# Package 'personalized'

July 23, 2025

```
Type Package
Title Estimation and Validation Methods for Subgroup Identification
     and Personalized Medicine
Version 0.2.7
Description Provides functions for fitting and validation of models for subgroup
     identification and personalized medicine / precision medicine under the general subgroup
     identification framework of Chen et al. (2017) <doi:10.1111/biom.12676>.
     This package is intended for use for both randomized controlled trials and
     observational studies and is described in detail in Huling and Yu (2021)
     <doi:10.18637/jss.v098.i05>.
URL https://jaredhuling.org/personalized/,
     https://arxiv.org/abs/1809.07905
BugReports https://github.com/jaredhuling/personalized/issues
License GPL-2
Encoding UTF-8
LazyData true
Suggests knitr, rmarkdown, testthat, nnet
Imports survival, methods, kernlab, foreach, xgboost
Depends glmnet (>= 2.0-13), mgcv, ggplot2, plotly
RoxygenNote 7.2.0
VignetteBuilder knitr
NeedsCompilation no
Author Jared Huling [aut, cre] (ORCID:
      <https://orcid.org/0000-0003-0670-4845>),
     Aaron Potvien [ctb],
     Alexandros Karatzoglou [cph],
     Alex Smola [cph]
Maintainer Jared Huling < jaredhuling@gmail.com>
Repository CRAN
Date/Publication 2022-06-27 20:20:03 UTC
```

2 check.overlap

# **Contents**

	check.overlap	2
	create.augmentation.function	4
	create.propensity.function	6
	fit.subgroup	8
	LaLonde	19
	plot.subgroup_fitted	21
	plotCompare	23
	predict.subgroup_fitted	25
	print.individual_treatment_effects	27
	print.subgroup_fitted	28
	subgroup.effects	29
	summarize.subgroups	30
	summary.subgroup_fitted	32
	treatment.effects	32
	validate.subgroup	35
	weighted.ksvm	39
Index		41

check.overlap

Check propensity score overlap

# Description

Results in a plot to check whether the propensity score has adequate overlap between treatment groups

# Usage

```
check.overlap(
    x,
    trt,
    propensity.func,
    type = c("histogram", "density", "both"),
    bins = 50L,
    alpha = ifelse(type == "both", 0.35, 0.5)
)
```

## **Arguments**

x The design matrix (not including intercept term)

trt treatment vector with each element equal to a 0 or a 1, with 1 indicating treatment status is active.

check.overlap 3

propensity.func

function that inputs the design matrix x and the treatment vector trt and outputs the propensity score, ie  $Pr(trt = 1 \mid X = x)$ . Function should take two arguments 1) x and 2) trt. See example below. For a randomized controlled trial this can simply be a function that returns a constant equal to the proportion of patients assigned to the treatment group, i.e.: propensity.func = function(x, trt) 0.5.

type

Type of plot to create. Options are either a histogram (type = "histogram") for each treatment group, a density (type = "density") for each treatment group, or to plot both a density and histogram (type = "code")

bins

integer number of bins for histograms when type = "histogram"

alpha

value between 0 and 1 indicating transparency level (1 for solid, 0 for fully transparent)

