# Package 'multiridge'

July 23, 2025

Title Fast Cross-Validation for Multi-Penalty Ridge Regression

Type Package

Version 1.11
<b>Date</b> 2022-06-13
Author Mark A. van de Wiel
Maintainer Mark A. van de Wiel <mark.vdwiel@amsterdamumc.nl></mark.vdwiel@amsterdamumc.nl>
<b>Depends</b> R (>= 3.5.0), survival, pROC, methods, mgcv, snowfall
<b>Description</b> Multi-penalty linear, logistic and cox ridge regression, including estimation of the penalty parameters by efficient (repeated) cross-validation and marginal likelihood maximization. Multiple high-dimensional data types that require penalization are allowed, as well as unpenalized variables. Paired and preferential data types can be specified. See Van de Wiel et al. (2021), <doi:10.48550 arxiv.2005.09301="">.</doi:10.48550>
License GPL (>= 3)
NeedsCompilation no
Repository CRAN
<b>Date/Publication</b> 2022-06-13 15:10:05 UTC
Contents
multiridge-package 2 augment 4 betasout 5 createXblocks 7 createXXblocks 8 CVfolds 9
CVscore

 doubleCV
 12

 fastCV2
 15

 IWLSCoxridge
 16

 IWLSridge
 18

 mgcv\_lambda
 19

2 multiridge-package

	mlikCV																							 . 20
	optLambdas																							 . 23
	optLambdasWrap .																							 . 25
	optLambdas_mgcv																							
	optLambdas_mgcv\	Wrap																						 . 29
	predictIWLS																							 . 30
	Scoring																							 . 31
	setupParallel																							 . 32
	SigmaFromBlocks																							 . 33
Index																								35
	tut dan an allana				7.	, ,.		<i>c</i>						1.	_	,				_		 	 	
multi	iridge-package	Fast	cros.	s-ve	анс	шп	on.	Joi	r n	ш	II-j	per	ıaı	ıy	ru	age	e r	egi	es	sic	on			

# **Description**

The package implements multi-penalty linear, logistic and cox ridge regression, including estimation of the penalty parameters by efficient (repeated) cross-validation or marginal likelihood maximization. It allows for multiple high-dimensional data types that require penalization, as well as unpenalized variables. Moreover, it allows a paired penalty for paired data types, and preferential data types can be specified.

#### **Details**

#### The DESCRIPTION file:

Package: multiridge Type: Package

Title: Fast Cross-Validation for Multi-Penalty Ridge Regression

Version: 1.11

Date: 2022-06-13

Author: Mark A. van de Wiel

Maintainer: Mark A. van de Wiel <mark.vdwiel@amsterdamumc.nl> Depends: R (>= 3.5.0), survival, pROC, methods, mgcv, snowfall

Description: Multi-penalty linear, logistic and cox ridge regression, including estimation of the penalty parameters by efficient

License: GPL (>=3)

# Index of help topics:

CVfolds Creates (repeated) cross-validation folds

CVscore Cross-validated score

IWLSCoxridge Iterative weighted least squares algorithm for

Cox ridge regression.

IWLSridge Iterative weighted least squares algorithm for

linear and logistic ridge regression.

Scoring Evaluate predictions

multiridge-package 3

SigmaFromBlocks Create penalized sample cross-product matrix

augment Augment data with zeros.

betasout Coefficient estimates from (converged) IWLS fit createXXblocks Creates list of (unscaled) sample covariance

matrices

createXblocks Create list of paired data blocks
dataXXmirmeth Contains R-object 'dataXXmirmeth'
doubleCV Double cross-validation for estimating

performance of 'multiridge'

fastCV2 Fast cross-validation per data block mgcv\_lambda Maximum marginal likelihood score

mlikCV Outer-loop cross-validation for estimating performance of marginal likelihood based

'multiridge'

multiridge-package Fast cross-validation for multi-penalty ridge

regression

optLambdas Find optimal ridge penalties.

optLambdasWrap Find optimal ridge penalties with sequential

optimization.

optLambdas\_mgcv Find optimal ridge penalties with maximimum

marginal likelihood

optLambdas\_mgcvWrap Find optimal ridge penalties with sequential

optimization.

predictIWLS Predictions from ridge fits setupParallel Setting up parallel computing

betasout: Coefficient estimates from (converged) IWLS fit

createXXblocks: Creates list of (unscaled) sample covariance matrices

CVscore: Cross-validated score for given penalty parameters

dataXXmirmeth: Example data

doubleCV: Double cross-validation for estimating performance fastCV2: Fast cross-validation per data block; no dependency

IWLSCoxridge: Iterative weighted least squares algorithm for Cox ridge regression

IWLSridge: Iterative weighted least squares algorithm for linear and logistic ridge regression

mlikCV: Cross-validation for estimating performance of marginal likelihood estimation

optLambdasWrap: Find optimal ridge penalties by cross-validation

optLambdas\_mgcvWrap: Find optimal ridge penalties in terms of marginal likelihood

predictIWLS: Predictions from ridge fits
setupParallel: Setting up parallel computing

SigmaFromBlocks: Create penalized sample cross-product matrix

# Author(s)

Mark A. van de Wiel (mark.vdwiel@amsterdamumc.nl)

### References

Mark A. van de Wiel, Mirrelijn van Nee, Armin Rauschenberger (2021). Fast cross-validation for high-dimensional ridge regression. J Comp Graph Stat

4 augment

### See Also

A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

#### **Examples**

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]</pre>
XXmirmeth <- dataXXmirmeth[[2]]</pre>
# Find initial lambdas: fast CV per data block separately.
cvperblock2 <- fastCV2(XXblocks=XXmirmeth,Y=resp,kfold=10,fixedfolds = TRUE)</pre>
lambdas <- cvperblock2$lambdas</pre>
# Create (repeated) CV-splits of the data.
leftout <- CVfolds(Y=resp,kfold=10,nrepeat=3,fixedfolds = TRUE)</pre>
# Compute cross-validated score for initial lambdas
CVscore(penalties=lambdas, XXblocks=XXmirmeth,Y=resp,folds=leftout,
score="loglik")
# Optimizes cross-validate criterion (default: log-lik)
# Increase the number of iterations for optimal results
jointlambdas <- optLambdasWrap(penaltiesinit=lambdas, XXblocks=XXmirmeth,Y=resp,
folds=leftout,score="loglik",save=T, maxItropt1=5, maxItropt2=5)
# Alternatively: optimize by using marginal likelihood criterion
## Not run:
jointlambdas2 <- optLambdas_mgcvWrap(penaltiesinit=lambdas, XXblocks=XXmirmeth,</pre>
Y=resp)
## End(Not run)
# Optimal lambdas
optlambdas <- jointlambdas$optpen</pre>
# Prepare fitting for the optimal lambdas.
XXT <- SigmaFromBlocks(XXmirmeth,penalties=optlambdas)</pre>
# Fit. fit$etas contains the n linear predictors
fit <- IWLSridge(XXT,Y=resp)</pre>
```

augment

Augment data with zeros.

#### **Description**

This function augments data with zeros to allow pairing of data on the same variables, but from DIFFERENT samples

betasout 5

#### Usage

