\_MAR\_rank()

#### **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
delete_MAR_censoring(ds, 0.2, "X", "Y")
# many dupplicated values can be problematic for sorting = FALSE:
ds_many_dup <- data.frame(X = 1:20, Y = c(rep(0, 10), rep(1, 10)))
delete_MAR_censoring(ds_many_dup, 0.2, "X", "Y") # 4 NAs as expected
quantile(ds_many_dup$Y, 0.2) # 0
# No value is BELOW 0 in ds_many_dup$Y, so no missing values will be created:
delete_MAR_censoring(ds_many_dup, 0.2, "X", "Y", sorting = FALSE) # No NA!</pre>
```

delete\_MAR\_one\_group Create MAR values by deleting values in one of two groups

## **Description**

Create missing at random (MAR) values by deleting values in one of two groups in a data frame or a matrix

# Usage

```
delete_MAR_one_group(
    ds,
    p,
    cols_mis,
    cols_ctrl,
    cutoff_fun = median,
    prop = 0.5,
    use_lpSolve = TRUE,
    ordered_as_unordered = FALSE,
    n_mis_stochastic = FALSE,
    ...,
    miss_cols,
    ctrl_cols,
    stochastic
)
```

# Arguments

_	
ds	A data frame or matrix in which missing values will be created.
p	A numeric vector with length one or equal to length cols_mis; the probability that a value is missing.
cols_mis	A vector of column names or indices of columns in which missing values will be created.
cols_ctrl	A vector of column names or indices of columns, which controls the creation of missing values in cols_mis. Must be of the same length as cols_mis.
cutoff_fun	Function that calculates the cutoff values in the cols_ctrl.
prop	Numeric of length one; (minimum) proportion of rows in group 1 (only used for unordered factors).
use_lpSolve	Logical; should lpSolve be used for the determination of groups, if cols_ctrl[i] is an unordered factor.
ordered_as_unordered	
	Logical; should ordered factors be treated as unordered factors.
n_mis_stochastic	
	$Logical, should the number of missing values be stochastic? If \verb n_mis_stochastic  $

= TRUE, the number of missing values for a column with missing values cols\_mis[i]

is a random variable with expected value nrow(ds) \* p[i]. If n\_mis\_stochastic = FALSE, the number of missing values will be deterministic. Normally, the number of missing values for a column with missing values cols\_mis[i] is round(nrow(ds) \* p[i]). Possible deviations from this value, if any exists, are documented in Details.

... Further arguments passed to cutoff\_fun.

miss\_cols Deprecated, use cols\_mis instead.

ctrl\_cols Deprecated, use cols\_ctrl instead.

stochastic Deprecated, use n\_mis\_stochastic instead.

#### **Details**

This function creates missing at random (MAR) values in the columns specified by the argument cols\_mis. The probability for missing values is controlled by p. If p is a single number, then the overall probability for a value to be missing will be p in all columns of cols\_mis. (Internally p will be replicated to a vector of the same length as cols\_mis. So, all p[i] in the following sections will be equal to the given single number p.) Otherwise, p must be of the same length as cols\_mis. In this case, the overall probability for a value to be missing will be p[i] in the column cols\_mis[i]. The position of the missing values in cols\_mis[i] is controlled by cols\_ctrl[i]. The following procedure is applied for each pair of cols\_ctrl[i] and cols\_mis[i] to determine the positions of missing values:

At first, the rows of ds are divided into two groups. Therefore, the cutoff\_fun calculates a cutoff value for cols\_ctrl[i] (via cutoff\_fun(ds[, cols\_ctrl[i]], ...). The group 1 consists of the rows, whose values in cols\_ctrl[i] are below the calculated cutoff value. If the so defined group 1 is empty, the rows that are equal to the cutoff value will be added to this group (otherwise, these rows will belong to group 2). The group 2 consists of the remaining rows, which are not part of group 1. Now one of these two groups is chosen randomly. In the chosen group, values are deleted in cols\_mis[i]. In the other group, no missing values will be created in cols\_mis[i].

If p is too high, it is possible that a group contains not enough objects to reach nrow(ds) \* p missing values. In this case, p is reduced to the maximum possible value (given the (random) group with missing data) and a warning is given. Obviously this case will occur regularly, if p > 0.5. Therefore, this function should normally not be called with p > 0.5. However, this can occur for smaller values of p, too (depending on the grouping). The warning can be silenced by setting the option missMethods.warn.too.high.p to false.

#### Value

An object of the same class as ds with missing values.

#### **Treatment of factors**

If ds[, cols\_ctrl[i]] is an unordered factor, then the concept of a cutoff value is not meaningful and cannot be applied. Instead, a combinations of the levels of the unordered factor is searched that

- guarantees at least a proportion of prop rows are in group 1
- minimize the difference between prop and the proportion of rows in group 1.

delete\_MAR\_rank 13

This can be seen as a binary search problem, which is solved by the solver from the package lpSolve, if use\_lpSolve = TRUE. If use\_lpSolve = FALSE, a very simple heuristic is applied. The heuristic only guarantees that at least a proportion of prop rows are in group 1. The choice use\_lpSolve = FALSE is not recommend and should only be considered, if the solver of lpSolve fails.

If ordered\_as\_unordered = TRUE, then ordered factors will be treated like unordered factors and the same binary search problem will be solved for both types of factors. If ordered\_as\_unordered = FALSE (the default), then ordered factors will be grouped via cutoff\_fun as described in Details.

#### References

Santos, M. S., Pereira, R. C., Costa, A. F., Soares, J. P., Santos, J., & Abreu, P. H. (2019). Generating Synthetic Missing Data: A Review by Missing Mechanism. *IEEE Access*, 7, 11651-11667

#### See Also

```
delete_MNAR_one_group
```

Other functions to create MAR: delete\_MAR\_1\_to\_x(), delete\_MAR\_censoring(), delete\_MAR\_rank()

## **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
delete_MAR_one_group(ds, 0.2, "X", "Y")
```

delete\_MAR\_rank

Create MAR values using a ranking mechanism

#### **Description**

Create missing at random (MAR) values using a ranking mechanism in a data frame or a matrix

```
delete_MAR_rank(
    ds,
    p,
    cols_mis,
    cols_ctrl,
    n_mis_stochastic = FALSE,
    ties.method = "average",
    miss_cols,
    ctrl_cols
)
```

14 delete\_MAR\_rank

#### **Arguments**

ds A data frame or matrix in which missing values will be created.

p A numeric vector with length one or equal to length cols\_mis; the probability

that a value is missing.

cols\_mis A vector of column names or indices of columns in which missing values will

be created.

cols\_ctrl A vector of column names or indices of columns, which controls the creation of

missing values in cols\_mis. Must be of the same length as cols\_mis.

n\_mis\_stochastic

Logical, should the number of missing values be stochastic? If n\_mis\_stochastic = TRUE, the number of missing values for a column with missing values cols\_mis[i] is a random variable with expected value nrow(ds) \* p[i]. If n\_mis\_stochastic = FALSE, the number of missing values will be deterministic. Normally, the number of missing values for a column with missing values cols\_mis[i] is round(nrow(ds) \* p[i]). Possible deviations from this value, if any exists,

are documented in Details.

ties.method How ties are handled. Passed to rank.
miss\_cols Deprecated, use cols\_mis instead.
ctrl\_cols Deprecated, use cols\_ctrl instead.

#### **Details**

This function creates missing at random (MAR) values in the columns specified by the argument cols\_mis. The probability for missing values is controlled by p. If p is a single number, then the overall probability for a value to be missing will be p in all columns of cols\_mis. (Internally p will be replicated to a vector of the same length as cols\_mis. So, all p[i] in the following sections will be equal to the given single number p.) Otherwise, p must be of the same length as cols\_mis. In this case, the overall probability for a value to be missing will be p[i] in the column cols\_mis[i]. The position of the missing values in cols\_mis[i] is controlled by cols\_ctrl[i]. The following procedure is applied for each pair of cols\_ctrl[i] and cols\_mis[i] to determine the positions of missing values:

At first, the probability for a value to be missing is calculated. This probability for a missing value in a row of cols\_mis[i] is proportional to the rank of the value in cols\_ctrl[i] in the same row. If n\_mis\_stochastic = FALSE these probabilities are given to the prob argument of sample. If n\_mis\_stochastic = TRUE, they are scaled to sum up to nrow(ds) \* p[i]. Then for each probability a uniformly distributed random number is generated. If this random number is less than the probability, the value in cols\_mis[i] is set NA.

