Package 'mpr'

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Description Fitting Multi-Parameter Regression (MPR) models to right-censored survival data. These are flexible parametric regression models which extend standard models, for example, proportional hazards. See Burke & MacKenzie (2016) <doi:10.1111 biom.12625=""> and Burke et al (2020) <doi:10.1111 rssc.12398="">.</doi:10.1111></doi:10.1111>
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addterm	All Possible Single-Term Additions to / Deletions from a Multi-
	Parameter Regression (MPR) Model

Description

Identifies all models which arise via single-term additions to / deletions from a component (or, simultaneously, multiple components) of the supplied mpr model, fits all such models and summarises these models in a table.

Usage

Arguments

٤	Suments	
	object	an object of class "mpr" which is the result of a call to mpr.
	upper	a one-sided formula (used in add term) specifying a maximal model which must include the current one. $ \\$
	lower	a one-sided formula (used in dropterm) specifying a minimal model which must be within the current one.
	comp	a numeric value (or vector) indicating the regression component (or components) where (simultaneous) additions / deletions occur. Note that "1" = λ , "2" = γ and "3" = ρ . For more information on the various components, see mpr and distributions.
	aic	logical. If TRUE, AIC is used as the basis for determining the best model among those considered. If FALSE, BIC is used.
	bestmodel	an initial best model which, by default, is the supplied current model. This argument is used within the stepmpr function but is unlikely to be used directly by the end user.
		additional arguments to be passed to internal methods.

Details

The hierarchy is respected when considering terms to be added or dropped, e.g., all main effects contained in a second-order interaction must remain.

When using addterm, the terms in the upper model formula must be a *superset* of the terms for each regression component indicated by comp. For example, if component 1 is \sim a + b + c and component 2 is \sim a + b (and terms are to be added to both simultaneously, i.e., comp=1:2), then upper = \sim a + b + c + d is acceptable and means that the variable d will be added simultaneously to components 1 and 2 (this can be written more compactly as upper = \sim . + d). On the other hand, \sim a + b + d is not

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acceptable since its terms do not form a superset of the terms in component 1 (however, this would be acceptable if we were only considering component 2, i.e., if comp=2).

When using dropterm, the terms in the lower model formula must be a *subset* of the terms for each regression component indicated by comp. Again, if component 1 is \sim a + b + c and component 2 is \sim a + b (and terms are to be dropped from both simultaneously, i.e., comp=1:2), then lower = \sim a is acceptable and means that the variable b will be dropped simultaneously from components 1 and 2 (this can be written more compactly as lower = \sim . - b). On the other hand, \sim c is not acceptable since its terms do not form a subset of the terms in component 2 (however, this would be acceptable if we were only considering component 1, i.e., if comp=1).

To summarise the above two paragraphs, the upper formula must *contain* each formula corresponding to the components under consideration whereas the lower formula must *be contained within* each of these formulae.

Value

A list containing the following components:

modeltab a table containing information about each of the fitted models. This information

comes from the "model" element of each of the mpr objects - see mpr for details.

 $\besit{the model with the lowest AIC (or BIC if aic = FALSE) among the fitted models} \\$

including the initial bestmodel passed to the addterm / dropterm function.

Author(s)

Kevin Burke.

See Also

```
mpr, stepmpr, update.mpr.
```

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```
dropterm(mod2, ~ 1, comp=1)$modeltab
dropterm(mod2, ~ 1, comp=2)$modeltab