```
augment(Xdata1, Xdata2)
```

#### **Arguments**

Xdata1 Data frame or data matrix of dimension  $n_1 \times p$ . Xdata2 Data frame or data matrix of dimension  $n_2 \times p$ 

#### **Details**

Xdata1 and Xdata2 should have the same number of columns. These columns represent variables. Augments both data matrices with zeros, such that the matrices can be paired using createXXblocks on the output of this function.

#### Value

List

Xaug1 Augmented data matrix 1
Xaug2 Augmented data matrix 2

# Examples

```
#Example
#Simulate
n1 <- 10
n2 <- 20
p <- 100
X1 <- matrix(rnorm(p*n1),nrow=n1)
X2 <- matrix(rnorm(p*n2),nrow=n2)

#check whether column dimension is correct
ncol(X1)==ncol(X2)

#create cross-product
Xaugm <- augment(X1,X2)

#check dimensions (should be (n1+n2) x p)
dim(Xaugm[[1]])
dim(Xaugm[[2]])</pre>
```

betasout

Coefficient estimates from (converged) IWLS fit

#### **Description**

Extracts estimated regression coefficients from the final Iterative Weighted Least Squares fit, as obtained from linear, logistic, or Cox ridge regression.

6 betasout

#### Usage

```
betasout(IWLSfit, Xblocks, X1=NULL, penalties, pairing = NULL)
```

#### **Arguments**

IWLSfit List object, see details

Xblocks List of data frames or matrices, representing b=1,...,B data blocks of dimen-

sions n x p\_b.

X1 Matrix. Dimension  $n \times p_0$ ,  $p_0 < n$ , representing unpenalized covariates.

penalties Numerical vector.

pairing Numerical vector of length 3 or NULL.

#### **Details**

IWLSfit should be the output of either IWLSridge or IWLSCoxridge. Xblocks may be created by createXblocks.

#### Value

List. Number of components equals number of components of Xblocks plus one, as the output is augmented with an intercept estimate (first component, NULL if absent). Each component is a numerical vector representing regression parameter estimates. Lengths of vectors match column dimensions of Xblocks (nr of variables for given data type)

#### See Also

```
createXblocks. A full demo and data are available from:
https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4
```

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
XXmirmeth <- dataXXmirmeth[[2]]
lambdas <- c(100,1000)

# Prepare fitting for the specified penalties.
XXT <- SigmaFromBlocks(XXmirmeth,penalties=lambdas)

# Fit. fit$etas contains the n linear predictors
fit <- IWLSridge(XXT,Y=resp)

# Computation of the regression coefficients requires the original
# (large!) nxp data sets, available from link above
## Not run:
Xbl <- createXblocks(list(datamir,datameth))
betas <- betasout(fit, Xblocks=Xbl, penalties=lambdas)

## End(Not run)</pre>
```

createXblocks 7

creat	~VL1	ماده
creat	exni	OCKS

Create list of paired data blocks

# **Description**

Create list of paired data blocks

### Usage

```
createXblocks(datablocks, which2pair = NULL)
```

# **Arguments**

datablocks List of data frames or matrices representing b=1,...,B data blocks of dimen-

sions n x p\_b.

which2pair Integer vector of size 2 (or NULL)

#### **Details**

Only use this function when you wish to pair two data blocks. If which2pair = NULL the output matches the input. If not, the function adds a paired data block, pairing the two data blocks corresponding to the elements of which2pair.

#### Value

List. Same length as datablocks when which2pair = NULL, or augmented with one paired data block.

#### See Also

```
createXXblocks. A full demo and data are available from:
https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4
```

```
n <- 43
p <- 100
fakeXbl <- createXblocks(list(X1 = matrix(rnorm(n*p),nrow=n),X2 = matrix(rnorm(n*p),nrow=n)))</pre>
```

8 createXXblocks

createXXblocks Creates list of (unscaled) sample covariance matrices
--

### **Description**

Creates list of (unscaled) sample covariance matrices  $X_b \% * (X_b)$  for data blocks b = 1,..., B.

# Usage

```
createXXblocks(datablocks, datablocksnew = NULL, which2pair = NULL)
```

# **Arguments**

```
datablocks List of data frames or matrices
datablocksnew List of data frames or matrices
which2pair Integer vector of size 2 (or NULL)
```

#### **Details**

The efficiency of multiridge for high-dimendional data relies largely on this function: all iterative calculation are performed on the out put of this function, which contains B blocks of nxn matrices. If which2pair != NULL, the function adds a paired covariance block, pairing the two data blocks corresponding to the elements of which2pair. If predictions for new samples are desired, one also needs to specify datablocksnew, which should have he exact same format as datablocks with matching column dimension (number of variables).

### Value

List. Same number of component as datablocks when which2pair = NULL, or augmented with one paired data block. Dimension is nxn for all components.

#### See Also

createXblocks, which is required when parameter estimates are desired (not needed for prediction). A full demo and data are available from:

```
https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4
```

```
#Example
#Simulate
Xbl1 <- matrix(rnorm(1000),nrow=10)
Xbl2 <- matrix(rnorm(2000),nrow=10)

#check whether dimensions are correct
ncol(Xbl1)==nrow(Xbl2)
#create cross-product</pre>
```

CVfolds 9

```
XXbl <- createXXblocks(list(Xbl1,Xbl2))
#suppose penalties for two data types equal 5,10, respectively
Sigma <- SigmaFromBlocks(XXbl,c(5,10))
#check dimensions (should be n x n)
dim(Sigma)</pre>
```

**CVfolds** 

Creates (repeated) cross-validation folds

#### **Description**

Creates (repeated) cross-validation folds for samples

### Usage

```
CVfolds(Y, model = NULL, balance = TRUE, kfold = 10, fixedfolds = TRUE, nrepeat = 1)
```

# **Arguments**

Y Response vector: numeric, binary, factor or survival.

model Character. Any of c("linear", "logistic", "cox"). Is inferred from Y when

NULL.

Boolean. Should the splits be balanced in terms of response labels?

kfold Integer. Desired fold.

fixedfolds Boolean. Should fixed splits be used for reproducibility?

nrepeat Numeric. Number of repeats.

### **Details**

Creates (repeated), possibly balanced, splits of the samples. Computing time will often largely depend on on kfold\*nrepeat, the number of training-test splits evaluated.

#### Value

List object with kfold\*nrepeat elements containing the sample indices of the left-out samples per split.