The ranks are calculated via rank. The argument ties.method is directly passed to this function. Possible choices for ties.method are documented in rank.

For high values of p it is mathematically not possible to get probabilities proportional to the ranks. In this case, a warning is given. This warning can be silenced by setting the option missMethods.warn.too.high.p to false.

## Value

An object of the same class as ds with missing values.

delete\_MCAR 15

## References

Santos, M. S., Pereira, R. C., Costa, A. F., Soares, J. P., Santos, J., & Abreu, P. H. (2019). Generating Synthetic Missing Data: A Review by Missing Mechanism. *IEEE Access*, 7, 11651-11667

#### See Also

```
rank, delete_MNAR_rank
```

Other functions to create MAR: delete\_MAR\_1\_to\_x(), delete\_MAR\_censoring(), delete\_MAR\_one\_group()

## **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
delete_MAR_rank(ds, 0.2, "X", "Y")</pre>
```

delete\_MCAR

Create MCAR values

## **Description**

Create missing completely at random (MCAR) values in a data frame or a matrix

## Usage

```
delete_MCAR(
   ds,
   p,
   cols_mis = seq_len(ncol(ds)),
   n_mis_stochastic = FALSE,
   p_overall = FALSE,
   miss_cols,
   stochastic
)
```

## **Arguments**

ds A data frame or matrix in which missing values will be created.

p A numeric vector with length one or equal to length cols\_mis; the probability

that a value is missing.

cols\_mis A vector of column names or indices of columns in which missing values will

be created.

 $n\_mis\_stochastic$ 

Logical, should the number of missing values be stochastic? If n\_mis\_stochastic = TRUE, the number of missing values for a column with missing values cols\_mis[i] is a random variable with expected value nrow(ds) \* p[i]. If n\_mis\_stochastic = FALSE, the number of missing values will be deterministic. Normally, the number of missing values for a column with missing values cols\_mis[i] is round(nrow(ds) \* p[i]). Possible deviations from this value, if any exists, are documented in Details.

16 delete\_MCAR

p_overall	Logical; see details.
miss_cols	Deprecated, use cols_mis instead.
stochastic	Deprecated, use n_mis_stochastic instead.

#### **Details**

This function creates missing completely at random (MCAR) values in the dataset ds. The proportion of missing values is specified with p. The columns in which missing values are created can be set via cols\_mis. If cols\_mis is not specified, then missing values are created in all columns of ds.

The probability for missing values is controlled by p. If p is a single number, then the overall probability for a value to be missing will be p in all columns of cols\_mis. (Internally p will be replicated to a vector of the same length as cols\_mis. So, all p[i] in the following sections will be equal to the given single number p.) Otherwise, p must be of the same length as cols\_mis. In this case, the overall probability for a value to be missing will be p[i] in the column cols\_mis[i].

If n\_mis\_stochastic = FALSE and p\_overall = FALSE (the default), then exactly round(nrow(ds) \* p[i]) values will be set NA in column cols\_mis[i]. If n\_mis\_stochastic = FALSE and p\_overall = TRUE, then p must be of length one and exactly round(nrow(ds) \* p \* length(cols\_mis)) values will be set NA (over all columns in cols\_mis). This can result in a proportion of missing values in every miss\_col unequal to p, but the proportion of missing values in all columns together will be close to p.

If  $n_mis\_stochastic = TRUE$ , then each value in column  $cols_mis[i]$  has probability p[i] to be missing (independently of all other values). Therefore, the number of missing values in  $cols_mis[i]$  is a random variable with a binomial distribution B(nrow(ds), p[i]). This can (and will most of the time) lead to more or less missing values than round(nrow(ds) \* p[i]) in column  $cols_mis[i]$ . If  $n_mis\_stochastic = TRUE$ , then the argument  $p\_overall$  is ignored because it is superfluous.

#### Value

An object of the same class as ds with missing values.

## References

Santos, M. S., Pereira, R. C., Costa, A. F., Soares, J. P., Santos, J., & Abreu, P. H. (2019). Generating Synthetic Missing Data: A Review by Missing Mechanism. *IEEE Access*, 7, 11651-11667

## **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
delete_MCAR(ds, 0.2)</pre>
```

# Description

Create missing not at random (MNAR) values using MNAR1:x in a data frame or a matrix

# Usage

```
delete_MNAR_1_to_x(
    ds,
    p,
    cols_mis,
    x,
    cutoff_fun = median,
    prop = 0.5,
    use_lpSolve = TRUE,
    ordered_as_unordered = FALSE,
    n_mis_stochastic = FALSE,
    x_stochastic = FALSE,
    add_realized_x = FALSE,
    ...,
    miss_cols,
    stochastic
)
```

## **Arguments**

ds	A data frame or matrix in which missing values will be created.
p	A numeric vector with length one or equal to length cols_mis; the probability that a value is missing.
cols_mis	A vector of column names or indices of columns in which missing values will be created.
х	Numeric with length one $(0 < x < Inf)$ ; odds are 1 to x for the probability of a value to be missing in group 1 against the probability of a value to be missing in group 2 (see details).
cutoff_fun	Function that calculates the cutoff values in the cols_ctrl.
prop	Numeric of length one; (minimum) proportion of rows in group 1 (only used for unordered factors).
use_lpSolve	Logical; should lpSolve be used for the determination of groups, if cols_ctrl[i] is an unordered factor.
ordered_as_unordered	
	T 1 - 1 - 1 - 1 - 1 - 1 1 C - 4 1 - 4 4 - 1 1 C - 4

Logical; should ordered factors be treated as unordered factors.

n\_mis\_stochastic

Logical, should the number of missing values be stochastic? If n\_mis\_stochastic = TRUE, the number of missing values for a column with missing values cols\_mis[i] is a random variable with expected value nrow(ds) \* p[i]. If n\_mis\_stochastic = FALSE, the number of missing values will be deterministic. Normally, the number of missing values for a column with missing values cols\_mis[i] is round(nrow(ds) \* p[i]). Possible deviations from this value, if any exists, are documented in Details.

x\_stochastic Logical; should the odds be stochastic or deterministic.

add\_realized\_x Logical; if TRUE the realized odds for cols\_mis will be returned (as attribute).

... Further arguments passed to cutoff\_fun.

miss\_cols Deprecated, use cols\_mis instead.

stochastic Deprecated, use n\_mis\_stochastic instead.

#### **Details**

The functions delete\_MNAR\_1\_to\_x and delete\_MAR\_1\_to\_x are sisters. The only difference between these two functions is the column that controls the generation of missing values. In delete\_MAR\_1\_to\_x a separate column cols\_ctrl[i] controls the generation of missing values in cols\_mis[i]. In contrast, in delete\_MNAR\_1\_to\_x the generation of missing values in cols\_mis[i] is controlled by cols\_mis[i] itself. All other aspects are identical for both functions. Therefore, further details can be found in delete\_MAR\_1\_to\_x.

## Value

An object of the same class as ds with missing values.