# does nothing since celltype is only in component 1
dropterm(mod2, ~ . - celltype, comp=1:2)$modeltab

# removes celltype from component 1
dropterm(mod2, ~ . - celltype, comp=1)$modeltab
```

Distributions

Distributions in the mpr Package

Description

Information on the distributions currently available within the mpr package.

Details

When fitting a Multi-Parameter Regression (MPR) model to data, the underlying distribution is selected using the "family" argument in the mpr function.

Currently the mpr package includes distributions which have upto three parameters:

- 1 λ . This is a *scale* parameter which controls the overall magnitude of the hazard function and is typically the "interest" parameter in standard Single-Parameter Regression (SPR) models. The Multi-Parameter Regression (MPR) framework is more general and considers all parameters to be of interest.
- 2 γ . This is a *shape* parameter which controls the time evolution of the hazard.
- 3 ρ . This is an additional *shape* parameter which controls the time evolution of the hazard (available within the Burr and PGW distributions).

The MPR framework allows these parameters to depend on covariates as follows:

$$g_1(\lambda) = x^T \beta$$
$$g_2(\gamma) = z^T \alpha$$
$$g_3(\rho) = w^T \tau$$

where $g_1(.)$, $g_2(.)$ and $g_3(.)$ are appropriate link functions (log-link for positive parameters and identity-link for unconstrained parameters), x, z and w are covariate vectors, which may or may not contain covariates in common, and β , α and τ are the corresponding vectors of regression coefficients.

The distributions currently available are described below in terms of their hazard functions:

family	\parallel Hazard $h(t)$	Parameters	Note
	II	I	I
Weibull	$\parallel \lambda \gamma t^{\gamma-1}$	$\lambda > 0, \gamma > 0$	$I SPR(\lambda) = PH$
	II .	I	1

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The acronymns which appear in the table above are:

 $\mathbf{SPR}(\lambda)$ a Single-Parameter Regression (SPR) model where covariates enter through the scale parameter, λ . For example, in the row corresponding to the Weibull model, " $\mathbf{SPR}(\lambda) = \mathbf{PH}$ " means that the Weibull $\mathbf{SPR}(\lambda)$ model is a PH model. Thus, this standard parametric PH model is generalised via the Weibull MPR model.

PH proportional hazards.

AFT accelerated failure time.

PO proportional odds.

TDL time-dependent logistic.

PGW power generalised Weibull.

Author(s)

Kevin Burke.

See Also

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mpr

Fitting a Multi-Parameter Regression (MPR) model.

Description

Fits a Multi-Parameter Regression (MPR) model using a Newton-type algorithm via the nlm function

Usage

```
mpr(formula, data, family = "Weibull", init, iterlim = 1000, ...)
```

Arguments

formula	a two-sided formula object with the response on the left hand side of the ~ operator and a list of one-sided formula objects on the right hand side (one for each regression component in the mpr model). The response must be a right-censored survival object as returned by the Surv function. See "Details" for more information on the struture of the formula within the mpr function as it differs from standard regression models.
data	an optional data. frame containing the variables in the model. If missing, the variables are taken from the environment from which mpr is called.
family	the name of the parametric distribution to be used in the model. See distributions for the list of distributions currently available.
init	an optional vector of initial values for the optimisation routine. If missing, default values are used. One may also set init="random" to randomly generate initial values.
iterlim	a positive integer specifying the maximum number of iterations to be performed before the optimisation procedure is terminated. This is supplied to nlm.
	additional arguments to be passed to nlm.

Details

Multi-Parameter Regression (MPR) models are generated by allowing *multiple* distributional parameters to depend on covariates, for example, both the scale and shape parameters. This is in contrast to the more typical approach where covariates enter a model only through *one* distributional parameter. As these standard models have a single regression component, we may refer to them as Single Parameter Regression (SPR) models and, clearly, they are special cases of MPR models. The parameter through which covariates enter such SPR models may be referred to as the "interest" parameter since it generally has some specific subject-matter importance. However, this standard approach neglects other parameters which may also be important in describing the phenomenon at hand. The MPR approach generalises the standard SPR approach by viewing all distributional parameters as interest parameters in which covariate effects can be investigated.