#### See Also

A full demo and data are available from:

```
https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4
```

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
leftout <- CVfolds(Y=resp,kfold=10,nrepeat=3,fixedfolds = TRUE)</pre>
```

10 CVscore

CVscore	Cross-validated score
---------	-----------------------

# Description

Cross-validated score for given penalty parameters.

# Usage

```
CVscore(penalties, XXblocks, Y, X1 = NULL, pairing = NULL, folds, intercept =
ifelse(is(Y, "Surv"), FALSE, TRUE), frac1 = NULL, score = "loglik", model =
NULL, eps = 1e-07, maxItr = 100, trace = FALSE, printCV = TRUE, save = FALSE,
parallel = FALSE)
```

# Arguments

penalties	Numeric vector.
XXblocks	List of nxn matrices. Usually output of createXXblocks.
Υ	Response vector: numeric, binary, factor or survival.
X1	Matrix. Dimension $n \times p_0$ , $p_0 < n$ , representing unpenalized covariates
pairing	Numerical vector of length 3 or NULL when pairs are absent. Represents the indices (in XXblocks) of the two data blocks involved in pairing, plus the index of the paired block.
folds	List of integer vector. Usually output of CVfolds.
intercept	Boolean. Should an intercept be included?
frac1	Scalar. Prior fraction of cases. Only relevant for model="logistic".
score	Character. See Details.
model	Character. Any of c("linear", "logistic", "cox"). Is inferred from Y when NULL.
eps	Scalar. Numerical bound for IWLS convergence.
maxItr	Integer. Maximum number of iterations used in IWLS.
trace	Boolean. Should the output of the IWLS algorithm be traced?
printCV	Boolean. Should the CV-score be printed on screen?
save	Boolean. If TRUE appends the penalties and resulting CV score to global variable all scores $$
parallel	Boolean. Should computation be done in parallel? If TRUE, requires to run setupParallel first.

# **Details**

See Scoring for details on score.

dataXXmirmeth 11

#### Value

Numeric, cross-validated prediction score for given penalties

#### See Also

doubleCV for double cross-validation, used for performance evaluation

### **Examples**

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
XXmirmeth <- dataXXmirmeth[[2]]

# Find initial lambdas: fast CV per data block separately.
cvperblock2 <- fastCV2(XXblocks=XXmirmeth,Y=resp,kfold=10,fixedfolds = TRUE)
lambdas <- cvperblock2$lambdas

# Create training-test splits
leftout <- CVfolds(Y=resp,kfold=10,nrepeat=3,fixedfolds = TRUE)
CVscore(penalties=lambdas, XXblocks=XXmirmeth,Y=resp,folds=leftout,score="loglik")</pre>
```

dataXXmirmeth

Contains R-object dataXXmirmeth

### **Description**

This list object contains the binary response (control/case) and two data blocks corresponding to miRNA and methylation data

### Usage

```
data(dataXXmirmeth)
```

# **Format**

The format is a list with two components: resp: numeric (0/1) [1:43]\ XXmirmeth: list with 2 components, each a matrix [1:43,1:43]\

### **Details**

The object XXmirmeth is created by applying createXXblocks(list(datamir, datameth)), where objects datamir and datameth are large data matrices stored in the mirmethdata. Rdata file, which is available from the link below.

12 doubleCV

#### **Source**

Snoek, B. C. et al. (2019), Genome-wide microRNA analysis of HPV-positive self-samples yields novel triage markers for early detection of cervical cancer, International Journal of Cancer 144(2), 372-379.

Verlaat, W. et al. (2018), Identification and validation of a 3-gene methylation classifier for hpv-based cervical screening on self-samples, Clinical Cancer Research 24(14), 3456-3464.

#### References

Mark A. van de Wiel, Mirrelijn van Nee, Armin Rauschenberger (2021). Fast cross-validation for multi-penalty high-dimensional ridge regression. J Comp Graph Stat

#### See Also

```
createXXblocks. Source data file is available from:
https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4
```

#### **Examples**

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
XXmirmeth <- dataXXmirmeth[[2]]</pre>
```

doubleCV

Double cross-validation for estimating performance of multiridge

# Description

Double cross-validation for estimating performance of multiridge. Outer fold is for testing, inner fold for penalty parameter tuning

#### Usage

```
doubleCV(penaltiesinit, XXblocks, Y, X1 = NULL, pairing = NULL, outfold = 5,
  infold = 10, nrepeatout = 1, nrepeatin = 1, balance = TRUE, fixedfolds =
  TRUE, intercept = ifelse(is(Y, "Surv"), FALSE, TRUE), frac1 = NULL,
  score = "loglik",model = NULL, eps = 1e-07, maxItr = 10, trace = FALSE,
  printCV = TRUE, reltol = 1e-04, optmethod1 = "SANN", optmethod2 =
  ifelse(length(penaltiesinit) == 1, "Brent", "Nelder-Mead"), maxItropt1 = 10,
  maxItropt2 = 25, save = FALSE, parallel = FALSE, pref = NULL, fixedpen = NULL)
```

### **Arguments**

```
penaltiesinit Numeric vector. Initial values for penaltyparameters. May be obtained from fastCV2.

XXblocks List of nxn matrices. Usually output of createXXblocks.

Y Response vector: numeric, binary, factor or survival.
```

doubleCV 13

X1 Matrix. Dimension  $n \times p_0$ ,  $p_0 < n$ , representing unpenalized covariates

pairing Numerical vector of length 3 or NULL when pairs are absent. Represents the

indices (in XXblocks) of the two data blocks involved in pairing, plus the index

of the paired block.

outfold Integer. Outer fold for test samples.

infold Integer. Inner fold for tuning penalty parameters.nrepeatout Integer. Number of repeated splits for outer fold.nrepeatin Integer. Number of repeated splits for inner fold.

balance Boolean. Should the splits be balanced in terms of response labels?

fixedfolds Boolean. Should fixed splits be used for reproducibility?

intercept Boolean. Should an intercept be included?

frac1 Scalar. Prior fraction of cases. Only relevant for model="logistic".

score Character. See Details.

model Character. Any of c("linear", "logistic", "cox"). Is inferred from Y when

NULL.

eps Scalar. Numerical bound for IWLS convergence.

maxItr Integer. Maximum number of iterations used in IWLS.

trace Boolean. Should the output of the IWLS algorithm be traced?

printCV Boolean. Should the CV-score be printed on screen? reltol Scalar. Relative tolerance for optimization methods.

optmethod1 Character. First, global search method. Any of the methods c("Brent", "Nelder-Mead",

"Sann") may be used, but simulated annealing by "Sann" is recommended to search a wide landscape. Other unconstrained methods offered by optim may

also be used, but have not been tested.

optmethod2 Character. Second, local search method. Any of the methods c("Brent",

"Nelder-Mead", "Sann") may be used, but "Nelder-Mead" is generally recommended. Other unconstrained methods offered by optim may also be used,

but have not been tested.

maxItropt1 Integer. Maximum number of iterations for optmethod1.
maxItropt2 Integer. Maximum number of iterations for optmethod2.

save Boolean. If TRUE appends the penalties and resulting CVscore to global vari-

able allscores

parallel Boolean. Should computation be done in parallel? If TRUE, requires to run

setupParallel first.

pref Integer vector or NULL. Contains indices of data types in XXblocks that are pref-

erential.

fixedpen Integer vector or NULL. Contains indices of data types of which penalty is fixed

to the corresponding value in penaltiesinit.

14 doubleCV

#### **Details**

WARNING: this function may be very time-consuming. The number of evaluations may equal nrepeatout\*outerfold\*nrepeatin\*innerfold\*maxItr\*(maxItropt1+maxItropt2). Computing time may be estimated by multiplying computing time of optLambdasWrap by nrepeatout\*outerfold. See Scoring for details on score.

#### Value

List with the following components:

sampleindex Numerical vector: sample indices

true True responses

linpred Cross-validated linear predictors

#### See Also

optLambdas, optLambdasWrap which optimize the penalties. Scoring which may applied to output of this function to obtain overall cross-validated performance score. A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
XXmirmeth <- dataXXmirmeth[[2]]

# Find initial lambdas: fast CV per data block separately.
cvperblock2 <- fastCV2(XXblocks=XXmirmeth,Y=resp,kfold=10,fixedfolds = TRUE)
lambdas <- cvperblock2$lambdas

# Double cross-validation
## Not run:
perf <- doubleCV(penaltiesinit=lambdas,XXblocks=XXmirmeth,Y=resp,
score="loglik",outfold=10, infold=10, nrepeatout=1, nrepeatin=3, parallel=TRUE)

# Performance metrics
Scoring(perf$linpred,perf$true,score="auc",print=TRUE)
Scoring(perf$linpred,perf$true,score="brier",print=TRUE)
Scoring(perf$linpred,perf$true,score="loglik",print=TRUE)
## End(Not run)</pre>
```