#### References

Santos, M. S., Pereira, R. C., Costa, A. F., Soares, J. P., Santos, J., & Abreu, P. H. (2019). Generating Synthetic Missing Data: A Review by Missing Mechanism. *IEEE Access*, 7, 11651-11667

#### See Also

```
delete_MAR_1_to_x
```

Other functions to create MNAR: delete\_MNAR\_censoring(), delete\_MNAR\_one\_group(), delete\_MNAR\_rank()

## **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
delete_MNAR_1_to_x(ds, 0.2, "X", X = 3)
```

delete\_MNAR\_censoring Create MNAR values using a censoring mechanism

## **Description**

Create missing not at random (MNAR) values using a censoring mechanism in a data frame or a matrix

## Usage

```
delete_MNAR_censoring(
   ds,
   p,
   cols_mis,
   n_mis_stochastic = FALSE,
   where = "lower",
   sorting = TRUE,
   miss_cols
)
```

## **Arguments**

ds A data frame or matrix in which missing values will be created.

p A numeric vector with length one or equal to length cols\_mis; the probability

that a value is missing.

cols\_mis A vector of column names or indices of columns in which missing values will

be created.

n\_mis\_stochastic

Logical, should the number of missing values be stochastic? If n\_mis\_stochastic = TRUE, the number of missing values for a column with missing values cols\_mis[i] is a random variable with expected value nrow(ds) \* p[i]. If n\_mis\_stochastic = FALSE, the number of missing values will be deterministic. Normally, the number of missing values for a column with missing values cols\_mis[i] is round(nrow(ds) \* p[i]). Possible deviations from this value, if any exists,

are documented in Details.

where Controls where missing values are created; one of "lower", "upper" or "both"

(see details).

sorting Logical; should sorting be used or a quantile as a threshold.

miss\_cols Deprecated, use cols\_mis instead.

#### **Details**

The functions delete\_MNAR\_censoring and delete\_MAR\_censoring are sisters. The only difference between these two functions is the column that controls the generation of missing values. In delete\_MAR\_censoring a separate column cols\_ctrl[i] controls the generation of missing values in cols\_mis[i]. In contrast, in delete\_MNAR\_censoring the generation of missing values in

cols\_mis[i] is controlled by cols\_mis[i] itself. All other aspects are identical for both functions. Therefore, further details can be found in delete\_MAR\_censoring.

#### Value

An object of the same class as ds with missing values.

#### References

Santos, M. S., Pereira, R. C., Costa, A. F., Soares, J. P., Santos, J., & Abreu, P. H. (2019). Generating Synthetic Missing Data: A Review by Missing Mechanism. *IEEE Access*, 7, 11651-11667

#### See Also

```
delete_MAR_censoring
```

Other functions to create MNAR: delete\_MNAR\_1\_to\_x(), delete\_MNAR\_one\_group(), delete\_MNAR\_rank()

## **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
delete_MNAR_censoring(ds, 0.2, "X")</pre>
```

delete\_MNAR\_one\_group Create MNAR values by deleting values in one of two groups

## Description

Create missing not at random (MNAR) values by deleting values in one of two groups in a data frame or a matrix

```
delete_MNAR_one_group(
   ds,
   p,
   cols_mis,
   cutoff_fun = median,
   prop = 0.5,
   use_lpSolve = TRUE,
   ordered_as_unordered = FALSE,
   n_mis_stochastic = FALSE,
   ...,
   miss_cols,
   stochastic
)
```

#### **Arguments**

ds A data frame or matrix in which missing values will be created.

p A numeric vector with length one or equal to length cols\_mis; the probability

that a value is missing.

cols\_mis A vector of column names or indices of columns in which missing values will

be created.

cutoff\_fun Function that calculates the cutoff values in the cols\_ctrl.

prop Numeric of length one; (minimum) proportion of rows in group 1 (only used for

unordered factors).

use\_lpSolve Logical; should lpSolve be used for the determination of groups, if cols\_ctrl[i]

is an unordered factor.

ordered\_as\_unordered

Logical; should ordered factors be treated as unordered factors.

n\_mis\_stochastic

Logical, should the number of missing values be stochastic? If n\_mis\_stochastic = TRUE, the number of missing values for a column with missing values cols\_mis[i] is a random variable with expected value nrow(ds) \* p[i]. If n\_mis\_stochastic = FALSE, the number of missing values will be deterministic. Normally, the number of missing values for a column with missing values cols\_mis[i] is round(nrow(ds) \* p[i]). Possible deviations from this value, if any exists,

are documented in Details.

... Further arguments passed to cutoff\_fun.

miss\_cols Deprecated, use cols\_mis instead.

stochastic Deprecated, use n\_mis\_stochastic instead.

#### **Details**

The functions delete\_MNAR\_one\_group and delete\_MAR\_one\_group are sisters. The only difference between these two functions is the column that controls the generation of missing values. In delete\_MAR\_one\_group a separate column cols\_ctrl[i] controls the generation of missing values in cols\_mis[i]. In contrast, in delete\_MNAR\_one\_group the generation of missing values in cols\_mis[i] is controlled by cols\_mis[i] itself. All other aspects are identical for both functions. Therefore, further details can be found in delete\_MAR\_one\_group.

#### Value

An object of the same class as ds with missing values.

#### References

Santos, M. S., Pereira, R. C., Costa, A. F., Soares, J. P., Santos, J., & Abreu, P. H. (2019). Generating Synthetic Missing Data: A Review by Missing Mechanism. *IEEE Access*, 7, 11651-11667

## See Also

```
delete_MAR_one_group
```

Other functions to create MNAR: delete\_MNAR\_1\_to\_x(), delete\_MNAR\_censoring(), delete\_MNAR\_rank()

22 delete\_MNAR\_rank

## **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
delete_MNAR_one_group(ds, 0.2, "X")</pre>
```

delete\_MNAR\_rank

Create MNAR values using a ranking mechanism

## Description

Create missing not at random (MNAR) values using a ranking mechanism in a data frame or a matrix

## Usage

```
delete_MNAR_rank(
   ds,
   p,
   cols_mis,
   n_mis_stochastic = FALSE,
   ties.method = "average",
   miss_cols
)
```

## Arguments

ds A data frame or matrix in which missing values will be created.

p A numeric vector with length one or equal to length cols\_mis; the probability

that a value is missing.

cols\_mis A vector of column names or indices of columns in which missing values will

be created.

n\_mis\_stochastic

Logical, should the number of missing values be stochastic? If n\_mis\_stochastic = TRUE, the number of missing values for a column with missing values cols\_mis[i] is a random variable with expected value nrow(ds) \* p[i]. If n\_mis\_stochastic = FALSE, the number of missing values will be deterministic. Normally, the number of missing values for a column with missing values cols\_mis[i] is round(nrow(ds) \* p[i]). Possible deviations from this value, if any exists,

are documented in Details.

ties.method How ties are handled. Passed to rank.

miss\_cols Deprecated, use cols\_mis instead.

#### **Details**

The functions delete\_MNAR\_rank and delete\_MAR\_rank are sisters. The only difference between these two functions is the column that controls the generation of missing values. In delete\_MAR\_rank a separate column cols\_ctrl[i] controls the generation of missing values in cols\_mis[i]. In contrast, in delete\_MNAR\_rank the generation of missing values in cols\_mis[i] is controlled by cols\_mis[i] itself. All other aspects are identical for both functions. Therefore, further details can be found in delete\_MAR\_rank.

#### Value

An object of the same class as ds with missing values.

#### References

```
Santos, M. S., Pereira, R. C., Costa, A. F., Soares, J. P., Santos, J., & Abreu, P. H. (2019). Generating Synthetic Missing Data: A Review by Missing Mechanism. IEEE Access, 7, 11651-11667
```

## See Also

```
delete_MAR_rank
```

Other functions to create MNAR: delete\_MNAR\_1\_to\_x(), delete\_MNAR\_censoring(), delete\_MNAR\_one\_group()

## **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
delete_MNAR_rank(ds, 0.2, "X")</pre>
```

evaluate\_imputation\_parameters

Evaluate estimated parameters after imputation

# Description

Compares estimated parameters after imputation to true parameters or estimates based on the original dataset

```
evaluate_imputation_parameters(
  ds_imp,
  ds_orig = NULL,
  pars_true = NULL,
  parameter = "mean",
  criterion = "RMSE",
  cols_which = seq_len(ncol(ds_imp)),
  tolerance = sqrt(.Machine$double.eps),
  ...,
```

```
imp_ds,
  true_pars,
  which_cols
)
```

## **Arguments**

ds_imp	A data frame or matrix with imputed values.
ds_orig	A data frame or matrix with original (true) values.
pars_true	True parameters, normally a vector or a matrix.
parameter	A string specifying the estimated parameters for comparison.
criterion	A string specifying the used criterion for comparing the imputed and original values.
cols_which	Indices or names of columns used for evaluation.
tolerance	Numeric, only used for criterion = "precision": numeric differences smaller than tolerance are treated as zero/equal.
	Further arguments passed to the function for parameter estimation.
imp_ds	Deprecated, renamed to ds_imp.
true_pars	Deprecated, renamed to pars_true.
which_cols	Deprecated, renamed to cols_which.