In the context of survival analysis (currently the focus of the mpr package), the Weibull model is one of the most popular parametric models. Its hazard function is given by

$$h(t) = \lambda \gamma t^{\gamma - 1}$$

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where $\lambda > 0$, the scale parameter, controls the overall magnitude of h(t) and $\gamma > 0$, the shape parameter, controls its time evolution. In the standard SPR Weibull model, λ depends on covariates via $\log \lambda = x^T \beta$ leading to a proportional hazards (PH) model. The MPR model generalises this by allowing *both* parameters to depend on covariates as follows

$$\log \lambda = x^T \beta$$

$$\log \gamma = z^T \alpha$$

where x and z are the scale and shape covariate vectors (which may or may not contain covariates in common) and β and α are the corresponding regression coefficients.

Note that the log-link is used above to ensure positivity of the parameters. More generally, we may have

$$g_1(\lambda) = x^T \beta$$

$$q_2(\gamma) = z^T \alpha$$

where $g_1(\cdot)$ and $g_2(\cdot)$ are appropriate link functions. The mpr function does not allow the user to alter these link functions but, rather, uses the following default link functions: **log-link** (for parameters which must be *positive*) and **identity-link** (for parameters which are *unconstrained*). Although the two-parameter Weibull distribution is discussed here (due to its popularity), other distributions may have additional shape parameters, for example,

$$q_3(\rho) = w^T \tau$$

where w and τ are the vectors of covariates and regression coefficients for this additional shape component. See distributions for further details on the distributions currently available.

The struture of the formula within the mpr function is, for example, $Surv(time, status) \sim list(\sim x1 + x2, \sim x1)$ which clearly generalises the typical formula used in standard models (i.e., those with only one regression component) in the sense that the right hand side is a list of one-sided formula objects. Note the requirement that the \sim operator precedes each element within the list. Specifically, the example shown here represents the case where the covariates x1 and x2 appear in the first regression component, λ , and the covariate x2 appears in the second regression component, γ . If there was a third regression component, ρ , then there would be an additional component in the list, for example, $Surv(time, status) \sim list(\sim x1 + x2, \sim x1, \sim x1)$. The mpr function also accepts more typical two-sided formula objects, such as $Surv(time, status) \sim x1 + x2$, which imply that the terms on the right hand side appear in *each* of the regression components.

Value

mpr returns an object of class "mpr".

The function summary (i.e., summary.mpr) can be used to obtain and print a summary of the results. The the generic accessor function coefficients extracts the list of regression coefficient vectors. One can also apply predict (i.e., predict.mpr) to predict various quantites from the fitted mpr model. A stepwise variable selection procedure has been implemented for mpr models - see stepmpr.

An object of class mpr is a list containing the following components:

model a data.frame containing useful information about the fitted model with the following headings:

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family the chosen distribution.

npar number of estimated parameters in the fitted model.

loglike value of the log-likelihood.

aic value of the AIC (Akaike Information Criterion). bic value of the BIC (Bayesian Information Criterion).

code an integer indicating why the Newton optimisation procedure terminated (for more details on this stop-code see nlm) where, in particular, "1" means "relative gradient is close to zero".

coefficients a list whose elements are named vectors of coefficients (one vector per regres-

sion component).

vcov the variance-covariance matrix for the estimates.

gradient the values of the (negative) score functions from nlm.

ncomp the number of regression components in the model, i.e., the number of distribu-

tional parameters in the underlying distribution.

formula the formula supplied.

xvars a record of the names of all variables (i.e., covariates) used in fitting.

xlevels a record of the levels of any factors (i.e., categorical variables) used in fitting.

call the matched call.

Author(s)

Kevin Burke.

See Also