fastCV2

|--|

# **Description**

Fast cross-validation for high-dimensional data. Finds optimal penalties separately per data block. Useful for initialization.

# Usage

```
fastCV2(XXblocks, Y, X1 = NULL, kfold = 10, intercept =
ifelse(is(Y, "Surv"), FALSE, TRUE), parallel = FALSE, fixedfolds = TRUE,
model = NULL, eps = 1e-10, reltol = 0.5, lambdamax= 10^6, traceCV=TRUE)
```

# Arguments

XXblocks	List of data frames or matrices, representing $b=1, \ldots, B$ data blocks of dimensions $n \times p_b$ .
Υ	Response vector: numeric, binary, factor or survival.
X1	Matrix. Dimension $n \times p_0$ , $p_0 < n$ , representing unpenalized covariates.
kfold	Integer. Desired fold.
intercept	Boolean. Should an intercept be included?
parallel	Boolean. Should computation be done in parallel? If TRUE, requires to run setupParallel first.
fixedfolds	Boolean. Should fixed splits be used for reproducibility?
mode1	Character. Any of c("linear", "logistic", " $cox$ "). Is inferred from Y when NULL.
eps	Scalar. Numerical bound for IWLS convergence.
reltol	Scalar. Relative tolerance for optimization method.
lambdamax	Numeric. Upperbound for lambda.
traceCV	Boolean. Should the CV results be traced and printed?

# **Details**

This function is basically a wrapper for applying optLambdas per data block separately using Brent optimization.

# Value

Numerical vector containing penalties optimized separately per data block. Useful for initialization.

# See Also

optLambdas, optLambdasWrap which optimize the penalties jointly. A full demo and data are available from:

```
https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4
```

16 IWLSCoxridge

#### **Examples**

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
XXmirmeth <- dataXXmirmeth[[2]]

cvperblock2 <- fastCV2(XXblocks=XXmirmeth,Y=resp,kfold=10,fixedfolds = TRUE)
lambdas <- cvperblock2$lambdas</pre>
```

**IWLSCoxridge** 

Iterative weighted least squares algorithm for Cox ridge regression.

# Description

Iterative weighted least squares algorithm for Cox ridge regression. Updates the weights and linear predictors until convergence.

#### Usage

```
IWLSCoxridge(XXT, Y, X1 = NULL, intercept = FALSE, eps = 1e-07, maxItr = 25,
trace = FALSE, E0 = NULL)
```

# Arguments

XXT	Matrix. Dimensions nxn. Sample cross-product from penalized variables, usually computed by $SigmaFromBlocks$ .
Υ	Response vector: class survival.
X1	Matrix. Dimension $n \times p_0$ , $p_0 < n$ , representing unpenalized covariates.
intercept	Boolean. Should an intercept be included?
eps	Scalar. Numerical bound for IWLS convergence.
maxItr	Integer. Maximum number of iterations used in IWLS.
trace	Boolean. Should the output of the IWLS algorithm be traced?
E0	Numerical vector or NULL. Optional initial values for linear predictor. Same length as Y. Usually NULL, which initializes linear predictor with 0.

# **Details**

Usually, Cox ridge regression does not use an intercept, as this is part of the baseline hazard. The latter is estimated using the Breslow estimator. To keep the function computationally efficient it returns the linear predictors (which suffice for predictions), instead of parameter estimates. These may be obtained by applying the betasout function to the output of this function.

IWLSCoxridge 17

#### Value

List, containing:

etas Numerical vector: Final linear predictors

Ypred Predicted survival

convergence Boolean: has IWLS converged?

nIt Number of iterations

Hres Auxiliary list object. Passed on to other functions

linearized Linearized predictions

unpen Boolean: are there any unpenalized covariates involved? Passed on to other

functions

intercept Boolean: Is an intercept included?

eta0 Numerical vector: Initial linear predictors

X1 Matrix: design matrix unpenalized variables

#### References

Mark A. van de Wiel, Mirrelijn van Nee, Armin Rauschenberger (2021). Fast cross-validation for high-dimensional ridge regression. J Comp Graph Stat

#### See Also

IWLSridge for linear and logistic ridge. betasout for obtaining parameter estimates. predictIWLS for predictions on new samples. A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
XXmirmeth <- dataXXmirmeth[[2]]
lambdas <- c(100,1000)

# Create fake survival data
respsurv <- Surv(rexp(length(resp)),resp)

# Prepare fitting for the specified penalties.
XXT <- SigmaFromBlocks(XXmirmeth,penalties=lambdas)

# Fit. fit$etas contains the n linear predictors
fit <- IWLSCoxridge(XXT,Y=respsurv)</pre>
```

18 IWLSridge

IWLSridge	Iterative weighted least squares algorithm for linear and logistic ridge regression.

# Description

Iterative weighted least squares algorithm for linear and logistic ridge regression. Updates the weights and linear predictors until convergence.

# Usage

```
IWLSridge(XXT, Y, X1 = NULL, intercept = TRUE, frac1 = NULL, eps = 1e-07,
maxItr = 25, trace = FALSE, model = NULL, E0 = NULL)
```

# **Arguments**

XXT	Matrix. Dimensions nxn. Sample cross-product from penalized variables, usually computed by SigmaFromBlocks.
Υ	Response vector: numeric, binary, or two-class factor
X1	Matrix. Dimension $n \times p_0$ , $p_0 < n$ , representing unpenalized covariates.
intercept	Boolean. Should an intercept be included?
frac1	Scalar. Prior fraction of cases. Only relevant for model="logistic".
eps	Scalar. Numerical bound for IWLS convergence.
maxItr	Integer. Maximum number of iterations used in IWLS.
trace	Boolean. Should the output of the IWLS algorithm be traced?
mode1	Character. Any of c("linear", "logistic"). Is inferred from Y when NULL. Note that the cox model for survival is covered by the function IWLSCoxridge.
E0	Numerical vector or NULL. Optional initial values for linear predictor. Same length as Y. Usually NULL, which initializes linear predictor with 0.

#### **Details**

An (unpenalized) intercept is included by default. To keep the function computationally efficient it returns the linear predictors (which suffice for predictions), instead of parameter estimates. These may be obtained by applying the betasout function to the output of this function.