## -----F

```
library(personalized)
set.seed(123)
n.obs <- 250
n.vars <- 15
x \leftarrow matrix(rnorm(n.obs * n.vars, sd = 3), n.obs, n.vars)
# simulate non-randomized treatment
xbetat <-0.25 + 0.5 * x[,11] - 0.5 * x[,12]
trt.prob <- exp(xbetat) / (1 + exp(xbetat))</pre>
         <- rbinom(n.obs, 1, prob = trt.prob)
trt01
# create function for fitting propensity score model
prop.func <- function(x, trt)</pre>
{
    # fit propensity score model
    propens.model <- cv.glmnet(y = trt,</pre>
                                x = x, family = "binomial")
    pi.x <- predict(propens.model, s = "lambda.min",</pre>
                    newx = x, type = "response")[,1]
    pi.x
}
check.overlap(x = x,
              trt = trt01,
              propensity.func = prop.func)
# now add density plot with histogram
check.overlap(x = x,
               trt = trt01,
              type = "both",
              propensity.func = prop.func)
```

```
# simulated non-randomized treatment with multiple levels
xbetat_1 <- 0.15 + 0.5 * x[,9] - 0.25 * x[,12]
xbetat_2 <- 0.15 - 0.5 * x[,11] + 0.25 * x[,15]
trt.1.prob <- exp(xbetat_1) / (1 + exp(xbetat_1) + exp(xbetat_2))</pre>
trt.2.prob <- exp(xbetat_2) / (1 + exp(xbetat_1) + exp(xbetat_2))</pre>
trt.3.prob <- 1 - (trt.1.prob + trt.2.prob)</pre>
prob.mat <- cbind(trt.1.prob, trt.2.prob, trt.3.prob)</pre>
       <- apply(prob.mat, 1, function(rr) rmultinom(1, 1, prob = rr))</pre>
trt
       <- apply(trt, 2, function(rr) which(rr == 1))
# use multinomial logistic regression model with lasso penalty for propensity
propensity.multinom.lasso <- function(x, trt)</pre>
{
    if (!is.factor(trt)) trt <- as.factor(trt)</pre>
   gfit <- cv.glmnet(y = trt, x = x, family = "multinomial")</pre>
    # predict returns a matrix of probabilities:
    # one column for each treatment level
    propens <- drop(predict(gfit, newx = x, type = "response", s = "lambda.min",</pre>
                             nfolds = 5, alpha = 0)
    # return the probability corresponding to the
    # treatment that was observed
    probs <- propens[,match(levels(trt), colnames(propens))]</pre>
    probs
}
check.overlap(x = x,
              trt = trt,
              type = "histogram",
              propensity.func = propensity.multinom.lasso)
```

create.augmentation.function

Creation of augmentation functions

## **Description**

Creates an augmentation function that optionally utilizes cross-fitting

# Usage

```
create.augmentation.function(
  family,
  crossfit = TRUE,
  nfolds.crossfit = 10,
```

```
cv.glmnet.args = NULL
)
```

#### Arguments

family

The response type (see options in glmnet help file)

crossfit

A logical value indicating whether to use cross-fitting (TRUE) or not (FALSE).

Cross-fitting is more computationally intensive, but helps to prevent overfitting, see Chernozhukov, et al. (2018)

nfolds.crossfit

An integer specifying the number of folds to use for cross-fitting. Must be greater than 1

cv.glmnet.args

A list of NAMED arguments to pass to the cv.glmnet function. For example, cv.glmnet.args = list(type.measure = "mse", nfolds = 10). See cv.glmnet and glmnet for all possible options.

#### Value

A function which can be passed to the augment. func argument of the fit.subgroup function.

#### References

Chernozhukov, V., Chetverikov, D., Demirer, M., Duflo, E., Hansen, C., Newey, W., & Robins, J. (2018). Double/debiased machine learning for treatment and structural parameters https://arxiv.org/abs/1608.00060

#### See Also

 $\label{limiting} \textbf{fit.subgroup} \ \ \textbf{for} \ \ \textbf{estimating} \ \ \textbf{ITRs} \ \ \textbf{and} \ \ \textbf{create.propensity}. \ \ \textbf{function} \ \ \textbf{for} \ \ \textbf{creation} \ \ \textbf{of} \ \ \textbf{propensity}.$ 

```
library(personalized)

set.seed(123)
n.obs <- 500
n.vars <- 15
x <- matrix(rnorm(n.obs * n.vars, sd = 3), n.obs, n.vars)

# simulate non-randomized treatment
xbetat <- 0.5 + 0.5 * x[,7] - 0.5 * x[,9]
trt.prob <- exp(xbetat) / (1 + exp(xbetat))
trt01 <- rbinom(n.obs, 1, prob = trt.prob)

trt <- 2 * trt01 - 1

# simulate response
# delta below drives treatment effect heterogeneity</pre>
```

```
delta <- 2 * (0.5 + x[,2] - x[,3] - x[,11] + x[,1] * x[,12])
xbeta \leftarrow x[,1] + x[,11] - 2 * x[,12]^2 + x[,13] + 0.5 * x[,15] ^ 2
xbeta <- xbeta + delta * trt</pre>
# continuous outcomes
y <- drop(xbeta) + rnorm(n.obs, sd = 2)
aug.func <- create.augmentation.function(family = "gaussian",</pre>
                                           crossfit = TRUE,
                                           nfolds.crossfit = 10,
                                           cv.glmnet.args = list(type.measure = "mae",
                                                                  nfolds = 5))
prop.func <- create.propensity.function(crossfit = TRUE,</pre>
                                          nfolds.crossfit = 10,
                                          cv.glmnet.args = list(type.measure = "auc",
                                                                 nfolds = 5))
## Not run:
subgrp.model \leftarrow fit.subgroup(x = x, y = y,
                              trt = trt01,
                              propensity.func = prop.func,
                              augment.func = aug.func,
                              loss = "sq_loss_lasso",
                              nfolds = 10) # option for cv.glmnet (for ITR estimation)
summary(subgrp.model)
## End(Not run)
```