## **Details**

Either ds\_orig or pars\_true must be supplied and the other one must be NULL (default: both are NULL, just supply one, see examples). The following parameters are implemented: "mean", "median", "var", "sd", "quantile", "cov", "cov\_only", cor", "cor\_only". Some details follow:

- "var", "cov" and "cov\_only": For "var" only the variances of the columns (the diagonal elements of the covariance matrix) are compared. For "cov" the whole covariance matrix is compared. For "cov\_only" only the upper triangle (excluding the diagonal) of the covariance matrix is compared.
- "cor", "cor\_only": For "cor" the whole correlation matrix is compared. For "cor\_only" only the upper triangle (excluding the diagonal) of the correlation matrix is compared.
- "quantile": the quantiles can be set via the additional argument probs (see examples). Otherwise, the default quantiles from quantile will be used.

The argument cols\_which allows the selection of columns for comparison (see examples). If pars\_true is used, it is assumed that only relevant parameters are supplied (see examples).

Possible choices for the argument criterion are documented in evaluate\_imputed\_values

#### Value

A numeric vector of length one.

## References

Cetin-Berber, D. D., Sari, H. I., & Huggins-Manley, A. C. (2019). Imputation Methods to Deal With Missing Responses in Computerized Adaptive Multistage Testing. *Educational and psychological measurement*, 79(3), 495-511.

#### See Also

Other evaluation functions: evaluate\_imputed\_values(), evaluate\_parameters()

## **Examples**

```
# only ds_orig known
ds\_orig <- data.frame(X = 1:10, Y = 101:101)
ds_imp <- impute_mean(delete_MCAR(ds_orig, 0.4))</pre>
evaluate_imputation_parameters(ds_imp, ds_orig = ds_orig)
# true parameters known
ds_orig <- data.frame(X = rnorm(100), Y = rnorm(100, mean = 10))</pre>
ds_imp <- impute_mean(delete_MCAR(ds_orig, 0.3))</pre>
evaluate_imputation_parameters(ds_imp, pars_true = c(0, 10), parameter = "mean")
evaluate_imputation_parameters(ds_imp, pars_true = c(1, 1), parameter = "var")
# set quantiles
evaluate_imputation_parameters(ds_imp,
  pars_true = c(qnorm(0.3), qnorm(0.3, mean = 10)),
  parameter = "quantile", probs = 0.3
)
# compare only column Y
evaluate_imputation_parameters(ds_imp,
  pars_true = c(Y = 10), parameter = "mean",
  cols_which = "Y"
)
```

evaluate\_imputed\_values

Evaluate imputed values

## **Description**

Compare imputed to true values

```
evaluate_imputed_values(
  ds_imp,
  ds_orig,
  criterion = "RMSE",
  M = NULL,
```

```
cols_which = seq_len(ncol(ds_imp)),
tolerance = sqrt(.Machine$double.eps),
imp_ds,
orig_ds,
which_cols
)
```

## **Arguments**

ds_imp	A data frame or matrix with imputed values.
ds_orig	A data frame or matrix with original (true) values.
criterion	A string specifying the used criterion for comparing the imputed and original values.
М	NULL (the default) or a missing data indicator matrix. The missing data indicator matrix is normally created via is.na(ds_mis), where ds_mis is the dataset after deleting values from ds_orig.
cols_which	Indices or names of columns used for evaluation.
tolerance	Numeric, only used for criterion = "precision": numeric differences smaller than tolerance are treated as zero/equal.
imp_ds	Deprecated, renamed to ds_imp.
orig_ds	Deprecated, renamed to ds_orig.
which_cols	Deprecated, renamed to cols_which.

## **Details**

The following criterions are implemented to compare the imputed values to the true values:

- "RMSE" (the default): The Root Mean Squared Error between the imputed and true values
- "bias": The mean difference between the imputed and the true values
- "cor": The correlation between the imputed and true values
- "MAE": The Mean Absolute Error between the imputed and true values
- "MSE": The Mean Squared Error between the imputed and true values
- "NRMSE\_col\_mean": For every column the RMSE divided by the mean of the true values is calculated. Then these columnwise values are squared and averaged. Finally, the square root of this average is returned.
- "NRMSE\_col\_mean\_sq": For every column the RMSE divided by the square root of the mean of the squared true values is calculated. Then these columnwise values are squared and averaged. Finally, the square root of this average is returned.
- "NRMSE\_col\_sd": For every column the RMSE divided by the standard deviation of all true values is calculated. Then these columnwise values are squared and averaged. Finally, the square root of this average is returned.
- "NRMSE\_tot\_mean": RMSE divided by the mean of all true values
- "NRMSE\_tot\_mean\_sq": RMSE divided by the square root of the mean of all squared true values

- "NRMSE\_tot\_sd": RMSE divided by the standard deviation of all true values
- "nr\_equal": number of imputed values that are equal to the true values
- "nr\_NA": number of values in ds\_imp that are NA (not imputed)
- "precision": proportion of imputed values that are equal to the true values

Additionally there are relative versions of bias and MAE implemented. In the relative versions, the differences are divided by the absolute values of the true values. These relative versions can be selected via "bias\_rel" and "MAE\_rel". The "NRMSE\_tot\_" and "NRMSE\_col\_" are equal, if the columnwise normalization values are equal to the total normalization value (see examples).

The argument cols\_which allows the selection of columns for comparison (see examples).

If M = NULL (the default), then all values of ds\_imp and ds\_orig will be used for the calculation of the evaluation criterion. If a missing data indicator matrix is given via M, only the truly imputed values (values that are marked as missing via M) will be used for the calculation. If you want to provide M, M must be a logical matrix of the same dimensions as ds\_orig and missing values must be coded as TRUE. This is the standard behavior, if you use is.na on a dataset with missing values to generate M (see examples). It is possible to combine M and cols\_which.

## Value

A numeric vector of length one.

#### References

Kim, H., Golub, G. H., & Park, H. (2005). Missing value estimation for DNA microarray gene expression data: local least squares imputation. *Bioinformatics*, 21(2), 187-198.

#### See Also

Other evaluation functions: evaluate\_imputation\_parameters(), evaluate\_parameters()

## **Examples**

```
ds_{orig} \leftarrow data.frame(X = 1:10, Y = 101:110)
ds_mis <- delete_MCAR(ds_orig, 0.3)</pre>
ds_imp <- impute_mean(ds_mis)</pre>
# compare all values from ds_orig and ds_imp
evaluate_imputed_values(ds_imp, ds_orig)
# compare only the imputed values
M <- is.na(ds_mis)
evaluate_imputed_values(ds_imp, ds_orig, M = M)
# compare only the imputed values in column X
evaluate_imputed_values(ds_imp, ds_orig, M = M, cols_which = "X")
# NRMSE_tot_mean and NRMSE_col_mean are equal, if columnwise means are equal
ds\_orig \leftarrow data.frame(X = 1:10, Y = 10:1)
ds_mis <- delete_MCAR(ds_orig, 0.3)</pre>
ds_imp <- impute_mean(ds_mis)</pre>
evaluate_imputed_values(ds_imp, ds_orig, "NRMSE_tot_mean")
evaluate_imputed_values(ds_imp, ds_orig, "NRMSE_col_mean")
```

28 evaluate\_parameters

evaluate\_parameters

Evaluate estimated parameters

## **Description**

Compare estimated parameters to true parameters

## Usage

```
evaluate_parameters(
  pars_est,
  pars_true,
  criterion = "RMSE",
  tolerance = sqrt(.Machine$double.eps),
  est_pars,
  true_pars
)
```

## **Arguments**

pars_est	A vector or matrix of estimated parameters.
pars_true	True parameters, normally a vector or a matrix.
	A string specifying the used criterion for comparing the imputed and original values.
	Numeric, only used for criterion = "precision": numeric differences smaller than tolerance are treated as zero/equal.
est_pars	Deprecated, renamed to pars_est.
true_pars	Deprecated, renamed to pars_true.