#### Value

List, containing:

etas Numerical vector: Final linear predictors

Ypred Predicted survival

convergence Boolean: has IWLS converged?

nIt Number of iterations

mgcv\_lambda 19

Hres Auxiliary list object. Passed on to other functions

linearized Linearized predictions

unpen Boolean: are there any unpenalized covariates involved? Passed on to other

functions

intercept Boolean: Is an intercept included?

eta0 Numerical vector: Initial linear predictors
X1 Matrix: design matrix unpenalized variables

#### References

Mark A. van de Wiel, Mirrelijn van Nee, Armin Rauschenberger (2021). Fast cross-validation for high-dimensional ridge regression. J Comp Graph Stat

#### See Also

IWLSCoxridge for Cox ridge. betasout for obtaining parameter estimates. predictIWLS for predictions on new samples. A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

# **Examples**

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
XXmirmeth <- dataXXmirmeth[[2]]
lambdas <- c(100,1000)

# Prepare fitting for the specified penalties.
XXT <- SigmaFromBlocks(XXmirmeth,penalties=lambdas)

# Fit. fit$etas contains the n linear predictors
fit <- IWLSridge(XXT,Y=resp)</pre>
```

mgcv_lambda	Maximum marginal likelihood score	

# Description

Computed maximum marginal likelihood score for given penalty parameters using mgcv.

# Usage

```
mgcv_lambda(penalties, XXblocks,Y, model=NULL, printscore=TRUE, pairing=NULL, sigmasq = 1,
    opt.sigma=ifelse(model=="linear",TRUE, FALSE))
```

20 mlikCV

#### **Arguments**

penalties Numeric vector.

XXblocks List of nxn matrices. Usually output of createXXblocks.

Y Response vector: numeric, binary, factor or survival.

model Character. Any of c("linear", "logistic", "cox"). Is inferred from Y when

NULL.

printscore Boolean. Should the score be printed?

pairing Numerical vector of length 3 or NULL when pairs are absent. Represents the

indices (in XXblocks) of the two data blocks involved in pairing, plus the index

of the paired block.

sigmasq Default error variance.

opt.sigma Boolean. Should the error variance be optimized as well? Only relevant for

model="linear".

#### **Details**

See gam for details on how the marginal likelihood is computed.

#### Value

Numeric, marginal likelihood score for given penalties

### References

Wood, S. N. (2011), Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models, J. Roy. Statist. Soc., B 73(1), 3-36.

### See Also

CVscore for cross-validation alternative. A full demo and data are available from: https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

mlikCV	Outer-loop cross-validation for estimating performance of marginal likelihood based multiridge

#### **Description**

Outer-loop cross-validation for estimating performance of marginal likelihood based multiridge. Outer fold is for testing; penalty parameter tuning is performed by marginal likelihood estimation

mlikCV 21

# Usage

```
mlikCV(penaltiesinit, XXblocks, Y, pairing = NULL, outfold = 5, nrepeatout = 1,
balance = TRUE, fixedfolds = TRUE, model = NULL, intercept =
ifelse(is(Y, "Surv"), FALSE, TRUE), reltol = 1e-04, trace = FALSE, optmethod1 = "SANN",
optmethod2 = ifelse(length(penaltiesinit) == 1, "Brent", "Nelder-Mead"),
maxItropt1 = 10, maxItropt2 = 25, parallel = FALSE, pref = NULL,
fixedpen = NULL, sigmasq = 1, opt.sigma=ifelse(model=="linear", TRUE, FALSE))
```

#### **Arguments**

penaltiesinit Numeric vector. Initial values for penaltyparameters. May be obtained from

fastCV2.

XXblocks List of nxn matrices. Usually output of createXXblocks.
Y Response vector: numeric, binary, factor or survival.

pairing Numerical vector of length 3 or NULL when pairs are absent. Represents the

indices (in XXblocks) of the two data blocks involved in pairing, plus the index

of the paired block.

outfold Integer. Outer fold for test samples.

nrepeatout Integer. Number of repeated splits for outer fold.

balance Boolean. Should the splits be balanced in terms of response labels?

fixedfolds Boolean. Should fixed splits be used for reproducibility?

intercept Boolean. Should an intercept be included?

model Character. Any of c("linear", "logistic", "cox"). Is inferred from Y when

NULL.

trace Boolean. Should the output of the IWLS algorithm be traced?

reltol Scalar. Relative tolerance for optimization methods.

optmethod1 Character. First, global search method. Any of the methods c("Brent", "Nelder-Mead",

"Sann") may be used, but simulated annealing by "Sann" is recommended to search a wide landscape. Other unconstrained methods offered by optim may

also be used, but have not been tested.

optmethod2 Character. Second, local search method. Any of the methods c("Brent",

"Nelder-Mead", "Sann") may be used, but "Nelder-Mead" is generally recommended. Other unconstrained methods offered by optim may also be used,

but have not been tested.

maxItropt1 Integer. Maximum number of iterations for optmethod1.
maxItropt2 Integer. Maximum number of iterations for optmethod2.

parallel Boolean. Should computation be done in parallel? If TRUE, requires to run

setupParallel first.

pref Integer vector or NULL. Contains indices of data types in XXblocks that are pref-

erential.

fixedpen Integer vector or NULL. Contains indices of data types of which penalty is fixed

to the corresponding value in penaltiesinit.

sigmasq Default error variance.

opt.sigma Boolean. Should the error variance be optimized as well? Only relevant for

model="linear".

22 mlikCV

#### **Details**

WARNING: this function may be very time-consuming. The number of evaluations may equal nrepeatout\*outerfold\*(maxItropt1+maxItropt2). Computing time may be estimated by multiplying computing time of optLambdas\_mgcvWrap by nrepeatout\*outerfold.

#### Value

List with the following components:

sampleindex Numerical vector: sample indices

true True responses

linpred Cross-validated linear predictors

#### See Also

optLambdas\_mgcv, optLambdas\_mgcvWrap which optimize the penalties. Scoring which may applied to output of this function to obtain overall cross-validated performance score. doubleCV for double cross-validation counterpart. A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
XXmirmeth <- dataXXmirmeth[[2]]

# Find initial lambdas: fast CV per data block separately.
cvperblock2 <- fastCV2(XXblocks=XXmirmeth,Y=resp,kfold=10,fixedfolds = TRUE)
lambdas <- cvperblock2$lambdas

# Outer cross-validation, inner marginal likelihood optimization
## Not run:
perfmlik <- mlikCV(penaltiesinit=lambdas, XXblocks=XXmirmeth, Y=resp,outfold=10,nrepeatout=1)

# Performance metrics
Scoring(perfmlik$linpred,perfmlik$true,score="auc",print=TRUE)
Scoring(perfmlik$linpred,perfmlik$true,score="brier",print=TRUE)
Scoring(perfmlik$linpred,perfmlik$true,score="loglik",print=TRUE)
## End(Not run)</pre>
```

optLambdas 23

# Description

Optimizes a cross-validated score w.r.t. ridge penalties for multiple data blocks.