```
distributions, summary.mpr, predict.mpr, stepmpr.
```

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predict.mpr

Predict method for Multi-Parameter Regression (MPR) Fits

Description

Survival predictions based on mpr objects.

Usage

Arguments

object	an object of class "mpr" which is the result of a call to mpr.
newdata	data.frame in which to look for variables with which to predict.
type	type of prediction which may be a survivor function, hazard function or percentile value.
tvec	vector of times at which the predicted survivor or hazard function will be evaluated. Only required if type is "survivor" or "hazard".
prob	numeric value between 0 and 1 (i.e., probability) indicating the percentile to be predicted. By default prob = 0.5 which corresponds to the median value. Only required if type is "percentile".
	further arguments passed to or from other methods.

Value

A matrix of predictions whose rows correspond to the rows of newdata. When type is "survivor" or "hazard", this matrix of predictions has columns corresponding to tvec. However, when type is "percentile", the matrix only has one column.

Author(s)

Kevin Burke.

See Also

```
mpr, summary.mpr
```

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Examples

```
library(survival)
# Veterans' administration lung cancer data
veteran <- survival::veteran</pre>
head(veteran)
# Weibull MPR treatment model
mod1 <- mpr(Surv(time, status) ~ list(~ trt, ~ trt), data=veteran,</pre>
            family="Weibull")
# predicted survivor function evaluated at four times
predict(mod1, newdata=data.frame(trt=c(1,2)), type="survivor",
        tvec=c(25, 50, 100, 150))
# predicted percentiles
predict(mod1, newdata=data.frame(trt=c(1,2)), type="percentile", prob=0.5)
predict(mod1, newdata=data.frame(trt=c(1,2)), type="percentile", prob=0.1)
# comparing predicted survivor functions to Kaplan-Meier curves
KM <- survfit(Surv(time, status) ~ trt, data=veteran)</pre>
plot(KM, col=1:2)
tvec <- seq(0, max(KM$time), length=100)</pre>
Stpred <- predict(mod1, newdata=data.frame(trt=c(1,2)), type="survivor",</pre>
                   tvec=tvec)
lines(tvec, Stpred[1,])
lines(tvec, Stpred[2,], col=2)
```

stepmpr

Stepwise Selection Procedure for Multi-Parameter Regression (MPR) Models

Description

Applies a stepwise selection procedure to an object of class "mpr" to find the best model in the sense of AIC (or BIC).

Usage

Arguments

object an object of class "mpr" which is the result of a call to mpr.

scope

either a single formula defining the upper (maximal) model or a list containing two formulae - the lower (minimal) and upper (maximal) models respectively. See "Details" for further information.

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comp	a numeric vector indicating the regression component(s) to which the selection procedure should be applied. Note that "1" = λ , "2" = γ and "3" = ρ . For more information on the various components, see mpr and distributions.
direction	the mode of stepwise search, which can be one of "both", "backward", or "forward", with a default of "both".
joint	logical. If TRUE, the selection procedure carries out <i>joint</i> component (i.e., simultaneous) steps in addition to <i>individual</i> component steps. If FALSE, only individual component steps are carried out. See "Details" for more information.
jointonly	logical. If TRUE, the selection procedure only carries out <i>joint</i> component steps.
aic	logical. If TRUE, AIC is used as the basis for determining the best model among those considered. If FALSE, BIC is used.
trace	if positive, information is printed during the running of stepmpr. Larger values may give more detailed information.
	additional arguments to be passed to internal methods.

Details

The function stepmpr uses repeated calls to addterm and dropterm and is based on the idea that variable selection should be applied to each component individually *and* to all components jointly (when joint = TRUE). As an example, consider the case where forward selection (direction = "forward") will be carried out in components 1 and 2 individually (comp = 1:2) *and* jointly (joint = TRUE). At a given iteration of the algorithm, the following single-term additions are then carried out:

individual step 1: each term currently absent from component 1 will be considered.individual step 2: each term currently absent from component 2 will be considered.joint step 1&2: each term currently absent from both components 1 and 2 will be considered.

The reason for the joint step is to account for the possibility that a covariate may only appear significant when it is present simultaneously in *both* regression components. This situation can arise as the variance-covariance matrix for the estimated regression coefficients is typically not block diagonal with respect to the regression components and, in particular, coefficients for the same covariate in different components are typically highly correlated. Of course, the stepmpr function has the flexibility to carry individual steps only, joint steps only or individual steps in a particular component only as the end user prefers. See "Examples" below.

The set of models searched is determined by the scope argument which is either a single upper formula or a list whose elements are lower and upper formulae. The upper formula must *contain* each formula corresponding to the components under consideration (as indicated by comp) whereas the lower formula must *be contained within* each of these formulae. For more information on the use of lower and upper, see addterm.

If scope is missing, the lower model is simply the null model (i.e., a model with no covariates) and the upper model is formed using terms from the initial model; specifically, all terms from the regession components under consideration (as indicated by comp) are used in the upper formula.

Value

A final "best" mpr model as selected using the stepwise procedure.

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Author(s)

Kevin Burke.

See Also

```
mpr, dropterm, addterm, update.mpr.
```

Examples

```
# Veterans' administration lung cancer data
veteran <- survival::veteran</pre>
head(veteran)
#######
mod0 <- mpr(Surv(time, status) ~ 1, data=veteran)</pre>
mod0 # family = "Weibull" by default
# the "upper" model formula (by default the lower will be ~ 1)
scope <- ~ trt + celltype</pre>
stepmpr(mod0, scope)
stepmpr(mod0, scope, direction="forward", aic=FALSE)
# individual steps only
stepmpr(mod0, scope, joint=FALSE)
# joint steps only
stepmpr(mod0, scope, jointonly=TRUE)
# component 1 only (and, hence, only individual steps)
stepmpr(mod0, scope, comp=1)
#######
mod1 <- mpr(Surv(time, status) ~ trt + celltype, data=veteran)</pre>
mod1
stepmpr(mod1)
stepmpr(mod1, scope = \sim .^2)
# "lower" model formula forces trt to stay in
stepmpr(mod1, scope = list(~trt, ~.))
```

summary.mpr

Summarising Multi-Parameter Regression (MPR) Fits

Description

summary method for class "mpr"

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Usage