## **Details**

The same criterions are implemented for evaluate\_parameters and evaluate\_imputed\_values. The possible choices are documented in evaluate\_imputed\_values.

## Value

A numeric vector of length one.

## References

Cetin-Berber, D. D., Sari, H. I., & Huggins-Manley, A. C. (2019). Imputation Methods to Deal With Missing Responses in Computerized Adaptive Multistage Testing. *Educational and psychological measurement*, 79(3), 495-511.

## See Also

Other evaluation functions: evaluate\_imputation\_parameters(), evaluate\_imputed\_values()

impute\_EM 29

## **Examples**

```
evaluate_parameters(1:4, 2:5, "RMSE")
```

impute\_EM

EM imputation

## **Description**

Impute missing values in a data frame or a matrix using parameters estimated via EM

## Usage

```
impute_EM(
   ds,
   stochastic = TRUE,
   maxits = 1000,
   criterion = 1e-04,
   verbose = FALSE
)
```

## **Arguments**

ds A data frame or matrix with missing values.

stochastic Logical; see details.

maxits Maximum number of iterations for the EM, passed to norm::em.norm().

criterion If maximum relative difference in parameter estimates is below this threshold,

the EM algorithm stops. Argument is directly passed to norm::em.norm().

verbose Should messages be given for special cases (see details)?

#### **Details**

At first parameters are estimated via norm::em.norm(). Then these parameters are used in regression like models to impute the missing values. If stochachstic = FALSE, the expected values (given the observed values and the estimated parameters via EM) are imputed for the missing values of an object. If stochastic = TRUE, residuals from a multivariate normal distribution are added to these expected values.

If all values in a row are NA or the required part of the covariance matrix for the calculation of the expected values is not invertible, parts of the estimated mean vector will be imputed. If stochastic = TRUE, residuals will be added to these values. If verbose = TRUE, a message will be given for these rows.

#### Value

An object of the same class as ds with imputed missing values.

The number of EM iterations are added as an attribute (iterations).

## See Also

- norm::em.norm(), which estimates the parameters
- impute\_expected\_values(), which calculates the imputation values

## **Examples**

```
ds_orig <- mvtnorm::rmvnorm(100, rep(0, 7))
ds_mis <- delete_MCAR(ds_orig, p = 0.2)
ds_imp <- impute_EM(ds_mis, stochastic = FALSE)</pre>
```

impute\_expected\_values

Impute expected values

# Description

Impute the missing values with expected values given the observed values and estimated parameters assuming a multivariate normal distribution

# Usage

```
impute_expected_values(
   ds,
   mu,
   S,
   stochastic = FALSE,
   M = is.na(ds),
   verbose = FALSE
)
```

## **Arguments**

ds A data frame or matrix with missing values.

mu Vector of means for the variables.S Covariance matrix of the variables.

stochastic Logical, should residuals be added to the expected values.

Missing data indicator matrix.

verbose Should messages be given for special cases (see details)?

#### **Details**

Normally, this function is called by other imputation function and should not be called directly. The function imputes the missing values assuming a multivariate normal distribution. This is equivalent to imputing the least squares estimate of the missing values in some kind of way.

If no values is observed in a row or a relevant submatrix of the covariance matrix (S\_22) is not invertible, the missing values are imputed with (parts of) mu (plus a residuum, if stochastich = TRUE). If verbose = TRUE, these cases will be listed in a message. Otherwise, they will be imputed silently.

#### Value

An object of the same class as ds with imputed missing values.

#### **Examples**

```
ds_orig <- mvtnorm::rmvnorm(100, rep(0, 2))
ds_mis <- delete_MCAR(ds_orig, p = 0.2)
# impute using true parameters:
ds_imp <- impute_expected_values(ds_mis, mu = c(0, 0), diag(1, 2))</pre>
```

```
impute_hot_deck_in_classes
```

Hot deck imputation in imputation classes

## **Description**

Impute missing values in a data frame or a matrix using a hot deck within imputation classes

```
impute_hot_deck_in_classes(
   ds,
   cols_class,
   type = "cols_seq",
   breaks = Inf,
   use_quantiles = FALSE,
   min_objs_in_class = 1,
   min_obs_comp = 0,
   min_obs_per_col = 1,
   donor_limit = Inf,
   add_imputation_classes = FALSE
)
```

#### **Arguments**

ds A data frame or matrix with missing values.

cols\_class Columns that are used for constructing the imputation classes.

The type of hot deck (for details, see impute\_sRHD()).

breaks Number of intervals / levels a column is broken into (see cut(), which is used

internally for cutting numeric columns). If breaks = Inf (the default), every unique value of a column can be in a separate class (if no other restrictions

apply).

use\_quantiles Should quantiles be used for cutting numeric vectors? Normally, cut() divides

the range of an vector into equal spaced intervals. If use\_quantiles = TRUE,

the classes will be of roughly equal content.

min\_objs\_in\_class

Minimum number of objects (rows) in an imputation class.

min\_obs\_comp Minimum number of completely observed objects (rows) in an imputation class.

min\_obs\_per\_col

Minimum number of observed values in every column of an imputation class.

donor\_limit Minimum odds between incomplete and complete values in a column, if type =

cols\_seq. If type = sim\_comp, minimum odds between incomplete and complete rows. For type = sim\_part the donor limit option is not implemented and

donor\_limit should be Inf.

add\_imputation\_classes

Should imputation classes be added as attributes to the imputed dataset?

## **Details**

This function is a combination of impute\_in\_classes() and impute\_sRHD(). It applies impute\_sRHD() inside of imputation classes (adjustment cells), which are constructed via impute\_in\_classes(). More details can be found in these two functions.

#### Value

An object of the same class as ds with imputed missing values.

#### References

Andridge, R.R. and Little, R.J.A. (2010), A Review of Hot Deck Imputation for Survey Non-response. International Statistical Review, 78: 40-64. doi:10.1111/j.1751-5823.2010.00103.x

#### See Also

impute\_in\_classes(), which is used for the construction of the imputation classes.

impute\_sRHD(), which is used for the imputation.

impute\_in\_classes 33

## **Examples**

```
impute_hot_deck_in_classes(data.frame(
    X = c(rep("A", 10), rep("B", 10)),
    Y = c(rep(NA, 5), 106:120)
),
    "X",
donor_limit = 1
)
```

impute\_in\_classes

Impute in classes

## **Description**

Apply an imputation function inside imputation classes

# Usage

```
impute_in_classes(
    ds,
    cols_class,
    FUN,
    breaks = Inf,
    use_quantiles = FALSE,
    min_objs_in_class = 1,
    min_obs_comp = 0,
    min_obs_per_col = 1,
    donor_limit = Inf,
    dl_type = "cols_seq",
    add_imputation_classes = FALSE,
    ...
)
```

## **Arguments**

ds A data frame or matrix with missing values.

cols\_class Columns that are used for constructing the imputation classes.

FUN An imputation function that is applied to impute the missing values.

breaks Number of intervals / levels a column is broken into (see cut(), which is used

internally for cutting numeric columns). If breaks = Inf (the default), every unique value of a column can be in a separate class (if no other restrictions

apply).

use\_quantiles Should quantiles be used for cutting numeric vectors? Normally, cut() divides

the range of an vector into equal spaced intervals. If  $use\_quantiles = TRUE$ ,

the classes will be of roughly equal content.

```
min_objs_in_class

Minimum number of objects (rows) in an imputation class.

min_obs_comp

Minimum number of completely observed objects (rows) in an imputation class.

min_obs_per_col

Minimum number of observed values in every column of an imputation class.

donor_limit

Minimum odds between incomplete and complete values in a column, if dl_type = cols_seq. If dl_type = sim_comp, minimum odds between incomplete and complete rows.

dl_type

See donor_limit.

add_imputation_classes

Should imputation classes be added as attributes to the imputed dataset?
```

#### **Details**

Imputation classes (sometimes also called adjustment cells) are build using cross-validation of all cols\_class. The classes are collapsed, if they do not satisfy all of the criteria defined by min\_objs\_in\_class, min\_obs\_comp, min\_obs\_per\_col and donor\_limit. Collapsing starts from the last value of cols\_class. Internally, a mixture of collapsing and early stopping is used for the construction of the classes.