# Usage

```
optLambdas(penaltiesinit = NULL, XXblocks, Y, X1 = NULL, pairing = NULL, folds,
  intercept = ifelse(is(Y, "Surv"), FALSE, TRUE), frac1 = NULL, score = "loglik",
  model = NULL, epsIWLS = 0.001, maxItrIWLS = 25, traceCV = TRUE, reltol = 1e-04,
  optmethod = ifelse(length(penaltiesinit) == 1, "Brent", "Nelder-Mead"), maxItropt = 500,
  save = FALSE, parallel = FALSE, fixedpen = NULL, fixedseed = TRUE)
```

#### **Arguments**

penaltiesinit	Numeric vector. Initial values for penaltyparameters. May be obtained from fastCV2.
XXblocks	List of nxn matrices. Usually output of createXXblocks.
Υ	Response vector: numeric, binary, factor or survival.
X1	Matrix. Dimension n x p_0, p_0 < n, representing unpenalized covariates
pairing	Numerical vector of length 3 or NULL when pairs are absent. Represents the indices (in XXblocks) of the two data blocks involved in pairing, plus the index of the paired block.
folds	List, containing the splits of the samples. Usually obtained by CVfolds
intercept	Boolean. Should an intercept be included?
frac1	Scalar. Prior fraction of cases. Only relevant for model="logistic".
score	Character. See Details.
model	Character. Any of c("linear", "logistic", "cox"). Is inferred from Y when NULL.
epsIWLS	Scalar. Numerical bound for IWLS convergence.
maxItrIWLS	Integer. Maximum number of iterations used in IWLS.
traceCV	Boolean. Should the output of the IWLS algorithm be traced?
reltol	Scalar. Relative tolerance for optimization methods.
optmethod	Character. Optimization method. Any of the methods c("Brent", "Nelder-Mead", "Sann") may be used, but "Nelder-Mead" is generally recommended. Other unconstrained methods offered by optim may also be used, but have not been tested.
maxItropt	Integer. Maximum number of iterations for optmethod.
save	Boolean. If TRUE appends the penalties and resulting CVscore to global variable allscores

24 optLambdas

parallel Boolean. Should computation be done in parallel? If TRUE, requires to run

setupParallel first.

fixedpen Integer vector or NULL. Contains indices of data types of which penalty is fixed

to the corresponding value in penaltiesinit.

fixedseed Boolean. Should the initialization be fixed? For reproducibility.

#### Details

See Scoring for details on score. We highly recommend to use smooth scoring functions, in particular "loglik". For ranking-based criteria like auc and cindex we advise to use repeated CV (see CVfolds) to avoid ending up in any of the many local optima.

#### Value

List, with components:

optres Output of the optimizer

optpen Vector with determined optimal penalties

allsc Matrix with CV scores for all penalty parameter configurations used by the op-

timizer

#### See Also

optLambdasWrap for i) (recommended) optimization in two steps: first global, then local; and ii) sequential optimization when some data types are preferred over others. fastCV2 for initialization of penalties. A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
XXmirmeth <- dataXXmirmeth[[2]]

# Find initial lambdas: fast CV per data block separately.
cvperblock2 <- fastCV2(XXblocks=XXmirmeth,Y=resp,kfold=10,fixedfolds = TRUE)
lambdas <- cvperblock2$lambdas

# Create (repeated) CV-splits of the data.
leftout <- CVfolds(Y=resp,kfold=10,nrepeat=3,fixedfolds = TRUE)

# One-pass optimization
# Increase the number of iterations for optimal results
jointlambdas <- optLambdas(penaltiesinit=lambdas, XXblocks=XXmirmeth,Y=resp,folds=leftout,score="loglik",save=T,maxItropt=5)</pre>
```

optLambdasWrap 25

optLambdasWrap	Find optimal ridge penalties with sequential optimization.	

# Description

Sequentially optimizes a cross-validated score w.r.t. ridge penalties for multiple data blocks. Also implements preferential ridge, which allows to first optimize for the preferential data types.

#### Usage

```
optLambdasWrap(penaltiesinit = NULL, XXblocks, Y, X1 = NULL, pairing = NULL,
  folds, intercept = ifelse(is(Y, "Surv"), FALSE, TRUE), frac1 = NULL,
  score = "loglik", model = NULL, epsIWLS = 0.001, maxItrIWLS = 25,
  traceCV = TRUE, reltol = 1e-04, optmethod1 = "SANN", optmethod2 =
  ifelse(length(penaltiesinit) == 1, "Brent", "Nelder-Mead"), maxItropt1 = 10,
  maxItropt2 = 25, save = FALSE, parallel = FALSE, pref = NULL, fixedpen = NULL)
```

#### **Arguments**

penaltiesinit	Numeric vector. Initial values for penaltyparameters. May be obtained from fastCV2.
XXblocks	List of nxn matrices. Usually output of createXXblocks.
Υ	Response vector: numeric, binary, factor or survival.
X1	Matrix. Dimension $n \times p_0$ , $p_0 < n$ , representing unpenalized covariates
pairing	Numerical vector of length 3 or NULL when pairs are absent. Represents the indices (in XXblocks) of the two data blocks involved in pairing, plus the index of the paired block.
folds	List, containing the splits of the samples. Usually obtained by CVfolds
intercept	Boolean. Should an intercept be included?
frac1	Scalar. Prior fraction of cases. Only relevant for model="logistic".
score	Character. See Details.
model	Character. Any of c("linear", "logistic", "cox"). Is inferred from Y when NULL.
epsIWLS	Scalar. Numerical bound for IWLS convergence.
maxItrIWLS	Integer. Maximum number of iterations used in IWLS.
traceCV	Boolean. Should the output of the IWLS algorithm be traced?
reltol	Scalar. Relative tolerance for optimization methods.
optmethod1	Character. First, global search method. Any of the methods c("Brent", "Nelder-Mead", "Sann") may be used, but simulated annealing by "Sann" is recommended to search a wide landscape. Other unconstrained methods offered by optim may

also be used, but have not been tested.

26 optLambdasWrap

optmethod2 Character. Second, local search method. Any of the methods c("Brent", "Nelder-Mead",

"Sann") may be used, but "Nelder-Mead" is generally recommended. Other unconstrained methods offered by optim may also be used, but have not been

tested.

maxItropt1 Integer. Maximum number of iterations for optmethod1.
maxItropt2 Integer. Maximum number of iterations for optmethod2.

save Boolean. If TRUE appends the penalties and resulting CVscore to global vari-

able allscores

parallel Boolean. Should computation be done in parallel? If TRUE, requires to run

setupParallel first.

pref Integer vector or NULL. Contains indices of data types in XXblocks that are pref-

erential.

fixedpen Integer vector or NULL. Contains indices of data types of which penalty is fixed

to the corresponding value in penaltiesinit.

#### **Details**

As opposed to optLambdas this function first searches globally, then locally. Hence, more time-consuming, but better guarded against multiple local optima.

See Scoring for details on score. We highly recommend to use smooth scoring functions, in particular "loglik". For ranking-based criteria like "auc" and "cindex" we advise to use repeated CV (see CVfolds) to avoid ending up in any of the many local optima.

#### Value

List, with components:

res Outputs of all optimizers used

lambdas List of penalties found by the optimizers optpen Numerical vector with final, optimal penalties

#### See Also

optLambdas for one-pass optimization. fastCV2 for initialization of penalties. A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]
XXmirmeth <- dataXXmirmeth[[2]]
# Find initial lambdas: fast CV per data block separately.
cvperblock2 <- fastCV2(XXblocks=XXmirmeth,Y=resp,kfold=10,fixedfolds = TRUE)
lambdas <- cvperblock2$lambdas
# Create (repeated) CV-splits of the data.</pre>
```