create.propensity.function

Creation of propensity fitting function

#### **Description**

Creates an propensity function that optionally utilizes cross-fitting

#### Usage

```
create.propensity.function(
  crossfit = TRUE,
  nfolds.crossfit = 10,
  cv.glmnet.args = NULL
)
```

#### **Arguments**

crossfit

A logical value indicating whether to use cross-fitting (TRUE) or not (FALSE). Cross-fitting is more computationally intensive, but helps to prevent overfitting, see Chernozhukov, et al. (2018)

```
nfolds.crossfit
```

An integer specifying the number of folds to use for cross-fitting. Must be greater than 1

#### Value

A function which can be passed to the augment. func argument of the fit.subgroup function.

#### References

Chernozhukov, V., Chetverikov, D., Demirer, M., Duflo, E., Hansen, C., Newey, W., & Robins, J. (2018). Double/debiased machine learning for treatment and structural parameters https://arxiv.org/abs/1608.00060

#### See Also

fit.subgroup for estimating ITRs and create.propensity.function for creation of propensity functions

```
library(personalized)
set.seed(123)
n.obs <- 500
n.vars <- 15
x \leftarrow matrix(rnorm(n.obs * n.vars, sd = 3), n.obs, n.vars)
# simulate non-randomized treatment
xbetat <-0.5 + 0.5 * x[,7] - 0.5 * x[,9]
trt.prob <- exp(xbetat) / (1 + exp(xbetat))</pre>
      <- rbinom(n.obs, 1, prob = trt.prob)
trt01
trt
         <- 2 * trt01 - 1
# simulate response
# delta below drives treatment effect heterogeneity
delta <- 2 * (0.5 + x[,2] - x[,3] - x[,11] + x[,1] * x[,12])
xbeta \leftarrow x[,1] + x[,11] - 2 * x[,12]^2 + x[,13] + 0.5 * x[,15] ^ 2
xbeta <- xbeta + delta * trt
# continuous outcomes
y <- drop(xbeta) + rnorm(n.obs, sd = 2)
aug.func <- create.augmentation.function(family = "gaussian",</pre>
                                          crossfit = TRUE,
                                          nfolds.crossfit = 10,
                                          cv.glmnet.args = list(type.measure = "mae",
```

fit.subgroup

Fitting subgroup identification models

## Description

Fits subgroup identification model class of Chen, et al (2017)

## Usage

```
fit.subgroup(
  х,
 у,
  trt,
  propensity.func = NULL,
  loss = c("sq_loss_lasso", "logistic_loss_lasso", "poisson_loss_lasso",
   "cox_loss_lasso", "owl_logistic_loss_lasso", "owl_logistic_flip_loss_lasso",
    "owl_hinge_loss", "owl_hinge_flip_loss", "sq_loss_lasso_gam",
    "poisson_loss_lasso_gam", "logistic_loss_lasso_gam", "sq_loss_gam",
    "poisson_loss_gam", "logistic_loss_gam", "owl_logistic_loss_gam",
    "owl_logistic_flip_loss_gam", "owl_logistic_loss_lasso_gam",
    "owl_logistic_flip_loss_lasso_gam", "sq_loss_xgboost", "custom"),
  method = c("weighting", "a_learning"),
 match.id = NULL,
  augment.func = NULL,
  fit.custom.loss = NULL,
  cutpoint = 0,
  larger.outcome.better = TRUE,
  reference.trt = NULL,
  retcall = TRUE,
)
```

#### **Arguments**

x The design matrix (not including intercept term)

y The response vector

trt treatment vector with each element equal to a 0 or a 1, with 1 indicating treatment status is active.