#### Value

An object of the same class as ds with imputed missing values.

Arguments passed to FUN.

## References

Andridge, R.R. and Little, R.J.A. (2010), A Review of Hot Deck Imputation for Survey Non-response. International Statistical Review, 78: 40-64. doi:10.1111/j.1751-5823.2010.00103.x

## **Examples**

```
# Mean imputation in classes
impute_in_classes(data.frame(X = 1:5, Y = c(NA, 12:15)), "X",
   impute_mean,
   min_obs_per_col = 2
)
```

impute\_LS\_adaptive

LSimpute\_adaptive

## **Description**

Perform LSimpute\_adaptive as described by Bo et al. (2004)

impute\_LS\_adaptive 35

## Usage

```
impute_LS_adaptive(
   ds,
   k = 10,
   eps = 1e-06,
   min_common_obs = 5,
   r_max_min = 100,
   p_mis_sim = 0.05,
   warn_r_max = FALSE,
   verbose_gene = FALSE,
   verbose_array = FALSE,
   verbose_array_p = FALSE))
```

## **Arguments**

ds	A data frame or matrix with missing values.
k	Directly passed to impute_LS_gene().
eps	Directly passed to impute_LS_gene().
min_common_obs	Directly passed to impute_LS_gene().
r_max_min	Minimum number of nearest genes used for imputation. The default value (100) corresponds to the choice of Bo et al. (2004).
p_mis_sim	Percentage of observed values that are set NA to estimate the mixing coefficient $p$ . The default value (0.05) corresponds to the choice of Bo et al. (2004).
warn_r_max	Should a warning be given, if r_max_min is set too high?
verbose_gene	Should impute_LS_gene() be verbose?
verbose_array	Should impute_LS_array() be verbose?
verbose_gene_p	Should impute_LS_gene() be verbose while estimating $p$ ?
verbose_array_p	0
	Should impute_LS_array() be verbose while estimating $p$ ?

#### **Details**

This function performs LSimpute\_adaptive as described by Bo et al. (2004). The function assumes that the genes are the rows of ds.

LSimpute\_adaptive combines imputation values from  $impute_LS_gene()$  and  $impute_LS_array()$  using a local (adaptive) approach for the mixing coefficient p.

If the dataset is too small or has too many missing values, there are some fallback systems implemented. First, if ncol(ds) <= min\_common\_obs (normally, this should not the case!), values are imputed through impute\_LS\_array(). Second, r\_max\_min is automatically adjusted, if it is too high. In this case, a warning will be given, if warn\_r\_max = TRUE. Third, if there are not enough observed values in a row (less than min\_common\_obs), the calculation of the mixing coefficient is not possible and missing values of these rows are imputed with the values from impute\_LS\_array().

impute\_LS\_array

The amount of feedback given from impute\_LS\_gene() and impute\_LS\_array() is controlled via verbose\_gene, verbose\_array, verbose\_gene\_p and verbose\_array\_p. The last two control the amount of feedback while estimating p and the first two the amount of feedback during the estimation of the values that are mixed with p. Internally, the imputed dataset from impute\_LS\_gene() is passed on to impute\_LS\_array(). Therefore, all messages from impute\_LS\_gene() are truly from impute\_LS\_gene() and not a part of impute\_LS\_array(), which never calls impute\_LS\_gene() in this case. Furthermore, all messages from impute\_expected\_values() belong to impute\_LS\_array().

#### Value

An object of the same class as ds with imputed missing values.

#### References

Bo, T. H., Dysvik, B., & Jonassen, I. (2004). LSimpute: accurate estimation of missing values in microarray data with least squares methods. Nucleic acids research, 32(3), e34

#### See Also

```
Other LSimpute functions: impute_LS_array(), impute_LS_combined(), impute_LS_gene()
```

## **Examples**

```
set.seed(123)
ds_mis <- delete_MCAR(mvtnorm::rmvnorm(100, rep(0, 10)), 0.1)
ds_imp <- impute_LS_adaptive(ds_mis)</pre>
```

impute\_LS\_array

LSimpute\_array

## **Description**

Perform LSimpute\_array as described by Bo et al. (2004)

```
impute_LS_array(
   ds,
   k = 10,
   eps = 1e-06,
   min_common_obs = 5,
   ds_impute_LS_gene = NULL,
   verbose_gene = FALSE,
   verbose_expected_values = FALSE
)
```

impute\_LS\_array 37

# Arguments

```
ds A data frame or matrix with missing values.

k Directly passed to impute_LS_gene().

eps Directly passed to impute_LS_gene().

min_common_obs Directly passed to impute_LS_gene().

ds_impute_LS_gene

Result of imputing ds with ds_impute_LS_gene(), if this already exists (see details).

verbose_gene Should impute_LS_gene() be verbose?

verbose_expected_values

Should impute_expected_values() be verbose?
```

# **Details**

This function performs LSimpute\_array as described by Bo et al. (2004). The function assumes that the genes are the rows of ds.

The mean vector and covariance matrix for the imputation in LSimpute\_array is based on a imputed dataset from LSimpute\_gene. This dataset can be supplied directly via ds\_impute\_LS\_gene or will automatically be created with impute\_LS\_gene() (if ds\_impute\_LS\_gene is NULL). The imputation values are the expected values given the estimated parameters and the observed values. They are calculated via impute\_expected\_values(). The amount of feedback from these two functions is controlled via verbose\_gene and verbose\_expected\_values. The values of these two arguments are passed on to the argument verbose from impute\_LS\_gene() and impute\_expected\_values().

## Value

An object of the same class as ds with imputed missing values.

## References

Bo, T. H., Dysvik, B., & Jonassen, I. (2004). LSimpute: accurate estimation of missing values in microarray data with least squares methods. Nucleic acids research, 32(3), e34

# See Also

```
Other LSimpute functions: impute_LS_adaptive(), impute_LS_combined(), impute_LS_gene()
```

# **Examples**

```
set.seed(123)
ds_mis <- delete_MCAR(mvtnorm::rmvnorm(100, rep(0, 10)), 0.1)
ds_imp <- impute_LS_array(ds_mis)</pre>
```

# **Description**

Perform LSimpute\_combined as described by Bo et al. (2004)

# Usage

```
impute_LS_combined(
   ds,
   k = 10,
   eps = 1e-06,
   min_common_obs = 5,
   p_mis_sim = 0.05,
   verbose_gene = FALSE,
   verbose_array = FALSE,
   verbose_array_p = FALSE)
```

# **Arguments**

```
A data frame or matrix with missing values.
ds
k
                 Directly passed to impute_LS_gene().
                 Directly passed to impute_LS_gene().
eps
min_common_obs Directly passed to impute_LS_gene().
                 Percentage of observed values that are set NA to estimate the mixing coefficient
p_mis_sim
                 p. The default value (0.05) corresponds to the choice of Bo et al. (2004).
                 Should impute_LS_gene() be verbose?
verbose_gene
                 Should impute_LS_array() be verbose?
verbose_array
verbose_gene_p Should impute_LS_gene() be verbose while estimating p?
verbose_array_p
                 Should impute_LS_array() be verbose while estimating p?
```

#### **Details**

This function performs LSimpute\_combined as described by Bo et al. (2004). The function assumes that the genes are the rows of ds.

LSimpute\_combined combines imputation values from impute\_LS\_gene() and impute\_LS\_array() using a global approach for the mixing coefficient p. The amount of feedback given from these underlying functions is controlled via verbose\_gene, verbose\_array, verbose\_gene\_p, verbose\_array\_p. The last two control the amount of feedback while estimating p and the first two the amount of feedback during the estimation of the values that are mixed with p. Internally, the imputed

impute\_LS\_gene 39

dataset from impute\_LS\_gene() is passed on to impute\_LS\_array(). Therefore, all messages from impute\_LS\_gene() are truly from impute\_LS\_gene() and not a part of impute\_LS\_array(), which never calls impute\_LS\_gene() in this case. Furthermore, all messages from impute\_expected\_values() belong to impute\_LS\_array().

#### Value

An object of the same class as ds with imputed missing values.