optLambdas\_mgcv 27

```
leftout <- CVfolds(Y=resp,kfold=10,nrepeat=3,fixedfolds = TRUE)

# Optimizes cross-validate criterion (default: log-lik)

# Increase the number of iterations for optimal results
jointlambdas <- optLambdasWrap(penaltiesinit=lambdas, XXblocks=XXmirmeth,Y=resp,
folds=leftout,score="loglik",save=T,maxItropt1=5, maxItropt2=5)</pre>
```

optLambdas\_mgcv

Find optimal ridge penalties with maximimum marginal likelihood

# Description

Optimizes a marginal likelihood score w.r.t. ridge penalties for multiple data blocks.

# Usage

```
optLambdas_mgcv(penaltiesinit=NULL, XXblocks,Y, pairing=NULL, model=NULL, reltol=1e-4,
  optmethod=ifelse(length(penaltiesinit)==1,"Brent", "Nelder-Mead"),maxItropt=500,
  tracescore=TRUE, fixedpen=NULL, fixedseed =TRUE, sigmasq = 1,
  opt.sigma=ifelse(model=="linear",TRUE, FALSE))
```

# **Arguments**

penaltiesinit	Numeric vector. Initial values for penaltyparameters. May be obtained from fastCV2.
XXblocks	List of nxn matrices. Usually output of createXXblocks.
Υ	Response vector: numeric, binary, factor or survival.
pairing	Numerical vector of length 3 or NULL when pairs are absent. Represents the indices (in XXblocks) of the two data blocks involved in pairing, plus the index of the paired block.
mode1	Character. Any of c("linear", "logistic", "cox"). Is inferred from Y when NULL.
reltol	Scalar. Relative tolerance for optimization methods.
optmethod	Character. Optimization method. Any of the methods c("Brent", "Nelder-Mead", "Sann") may be used, but "Nelder-Mead" is generally recommended. Other unconstrained methods offered by optim may also be used, but have not been tested.
maxItropt	Integer. Maximum number of iterations for optmethod.
tracescore	Boolean. Should the output of the scores be traced?
fixedpen	Integer vector or NULL. Contains indices of data types of which penalty is fixed to the corresponding value in penaltiesinit.
fixedseed	Boolean. Should the initialization be fixed? For reproducibility.
sigmasq	Default error variance.
opt.sigma	Boolean. Should the error variance be optimized as well? Only relevant for model="linear".

28 optLambdas\_mgcv

#### **Details**

See gam for details on how the marginal likelihood is computed.

#### Value

List, with components:

optres Output of the optimizer

optpen Vector with determined optimal penalties

allsc Matrix with marginal likelihood scores for all penalty parameter configurations

used by the optimizer

#### See Also

optLambdas\_mgcvWrap for i) (recommended) optimization in two steps: first global, then local; and ii) sequential optimization when some data types are preferred over others. A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

```
data(dataXXmirmeth)
resp <- dataXXmirmeth[[1]]</pre>
XXmirmeth <- dataXXmirmeth[[2]]</pre>
# Find initial lambdas: fast CV per data block separately.
cvperblock2 <- fastCV2(XXblocks=XXmirmeth,Y=resp,kfold=10,fixedfolds = TRUE)</pre>
lambdas <- cvperblock2$lambdas</pre>
# Create (repeated) CV-splits of the data.
leftout <- CVfolds(Y=resp,kfold=10,nrepeat=3,fixedfolds = TRUE)</pre>
# Compute cross-validated score for initial lambdas
CVscore(penalties=lambdas, XXblocks=XXmirmeth,Y=resp,folds=leftout,
score="loglik")
# Optimize by using marginal likelihood criterion
jointlambdas2 <- optLambdas_mgcvWrap(penaltiesinit=lambdas, XXblocks=XXmirmeth,</pre>
Y=resp)
# Optimal lambdas
optlambdas <- jointlambdas2$optpen
```

optLambdas\_mgcvWrap Find optimal ridge penalties with sequential optimization.

# Description

Sequentially optimizes a marginal likelihood score w.r.t. ridge penalties for multiple data blocks.

# Usage

```
optLambdas_mgcvWrap(penaltiesinit=NULL, XXblocks,Y, pairing=NULL, model=NULL, reltol=1e-4,
  optmethod1= "SANN", optmethod2 =ifelse(length(penaltiesinit)==1,"Brent", "Nelder-Mead"),
  maxItropt1=10,maxItropt2=25,tracescore=TRUE,fixedseed =TRUE, pref=NULL, fixedpen=NULL,
  sigmasq = 1, opt.sigma=ifelse(model=="linear",TRUE, FALSE))
```

# **Arguments**

penaltiesinit	Numeric vector. Initial values for penaltyparameters. May be obtained from fastCV2.
XXblocks	List of nxn matrices. Usually output of createXXblocks.
Υ	Response vector: numeric, binary, factor or survival.
pairing	Numerical vector of length 3 or NULL when pairs are absent. Represents the indices (in XXblocks) of the two data blocks involved in pairing, plus the index of the paired block.
model	Character. Any of c("linear", "logistic", "cox"). Is inferred from Y when NULL.
reltol	Scalar. Relative tolerance for optimization methods.
optmethod1	Character. First, global search method. Any of the methods c("Brent", "Nelder-Mead", "Sann") may be used, but simulated annealing by "Sann" is recommended to search a wide landscape. Other unconstrained methods offered by optim may also be used, but have not been tested.
optmethod2	Character. Second, local search method. Any of the methods c("Brent", "Nelder-Mead", "Sann") may be used, but "Nelder-Mead" is generally recommended. Other unconstrained methods offered by optim may also be used, but have not been tested.
maxItropt1	Integer. Maximum number of iterations for optmethod1.
maxItropt2	Integer. Maximum number of iterations for optmethod2.
tracescore	Boolean. Should the output of the scores be traced?
fixedseed	Boolean. Should the initialization be fixed? For reproducibility.
pref	Integer vector or NULL. Contains indices of data types in XXblocks that are preferential.
fixedpen	Integer vector or NULL. Contains indices of data types of which penalty is fixed to the corresponding value in penaltiesinit.
sigmasq	Default error variance.
opt.sigma	Boolean. Should the error variance be optimized as well? Only relevant for model="linear".

30 predictIWLS

#### **Details**

As opposed to optLambdas\_mgcv this function first searches globally, then locally. Hence, more time-consuming, but better guarded against multiple local optima. See gam for details on how the marginal likelihood is computed.

#### Value

List, with components:

res Outputs of all optimizers used

lambdas List of penalties found by the optimizers optpen Numerical vector with final, optimal penalties

#### References

Wood, S. N. (2011), Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models, J. Roy. Statist. Soc., B 73(1), 3-36.