propensity.func

function that inputs the design matrix x and the treatment vector trt and outputs the propensity score, ie  $Pr(trt = 1 \mid X = x)$ . Function should take two arguments 1) x and 2) trt. See example below. For a randomized controlled trial this can simply be a function that returns a constant equal to the proportion of patients assigned to the treatment group, i.e.: propensity.func = function(x, trt) 0.5.

loss

### • Continuous Outcomes

- "sq\_loss\_lasso"  $M(y, v) = (v y) ^ 2$  with linear model and lasso penalty
- "owl\_logistic\_loss\_lasso" M(y, v) = ylog(1 + exp{-v}) (method of Regularized Outcome Weighted Subgroup Identification)
- "owl\_logistic\_flip\_loss\_lasso"  $M(y, v) = |y|log(1 + exp{-sign(y)v})$
- "owl\_hinge\_loss" M(y, v) = ymax(0, 1 v) (method of Estimating individualized treatment rules using outcome weighted learning)
- "owl\_hinge\_flip\_loss" M(y, v) = lylmax(0, 1 sign(y)v)
- "sq\_loss\_lasso\_gam"  $M(y, v) = (v y) ^ 2$  with variables selected by lasso penalty and generalized additive model fit on the selected variables
- "sq\_loss\_gam"  $M(y, v) = (v y) ^ 2$  with generalized additive model fit on all variables
- "owl\_logistic\_loss\_gam"  $M(y, v) = ylog(1 + exp{-v})$  with generalized additive model fit on all variables
- "owl\_logistic\_flip\_loss\_gam"  $M(y, v) = |y|log(1 + exp{-sign}(y)v)$  with generalized additive model fit on all variables

- "owl\_logistic\_loss\_lasso\_gam" M(y, v) = ylog(1 + exp{-v}) with variables selected by lasso penalty and generalized additive model fit on the selected variables
- "owl\_logistic\_flip\_loss\_lasso\_gam"  $M(y, v) = |y|log(1 + exp{-sign(y)v})$  with variables selected by lasso penalty and generalized additive model fit on the selected variables
- "sq\_loss\_xgboost"  $M(y, v) = (v y) ^ 2$  with gradient-boosted decision trees model

#### • Binary Outcomes

- All losses for continuous outcomes can be used plus the following:
- "logistic\_loss\_lasso" M(y, v) = -[yv  $log(1 + exp{-v})$ ] with with linear model and lasso penalty
- "logistic\_loss\_lasso\_gam"  $M(y, v) = -[yv log(1 + exp{-v})]$  with variables selected by lasso penalty and generalized additive model fit on the selected variables
- "logistic\_loss\_gam" M(y, v) = -[yv  $log(1 + exp{-v})$ ] with generalized additive model fit on all variables

#### Count Outcomes

- All losses for continuous outcomes can be used plus the following:
- "poisson\_loss\_lasso" M(y, v) = -[yv exp(v)] with with linear model and lasso penalty
- "poisson\_loss\_lasso\_gam" M(y, v) = -[yv exp(v)] with variables selected by lasso penalty and generalized additive model fit on the selected variables
- "poisson\_loss\_gam" M(y, v) = -[yv exp(v)] with generalized additive model fit on all variables

#### • Time-to-Event Outcomes

 "cox\_loss\_lasso" - M corresponds to the negative partial likelihood of the cox model with linear model and additionally a lasso penalty

method

subgroup ID model type. Either the weighting or A-learning method of Chen et al, (2017)

match.id

a (character, factor, or integer) vector with length equal to the number of observations in x indicating using integers or levels of a factor vector which patients are in which matched groups. Defaults to NULL and assumes the samples are not from a matched cohort. Matched case-control groups can be created using any method (propensity score matching, optimal matching, etc). If each case is matched with a control or multiple controls, this would indicate which case-control pairs or groups go together. If match. id is supplied, then it is unecessary to specify a function via the propensity. func argument. A quick usage example: if the first patient is a case and the second and third are controls matched to it, and the fouth patient is a case and the fifth through seventh patients are matched with it, then the user should specify match.id = c(1,1,1,2,2,2,2) or match.id = c(rep("Grp1", 3), rep("Grp2", 4))

augment.func

function which inputs the response y, the covariates x, and trt and outputs predicted values (on the link scale) for the response using a model constructed with x. augment.func() can also be simply a function of x and y. This function is

used for efficiency augmentation. When the form of the augmentation function is correct, it can provide efficient estimation of the subgroups. Some examples of possible augmentation functions are:

Example 1: augment.func <- function(x, y)  $\{lmod <- lm(y \sim x); return(fitted(lmod))\}$ Example 2:

```
augment.func <- function(x, y, trt) {
    data <- data.frame(x, y, trt)
    lmod <- lm(y ~ x * trt)
    ## get predictions when trt = 1
    data$trt <- 1
    preds_1 <- predict(lmod, data)

## get predictions when trt = -1
    data$trt <- -1
    preds_n1 <- predict(lmod, data)

## return predictions averaged over trt
    return(0.5 * (preds_1 + preds_n1))
}</pre>
```

For binary and time-to-event outcomes, make sure that predictions are returned on the scale of the predictors

Example 3:

```
augment.func <- function(x, y) {
    bmod <- glm(y ~ x, family = binomial())
    return(predict(bmod, type = "link"))
}</pre>
```

fit.custom.loss

A function which *minimizes* a user-specified custom loss function M(y,v) to be used in model fitting. If provided, fit.custom.loss should take the modified design matrix (which includes an intercept term) as an argument and the responses and optimize a custom weighted loss function.

The loss function M(y,v) to be minimized  $\operatorname{MUST}$  meet the following two criteria:

- 1.  $D_M(y,v) = \partial M(y,v)/\partial v$  must be increasing in v for each fixed y.  $D_M(y,v)$  is the partial derivative of the loss function M(y, v) with respect to v
- 2.  $D_M(y,0)$  is monotone in y

An example of a valid loss function is  $M(y,v)=(y-v)^2$ . In this case  $D_M(y,v)=-2(y-v)$ . See Chen et al. (2017) for more details on the restrictions on the loss function M(y,v).

The provided function **MUST** return a list with the following elements:

 predict a function that inputs a design matrix and a 'type' argument for the type of predictions and outputs a vector of predictions on the scale of the linear predictor. Note that the matrix provided to 'fit.custom.loss'

has a column appended to the first column of x corresponding to the treatment main effect. Thus, the prediction function should deal with this, e.g. predict(model, cbind(1, x))

- model a fitted model object returned by the underlying fitting function
- coefficients if the underlying fitting function yields a vector of coefficient estimates, they should be provided here

The provided function **MUST** be a function with the following arguments:

- 1. x design matrix
- 2. y vector of responses
- 3. weights vector for observations weights. The underlying loss function **MUST** have samples weighted according to this vector. See below example
- 4. ... additional arguments passed via '...'. This can be used so that users can specify more arguments to the underlying fitting function if so desired.

The provided function can also optionally take the following arguments:

- match.id vector of case/control cluster IDs. This is useful if cross validation is used in the underlying fitting function in which case it is advisable to sample whole clusters randomly instead of individual observations.
- offset if efficiency augmentation is used, the predictions from the outcome model from augment. func will be provided via the offset argument, which can be used as an offset in the underlying fitting function as a means of incorporating the efficiency augmentation model's predictions
- trt vector of treatment statuses
- family family of outcome
- n.trts numer of treatment levels. Can be useful if there are more than 2 treatment levels

```
Example 1: Here we minimize M(y, v) = (y - v)^2
 fit.custom.loss <- function(x, y, weights, ...) {</pre>
     df <- data.frame(y = y, x)
     # minimize squared error loss with NO lasso penalty
     lmf <- lm(y \sim x - 1, weights = weights,
               data = df, ...)
     # save coefficients
     cfs = coef(lmf)
     # create prediction function. Notice
     # how a column of 1's is appended
     # to ensure treatment main effects are included
     # in predictions
     prd = function(x, type = "response")
     {
         dfte <- cbind(1, x)
         colnames(dfte) <- names(cfs)</pre>
         predict(lmf, data.frame(dfte))
```

```
# return lost of required components
     list(predict = prd, model = lmf, coefficients = cfs)
 }
Example 2: M(y, v) = y \exp(-v)
 fit.expo.loss <- function(x, y, weights, ...)</pre>
     ## define loss function to be minimized
     expo.loss <- function(beta, x, y, weights) {</pre>
         sum(weights * y * exp(-drop(tcrossprod(x, t(beta))))
     }
     # use optim() to minimize loss function
   opt <- optim(rep(0, NCOL(x)), fn = expo.loss, x = x, y = y, weights = weights)
     coefs <- opt$par
     pred <- function(x, type = "response") {</pre>
         tcrossprod(cbind(1, x), t(coefs))
     }
     # return list of required components
     list(predict = pred, model = opt, coefficients = coefs)
 }
```