#### References

Bo, T. H., Dysvik, B., & Jonassen, I. (2004). LSimpute: accurate estimation of missing values in microarray data with least squares methods. Nucleic acids research, 32(3), e34

# See Also

```
Other LSimpute functions: impute_LS_adaptive(), impute_LS_array(), impute_LS_gene()
```

# Examples

```
set.seed(123)
ds_mis <- delete_MCAR(mvtnorm::rmvnorm(100, rep(0, 10)), 0.1)
ds_imp <- impute_LS_combined(ds_mis)</pre>
```

impute\_LS\_gene

LSimpute\_gene

# **Description**

Perform LSimpute\_gene as described by Bo et al. (2004)

# Usage

```
impute_LS_gene(
   ds,
   k = 10,
   eps = 1e-06,
   min_common_obs = 5,
   return_r_max = FALSE,
   verbose = FALSE
)
```

40 impute\_LS\_gene

#### **Arguments**

ds	A data frame or matrix with missing values.
k	Number of most correlated genes used for the imputation of a gene.
eps	Used in the calculation of the weights (Bo et al. (2004) used eps = 1e-6).
min_common_obs	A row can only take part in the imputation of another row, if both rows share at least min_common_obs columns with no missing values.
return_r_max	Logical; normally, this should be FALSE. TRUE is used inside of impute_LS_adaptive() to speed up some computations.

verbose Should messages be given for special cases (see details)?

#### Details

This function performs LSimpute\_gene as described by Bo et al. (2004). The function assumes that the genes are the rows of ds.

Bo et al. (2004) seem to have chosen min\_common\_obs = 5. However, they did not document this behavior. This value emerged from inspecting imputation results from the original jar-file, which is provided by Bo et al. (2004).

If there are less than min\_common\_obs observed values in a row and at least one observed value, the mean of the observed row values is imputed. If no value is observed in a row, the observed column means are imputed for the missing row values. This is the only known difference between this function and the original one from Bo et al. (2004). The original function would not impute such a row and return a dataset with missing values in this row. There is one more case that needs a special treatment: If no suitable row can be found to impute a row, the mean of the observed values is imputed, too. If verbose = TRUE, a message will be given for the encountered instances of the described special cases. If verbose = FALSE, the function will deal with these cases silently.

## Value

An object of the same class as ds with imputed missing values.

If  $return_r_max = TRUE$ , a list with the imputed dataset and  $r_max$ .

# References

Bo, T. H., Dysvik, B., & Jonassen, I. (2004). LSimpute: accurate estimation of missing values in microarray data with least squares methods. Nucleic acids research, 32(3), e34

## See Also

```
Other LSimpute functions: impute_LS_adaptive(), impute_LS_array(), impute_LS_combined()
```

## **Examples**

```
set.seed(123)
ds_mis <- delete_MCAR(mvtnorm::rmvnorm(100, rep(0, 10)), 0.1)
ds_imp <- impute_LS_gene(ds_mis)</pre>
```

impute\_mean 41

## Description

Impute an observed mean for the missing values

# Usage

```
impute_mean(ds, type = "columnwise", convert_tibble = TRUE)
```

# **Arguments**

ds A data frame or matrix with missing values.

type A string specifying the values used for imputation; one of: "columnwise", "row-

wise", "total", "Two-Way" or "Winer" (see details).

convert\_tibble If ds is a tibble, should it be converted (see section A note for tibble users).

#### **Details**

For every missing value the mean of some observed values is imputed. The observed values to be used are specified via type. For example, type = "columnwise" (the default) imputes the mean of the observed values in a column for all missing values in the column. This is normally meant, if someone speaks of "imputing the mean" or "mean imputation".

Other options for type are: "rowwise", "total", "Winer" and "Two-way". The option "rowwise" imputes all missing values in a row with the mean of the observed values in the same row. "total" will impute every missing value with the mean of all observed values in ds. "Winer" imputes the mean of the rowwise and columnwise mean. Beland et al. (2016) called this method "Winer" and they attributed the method to Winer (1971). "Two-way" imputes the sum of rowwise and columnwise mean minus the total mean. This method was suggested by D.B Rubin to Bernaards & Sijtsma, K. (2000).

## Value

An object of the same class as ds with imputed missing values.

## A note for tibble users

If you use tibbles and convert\_tibble is TRUE the tibble is first converted to a data frame, then imputed and converted back. If convert\_tibble is FALSE no conversion is done. However, depending on the tibble and the package version of tibble you use, imputation may not be possible and some errors will be thrown.

42 impute\_median

#### References

Beland, S., Pichette, F., & Jolani, S. (2016). Impact on Cronbach's  $\alpha$  of simple treatment methods for missing data. *The Quantitative Methods for Psychology*, 12(1), 57-73.

Bernaards, C. A., & Sijtsma, K. (2000). Influence of imputation and EM methods on factor analysis when item nonresponse in questionnaire data is nonignorable. *Multivariate Behavioral Research*, 35(3), 321-364.

Winer, B. J. (1971). Statistical principles in experimental design (2ed ed.) New York: McGraw-Hill

# See Also

```
apply_imputation the workhorse for this function.
```

Other location parameter imputation functions: impute\_median(), impute\_mode()

# **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
ds_mis <- delete_MCAR(ds, 0.2)
ds_imp <- impute_mean(ds_mis)
# completely observed columns can be of any type:
ds_mis_char <- cbind(ds_mis, letters[1:20])
ds_imp_char <- impute_mean(ds_mis_char)</pre>
```

impute\_median

Median imputation

# Description

Impute an observed median value for every missing value

#### Usage

```
impute_median(
   ds,
   type = "columnwise",
   ordered_low = FALSE,
   convert_tibble = TRUE
)
```

# **Arguments**

ds A data frame or matrix with missing values.

type A string specifying the values used for imputation; one of: "columnwise", "row-

wise", "total", "Two-Way" or "Winer" (see details).

ordered\_low Logical; used for the calculation of the median from ordered factors (for details

see: median.factor).

convert\_tibble If ds is a tibble, should it be converted (see section A note for tibble users).

impute\_mode 43

#### **Details**

This function behaves exactly like <code>impute\_mean</code>. The only difference is that it imputes a median instead of a mean. All types from <code>impute\_mean</code> are also implemented for <code>impute\_median</code>. They are documented in <code>impute\_mean</code> and <code>apply\_imputation</code>. The function median is used for the calculation of the median values for imputation.

# Value

An object of the same class as ds with imputed missing values.

## A note for tibble users

If you use tibbles and convert\_tibble is TRUE the tibble is first converted to a data frame, then imputed and converted back. If convert\_tibble is FALSE no conversion is done. However, depending on the tibble and the package version of tibble you use, imputation may not be possible and some errors will be thrown.

#### References

Beland, S., Pichette, F., & Jolani, S. (2016). Impact on Cronbach's  $\alpha$  of simple treatment methods for missing data. *The Quantitative Methods for Psychology*, 12(1), 57-73.

#### See Also

```
apply_imputation the workhorse for this function.
median, median.factor
Other location parameter imputation functions: impute_mean(), impute_mode()
```

# **Examples**

```
ds <- data.frame(X = 1:20, Y = ordered(LETTERS[1:20]))
ds_mis <- delete_MCAR(ds, 0.2)
ds_imp <- impute_median(ds_mis)
# completely observed columns can be of any type:
ds_mis_char <- cbind(ds_mis, letters[1:20])
ds_imp_char <- impute_median(ds_mis_char)</pre>
```

impute\_mode

Mode imputation

## **Description**

Impute an observed mode value for every missing value

# Usage

```
impute_mode(ds, type = "columnwise", convert_tibble = TRUE)
```

44 impute\_sRHD

# Arguments

ds A data frame or matrix with missing values.

type A string specifying the values used for imputation; one of: "columnwise", "row-

wise", "total", "Two-Way" or "Winer" (see details).

convert\_tibble If ds is a tibble, should it be converted (see section A note for tibble users).

#### **Details**

This function behaves exactly like impute\_mean. The only difference is that it imputes a mode instead of a mean. All types from impute\_mean are also implemented for impute\_mode. They are documented in impute\_mean and apply\_imputation.

A mode value of a vector x is a most frequent value of x. If this value is not unique, the first occurring mode value in x will be used as imputation value.

#### Value

An object of the same class as ds with imputed missing values.

# References

Beland, S., Pichette, F., & Jolani, S. (2016). Impact on Cronbach's  $\alpha$  of simple treatment methods for missing data. *The Quantitative Methods for Psychology*, 12(1), 57-73.

#### See Also