#### See Also

optLambdas\_mgcv for one-pass optimization. A full demo and data are available from: https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

predictIWLS Predictions from ridge fits

### **Description**

Produces predictions from ridge fits for new data.

#### Usage

```
predictIWLS(IWLSfit, X1new = NULL, Sigmanew)
```

#### **Arguments**

IWLSfit List, containing fits from either IWLSridge (linear, logistic ridge) or IWLSCoxridge

X1new Matrix. Dimension nnew x p\_0, representing unpenalized covariates for new

data.

Sigmanew Matrix. Dimensions nnew x n. Sample cross-product from penalized variables,

usually computed by first applying createXXblocks and then SigmaFromBlocks.

#### Details

Predictions rely purely on the linear predictors, and do not require producing the parameter vector.

Scoring 31

#### Value

Numerical vector of linear predictor for the test samples.

#### See Also

IWLSridge (IWLSCoxridge) for fitting linear and logistic ridge (Cox ridge). betasout for obtaining parameter estimates. Scoring to evaluate the predictions. A full demo and data are available from: https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

# Examples

```
#Example below shows how to create the input argument Sigmanew (for simulated data)
Xbl1 <- matrix(rnorm(1000),nrow=10)</pre>
Xbl2 <- matrix(rnorm(2000),nrow=10)</pre>
Xbl1new <- matrix(rnorm(200),nrow=2)</pre>
Xbl2new <- matrix(rnorm(400),nrow=2)</pre>
#check whether dimensions are correct
nrow(Xbl1)==nrow(Xbl1new)
nrow(Xbl2)==nrow(Xbl2new)
ncol(Xbl1)==nrow(Xbl2)
ncol(Xbl1new)==ncol(Xbl2new)
#create cross-product
XXbl <- createXXblocks(list(Xbl1, Xbl2), list(Xbl1new, Xbl2new))</pre>
#suppose penalties for two data types equal 5,10, respectively
Sigmanew <- SigmaFromBlocks(XXbl,c(5,10))</pre>
#check dimensions (should be nnew x n)
dim(Sigmanew)
```

Scoring

Evaluate predictions

#### **Description**

Evaluates predictions by a score suitable for the corresponding response

# Usage

```
Scoring(lp, Y, model = NULL, score = ifelse(model == "linear", "mse", "loglik"),
    print = TRUE)
```

32 setupParallel

#### **Arguments**

lp Numerical vector. Linear predictor.

Y Response vector: numeric, binary, factor or survival.

score Character. See Details.

model Character. Any of c("linear", "logistic", "cox"). Is inferred from Y when

NULL.

print Boolean. Should the score be printed on screen.

#### **Details**

Several scores are allowed, depending on the type of output. For model = "linear", score equals any of c("loglik", "mse", "abserror", "cor", "kendall", "spearman"), denoting CV-ed log-likelihood, mean-squared error, mean absolute error, Pearson (Kendall, Spearman) correlation with response. For model = "logistic", score equals any of c("loglik", "auc", "brier"), denoting CV-ed log-likelihood, area-under-the-ROC-curve, and brier score a.k.a. MSE. For model = "cox", score equals any of c("loglik", "cindex"), denoting CV-ed log-likelihood, and c-index.

#### Value

Numerical value.

#### See Also

CVscore for obtaining the cross-validated score (for given penalties), and doubleCV to obtain doubly cross-validated linear predictors to which Scoring can be applied to estimated predictive performance by double cross-validation. A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

setupParallel

Setting up parallel computing

# Description

This function sets up parallel computing by the package snowfall.

#### Usage

```
setupParallel(ncpus = 2, sourcefile = NULL, sourcelibraries =
c("multiridge", "survival", "pROC", "risksetROC"))
```

### **Arguments**

ncpus Integer. Number of cpus to use. Should be  $\geq 2$ .

sourcefile Character. Additional source files to be loaded in parallel. Only required when

parallel computing is also desired for functions not available in multiridge.

sourcelibraries

Character vector. Libraries to be loaded in parallel. Defaults to the libraries

multiridge depends on.

SigmaFromBlocks 33

#### **Details**

Parallel computing is available for several functions that rely on cross-validation. If double CV is used, parallel computing is applied to the outer loop, to optimize efficiency.

#### Value

No return value, called for side effects

#### See Also

Snowfall package for further documentation on parallel computing. A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

# **Examples**

```
## Not run:
setupParallel(ncpus=4)
## End(Not run)
```

SigmaFromBlocks

Create penalized sample cross-product matrix

# **Description**

Creates penalized sample cross-product matrix, dimension nxn.

### Usage

```
SigmaFromBlocks(XXblocks, penalties, pairing = NULL)
```

#### **Arguments**

XXblocks List of nxn matrices. Usually output of createXXblocks.

penalties Numeric vector, representing penaltyparameters.

pairing Numerical vector of length 3 or NULL when pairs are absent. Represents the

indices (in XXblocks) of the two data blocks involved in pairing, plus the index

of the paired block.

#### Value

Matrix of size nxn.

#### See Also

A full demo and data are available from:

https://drive.google.com/open?id=1NUfeOtN8-KZ8A2HZzveG506nBwgW64e4

34 SigmaFromBlocks

```
#Example
#Simulate
Xbl1 <- matrix(rnorm(1000),nrow=10)
Xbl2 <- matrix(rnorm(2000),nrow=10)

#check whether dimensions are correct
ncol(Xbl1)==nrow(Xbl2)

#create cross-product
XXbl <- createXXblocks(list(Xbl1,Xbl2))

#suppose penalties for two data types equal 5,10, respectively
Sigma <- SigmaFromBlocks(XXbl,c(5,10))

#check dimensions (should be n x n)
dim(Sigma)</pre>
```

# **Index**

```
* datasets
    dataXXmirmeth, 11
* package
    multiridge-package, 2
augment, 4
betasout, 3, 5, 16-19, 31
createXblocks, 6, 7, 8
createXXblocks, 3, 5, 7, 8, 10, 12, 20, 21, 23,
         25, 27, 29, 30, 33
CVfolds, 9, 10, 23–26
CVscore, 3, 10, 20, 32
dataXXmirmeth, 3, 11
doubleCV, 3, 11, 12, 22, 32
fastCV2, 3, 12, 15, 21, 23-27, 29
gam, 20, 28, 30
IWLSCoxridge, 3, 6, 16, 18, 19, 30, 31
IWLSridge, 3, 6, 17, 18, 30, 31
mgcv_lambda, 19
mlikCV, 3, 20
multiridge (multiridge-package), 2
multiridge-package, 2
optim, 13, 21, 23, 25–27, 29
optLambdas, 14, 15, 23, 26
optLambdas_mgcv, 22, 27, 30
optLambdas_mgcvWrap, 3, 22, 28, 29
optLambdasWrap, 3, 14, 15, 24, 25
predictIWLS, 3, 17, 19, 30
Scoring, 10, 14, 22, 24, 26, 31, 31
setupParallel, 3, 10, 13, 15, 21, 24, 26, 32
SigmaFromBlocks, 3, 16, 18, 30, 33
```