cutpoint

numeric value for patients with benefit scores above which (or below which if larger.outcome.better = FALSE) will be recommended to be in the treatment group. Can also set cutpoint = "median", which will use the median value of the benefit scores as the cutpoint or can set specific quantile values via "quantx" where "x" is a number between 0 and 100 representing the quantile value; e.g. cutpoint = "quant75" will use the 75th perent upper quantile of the benefit scores as the quantile.

#### larger.outcome.better

boolean value of whether a larger outcome is better/preferable. Set to TRUE if a larger outcome is better/preferable and set to FALSE if a smaller outcome is better/preferable. Defaults to TRUE.

reference.trt

which treatment should be treated as the reference treatment. Defaults to the first level of trt if trt is a factor or the first alphabetical or numerically first treatment level. Not used for multiple treatment fitting with OWL-type losses.

retcall

boolean value. if TRUE then the passed arguments will be saved. Do not set to FALSE if the validate.subgroup() function will later be used for your fitted subgroup model. Only set to FALSE if memory is limited as setting to TRUE saves the design matrix to the fitted object

• • •

options to be passed to underlying fitting function. For all loss options with 'lasso', this will be passed to cv.glmnet. For all loss options with 'gam', this

will be passed to gam from the **mgcv** package Note that for all loss options that use gam() from the **mgcv** package, the user cannot supply the gam argument method because it is also an argument of fit.subgroup, so instead, to change the gam method argument, supply method.gam, ie method.gam = "REML".

For all loss options with 'hinge', this will be passed to both weighted.ksvm and ipop from the **kernlab** package

#### Value

An object of class "subgroup\_fitted".

predict A function that returns predictions of the covariate-conditional treatment effects

model An object returned by the underlying fitting function used. For example, if the

lasso use used to fit the underlying subgroup identification model, this will be

an object returned by cv.glmnet.

will contain the estimated coefficients of the model.

call The call that produced the returned object. If retcall = TRUE, this will contain

all objects supplied to fit.subgroup()

family The family corresponding to the outcome provided

loss The loss function used

method The method used (either weighting or A-learning)

propensity.func

The propensity score function used

larger.outcome.better

If larger outcomes are preferred for this model

cutpoint Benefit score cutoff value used for determining subgroups

var.names The names of all variables used n.trts The number of treatment levels

comparison.trts

All treatment levels other than the reference level

reference.trt The reference level for the treatment. This should usually be the control group/level

trts All treatment levels

trt.received The vector of treatment assignments

pi.x A vector of propensity scores

y A vector of outcomes

benefit.scores A vector of conditional treatment effects, i.e. benefit scores

recommended.trts

A vector of treatment recommendations (i.e. for each patient, which treatment

results in the best expected potential outcomes)

subgroup.trt.effects

(Biased) estimates of the conditional treatment effects and conditional outcomes. These are essentially just empirical averages within different combinations of treatment assignments and treatment recommendations

individual.trt.effects

estimates of the individual treatment effects as returned by treat.effects

#### References

Huling. J.D. and Yu, M. (2021), Subgroup Identification Using the personalized Package. Journal of Statistical Software 98(5), 1-60. doi:10.18637/jss.v098.i05

Chen, S., Tian, L., Cai, T. and Yu, M. (2017), A general statistical framework for subgroup identification and comparative treatment scoring. Biometrics. doi:10.1111/biom.12676 doi:10.1111/biom.12676

Xu, Y., Yu, M., Zhao, Y. Q., Li, Q., Wang, S., & Shao, J. (2015), Regularized outcome weighted subgroup identification for differential treatment effects. Biometrics, 71(3), 645-653. doi: 10.1111/biom.12322 doi:10.1111/biom.12322

Zhao, Y., Zeng, D., Rush, A. J., & Kosorok, M. R. (2012), Estimating individualized treatment rules using outcome weighted learning. Journal of the American Statistical Association, 107(499), 1106-1118. doi: 10.1080/01621459.2012.695674