```
apply_imputation the workhorse for this function.
```

Other location parameter imputation functions: impute\_mean(), impute\_median()

# **Examples**

```
ds <- data.frame(X = c(1:12, rep(8, 8)), Y = 101:120)
ds_mis <- delete_MCAR(ds, 0.2)
ds_imp <- impute_mode(ds_mis)
```

impute\_sRHD

Simple random hot deck imputation

# **Description**

Impute missing values in a data frame or a matrix using a simple random hot deck

# Usage

```
impute_sRHD(ds, type = "cols_seq", donor_limit = Inf)
```

impute\_sRHD 45

## **Arguments**

ds A data frame or matrix with missing values.

type The type of hot deck; the default ("cols\_seq") is a random hot deck that imputes

each column separately. Other choices are "sim\_comp" and "sim\_part". Both impute all missing values in an object (row) simultaneously using a single donor object. The difference between the two types is the choice of objects that can act as donors. "sim\_comp:" only completely observed objects can be donors. "sim\_part": all objects that have no missing values in the missing parts of a

recipient can be donors.

donor\_limit Numeric of length one or "min"; how many times an object can be a donor.

Default is Inf (no restriction).

#### **Details**

There are three types of simple random hot decks implemented. They can be selected via type:

- "cols\_seq" (the default): Each variable (column) is handled separately. If an object (row) has a missing value in a variable (column), then one of the observed values in the same variable is chosen randomly and the missing value is replaced with this chosen value. This is done for all missing values.
- "sim\_comp": All missing variables (columns) of an object are imputed together ("simultaneous"). For every object with missing values (such an object is called a recipient in hot deck terms), one complete object is chosen randomly and all missing values of the recipient are imputed with the values from the complete object. A complete object used for imputation is called a donor.
- "sim\_part": All missing variables (columns) of an object are imputed together ("simultaneous"). For every object with missing values (recipient) one donor is chosen. The donor must have observed values in all the variables that are missing in the recipient. The donor is allowed to have unobserved values in the non-missing parts of the recipient. So, in contrast to "sim\_comp", the donor can be partly incomplete.

The parameter donor\_limit controls how often an object can be a donor. This parameter is only implemented for types "cols\_seq" and "sim\_comp". If type = "sim\_part" and donor\_limit is not Inf, then an error will be thrown. For "sim\_comp" the default value (Inf) allows every object to be a donor for an infinite number of times (there is no restriction on the times an object can be a donor). If a numeric value less than Inf is chosen, then every object can be a donor at most donor\_limit times. For example donor\_limit = 1 ensures that every object donates at most one time. If there are only few complete objects and donor\_limit is set too low, then an imputation might not be possible with the chosen donor\_limit. In this case, the donor\_limit will be adjusted (see examples). Setting donor\_limit = "min" chooses automatically the minimum value for donor\_limit that allows imputation of all missing values. For type = "cols\_seq" the donor limit is applied for every column separately.

#### Value

An object of the same class as ds with imputed missing values.

46 median.factor

#### References

Andridge, R. R., & Little, R. J. (2010). A review of hot deck imputation for survey non-response. *International statistical review*, 78(1), 40-64.

## **Examples**

```
ds <- data.frame(X = 1:20, Y = 101:120)
ds_mis <- delete_MCAR(ds, 0.2)
ds_imp <- impute_sRHD(ds_mis)

# Warning: donor limit to low
ds_mis_one_donor <- ds
ds_mis_one_donor[1:19, "X"] <- NA
impute_sRHD(ds_mis_one_donor, donor_limit = 3)</pre>
```

median.factor

Median for ordered factors

# **Description**

Compute the median of an ordered factor

# Usage

```
## S3 method for class 'factor'
median(x, na.rm = FALSE, ordered_low = FALSE, ...)
```

#### **Arguments**

x An ordered factor (for unordered factors an error will be thrown).

na.rm Logical; should NA be removed before computation?

ordered\_low Logical; only used if the length of x is even and the two middle values are

unequal (see details).

... Not used in this function.

#### **Details**

Currently, the median for an ordered factor is not implemented in base R. This function is a remedy for this. It allows the computation of "a median" for ordered factors (see below) and overwrites the error message for unordered factors from median.default (hence, the function name is median.factor and not median.ordered).

If the length of x is odd, then the median will be the middle value of the sorted list of elements from x. If the length of x is even and the two middle values of the sorted list of elements from x are equal, then the median is one of these (equal) middle values. The only problematic case is an even length x with unequal middle values. In this case, the median of a numeric vector is normally defined as the

median.factor 47

mean of the two middle values. However, for ordered factors the mean is not defined. The argument ordered\_low cures this problem. If ordered\_low = FALSE (the default), then the larger of the two middle values is returned (this value is called 'hi-median' in mad). If ordered\_low = TRUE, then the smaller of the two middle values is returned (this value is called 'low-median' in mad).

# Value

a length-one factor

# **Examples**

```
ord_factor_odd <- ordered(letters[1:5])
median(ord_factor_odd) # calls median.factor, if package is loaded
# If only base R is loaded, median.default will be called
# and will throw an error:
tryCatch(median.default(ord_factor_odd), error = function(e) e)

ord_factor_even <- ordered(letters[1:4])
median(ord_factor_even, ordered_low = FALSE)
median(ord_factor_even, ordered_low = TRUE)</pre>
```

# **Index**

* LSimpute functions	evaluate_imputation_parameters, 23, 27, 28
<pre>impute_LS_adaptive, 34 impute_LS_array, 36 impute_LS_combined, 38</pre>	evaluate_imputed_values, 24, 25, 25, 28 evaluate_parameters, 25, 27, 28
<pre>impute_LS_gene, 39 * evaluation functions     evaluate_imputation_parameters, 23     evaluate_imputed_values, 25     evaluate_parameters, 28 * functions to create MAR     delete_MAR_1_to_x, 5     delete_MAR_censoring, 8</pre>	<pre>impute_EM, 29 impute_expected_values, 30 impute_expected_values(), 30, 36, 37, 39 impute_hot_deck_in_classes, 31 impute_in_classes, 33 impute_in_classes(), 32 impute_LS_adaptive, 34, 37, 39, 40</pre>
delete_MAR_one_group, 11 delete_MAR_rank, 13 * functions to create MNAR delete_MNAR_1_to_x, 17 delete_MNAR_censoring, 19 delete_MNAR_one_group, 20 delete_MNAR_rank, 22 * location parameter imputation functions impute_mean, 41 impute_median, 42	impute_LS_array, 36, 36, 39, 40 impute_LS_array(), 35, 38 impute_LS_combined, 36, 37, 38, 40 impute_LS_gene, 36, 37, 39, 39 impute_LS_gene(), 35, 37, 38 impute_mean, 4, 41, 43, 44 impute_median, 4, 42, 42, 44 impute_mode, 4, 42, 43, 43 impute_sRHD, 44 impute_sRHD(), 32 is.na, 27
<pre>impute_mode, 43  apply, 3 apply_imputation, 2, 42-44</pre>	mad, 47 median, 43 median.default, 46 median.factor, 42, 43, 46
count_NA, 4 cut(), 32, 33	norm::em.norm(), 29, 30
delete_MAR_1_to_x, 5, 10, 13, 15, 18 delete_MAR_censoring, 8, 8, 13, 15, 19, 20 delete_MAR_one_group, 8, 10, 11, 15, 21 delete_MAR_rank, 8, 10, 13, 13, 23 delete_MCAR, 15 delete_MNAR_1_to_x, 8, 17, 20, 21, 23 delete_MNAR_censoring, 10, 18, 19, 21, 23 delete_MNAR_one_group, 13, 18, 20, 20, 23	quantile, 10, 24 rank, 14, 15, 22 sample, 7, 14
delete_MNAR_rank, 15, 18, 20, 21, 22	