```
## S3 method for class 'mpr'
summary(object, overall = TRUE, ...)
```

Arguments

object an object of class "mpr" which is the result of a call to mpr.

overall logical. If TRUE, p-values testing the overall effect of a covariate are shown. See

"Details" for more information.

... further arguments passed to or from other methods.

Details

The function print.summary.lm produces a typical table of coefficients, standard errors and p-values along with "significance stars". In addition, a table of overall p-values are shown.

Multi-Parameter Regression (MPR) models are defined by allowing multiple distributional parameters to depend on covariates. The regression components are:

$$g_1(\lambda) = x^T \beta$$

$$g_2(\gamma) = z^T \alpha$$

$$g_3(\rho) = w^T \tau$$

and the table of coefficients displayed by print.summary.lm follows this ordering. Furthermore, the names of the coefficients in the table are proceeded by ".b" for β coefficients, ".a" for α coefficients and ".t" for τ coefficients to avoid ambiguity.

Let us assume that a covariate c, say, appears in both the λ and γ regression components. The standard table of coefficients provides p-values corresponding to the following null hypotheses:

$$H_0: \beta_c = 0$$

$$H_0: \alpha_c = 0$$

where β_c and α_c are the regression coefficients of c (one for each of the two components in which c appears). However, in the context of MPR models, it may be of interest to test the hypothesis that the **overall** effect of c is zero, i.e., that its β and α effects are jointly zero:

$$H_0: \beta_c = \alpha_c = 0$$

Thus, if overall=TRUE, print.summary.lm displays a table of such "overall p-values".

Value

The function summary.mpr returns a list containing the following components:

call the matched call from the mpr object.

model a data. frame containing useful information about the fitted model. This is the

same as the "model" element of the mpr object - see mpr for details.

coefmat a typical coefficient matrix whose columns are the estimated regression coeffi-

cients, standard errors and p-values.

overallpmat a matrix containing the overall p-values as described above in "Details".

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Author(s)

Kevin Burke.

See Also

```
mpr, predict.mpr.
```

Examples

```
# Veterans' administration lung cancer data
veteran <- survival::veteran
head(veteran)

# Weibull MPR treatment model (family = "Weibull" by default)
mod1 <- mpr(Surv(time, status) ~ list(~ trt, ~ trt), data=veteran)
summary(mod1)</pre>
```

update.mpr

Update and Re-fit a Multi-Parameter Regression (MPR) Model Call

Description

Updates the right-hand side of the formula and re-fits the mpr model.

Usage

```
## S3 method for class 'mpr'
update(object, new, comp = 1:(object$ncomp), ...)
```

Arguments

object	an object of class "mpr" which is the result of a call to mpr.
new	either a one-sided formula (in which case the comp argument is also required) or a list of one-sided formula objects whose length is equal to the number of regression components in the mpr object, e.g., the Weibull model has two components.
comp	a numeric vector indicating the regression component(s) to be updated (only needed when new is a one-sided formula) where "1" = λ , "2" = γ and "3" = ρ . For more information on the various components, see mpr and distributions.
	additional arguments to be passed to the updated mpr call.

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Details

There are two ways in which the update.mpr function can be used. The first specificies which component(s) will be updated (via the comp argument) along with the update to be applied via new which must then be a one-sided formula. The second approach specifies both the components in question and the updates to be applied through new which is a list of one-sided formula objects (in this case comp is ignored). See "Examples" below.

In the new formula (or list of formulae). means "what is already there".

Value

The fitted, updated mpr object.

Author(s)

Kevin Burke.

See Also

```
mpr, addterm, dropterm, stepmpr.
```

```
# Veterans' administration lung cancer data
veteran <- survival::veteran</pre>
head(veteran)
# Weibull MPR treatment model
mod1 <- mpr(Surv(time, status) ~ list(~ trt, ~ trt), data=veteran,</pre>
            family="Weibull")
# remove trt from first component
update(mod1, ~ . - trt, comp=1)
update(mod1, list(~ . - trt, ~ .))
# remove trt from both components
update(mod1, ~ . - trt, comp=1:2)
update(mod1, list(\sim . - trt, \sim . - trt))
# add celltype to second component
update(mod1, ~ . + celltype, comp=2)
update(mod1, list(\sim . , \sim . + celltype))
# simultaneously remove trt from first component and add celltype to second
# component. This is only possible using the approach where "new" is a list.
update(mod1, list(~ . - trt, ~ . + celltype))
# can also update other things, e.g. "family"
update(mod1, ~ ., family="Gompertz")
update(mod1, ~ . + celltype, family="Loglogistic")
mod2 <- update(mod1, ~ ., family="Burr") # change to Burr model</pre>
```

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```
mod2 update(mod2, ~ . + celltype, comp=2:3) # add celltype to components 2 and 3
```

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