#### See Also

validate.subgroup for function which creates validation results for subgroup identification models, predict.subgroup\_fitted for a prediction function for fitted models from fit.subgroup, plot.subgroup\_fitted for a function which plots results from fitted models, and print.subgroup\_fitted for arguments for printing options for fit.subgroup(). from fit.subgroup.

```
library(personalized)
set.seed(123)
n.obs <- 500
n.vars <- 15
x \leftarrow matrix(rnorm(n.obs * n.vars, sd = 3), n.obs, n.vars)
# simulate non-randomized treatment
xbetat <-0.5 + 0.5 * x[,7] - 0.5 * x[,9]
trt.prob <- exp(xbetat) / (1 + exp(xbetat))</pre>
       <- rbinom(n.obs, 1, prob = trt.prob)
trt01
trt
         <- 2 * trt01 - 1
# simulate response
# delta below drives treatment effect heterogeneity
delta <- 2 * (0.5 + x[,2] - x[,3] - x[,11] + x[,1] * x[,12] )
xbeta \leftarrow x[,1] + x[,11] - 2 * x[,12]^2 + x[,13] + 0.5 * x[,15] ^ 2
xbeta <- xbeta + delta * trt
# continuous outcomes
y \leftarrow drop(xbeta) + rnorm(n.obs, sd = 2)
# binary outcomes
y.binary \leftarrow 1 * (xbeta + rnorm(n.obs, sd = 2) > 0)
# count outcomes
```

```
y.count <- round(abs(xbeta + rnorm(n.obs, sd = 2)))</pre>
# time-to-event outcomes
surv.time \leftarrow \exp(-20 - xbeta + rnorm(n.obs, sd = 1))
cens.time \leftarrow exp(rnorm(n.obs, sd = 3))
y.time.to.event <- pmin(surv.time, cens.time)</pre>
               <- 1 * (surv.time <= cens.time)
# create function for fitting propensity score model
prop.func <- function(x, trt)</pre>
{
   # fit propensity score model
   propens.model <- cv.glmnet(y = trt,</pre>
                            x = x, family = "binomial")
   pi.x <- predict(propens.model, s = "lambda.min",</pre>
                  newx = x, type = "response")[,1]
   pi.x
}
subgrp.model \leftarrow fit.subgroup(x = x, y = y,
                         trt = trt01,
                         propensity.func = prop.func,
                         loss = "sq_loss_lasso",
                         # option for cv.glmnet,
                         # better to use 'nfolds=10'
                         nfolds = 3)
summary(subgrp.model)
# estimates of the individual-specific
# treatment effect estimates:
subgrp.model$individual.trt.effects
# fit lasso + gam model with REML option for gam
subgrp.modelg <- fit.subgroup(x = x, y = y,
                          trt = trt01,
                          propensity.func = prop.func,
                          loss = "sq_loss_lasso_gam",
                          method.gam = "REML", # option for gam
                          nfolds = 5)
                                                 # option for cv.glmnet
subgrp.modelg
## augmentation funcions involve modeling the conditional mean E[Y|T, X]
## and returning predictions that are averaged over the treatment values
```

```
## return <- 1/2 * (hat{E}[Y|T=1, X] + hat{E}[Y|T=-1, X])
augment.func <- function(x, y, trt) {</pre>
   data <- data.frame(x, y, trt)</pre>
   xm <- model.matrix(y~trt*x-1, data = data)</pre>
   lmod <- cv.glmnet(y = y, x = xm)
   ## get predictions when trt = 1
   data$trt <- 1
   xm <- model.matrix(y~trt*x-1, data = data)</pre>
   preds_1 <- predict(lmod, xm, s = "lambda.min")</pre>
   ## get predictions when trt = -1
   data$trt <- -1
   xm <- model.matrix(y~trt*x-1, data = data)</pre>
   preds_n1 <- predict(lmod, xm, s = "lambda.min")</pre>
   ## return predictions averaged over trt
   return(0.5 * (preds_1 + preds_n1))
}
subgrp.model.aug <- fit.subgroup(x = x, y = y,
                       trt = trt01,
                       propensity.func = prop.func,
                       augment.func = augment.func,
                       loss = "sq_loss_lasso",
                       # option for cv.glmnet,
                       # better to use 'nfolds=10'
                       nfolds = 3) # option for cv.glmnet
summary(subgrp.model.aug)
# use logistic loss for binary outcomes
subgrp.model.bin <- fit.subgroup(x = x, y = y.binary,
                       trt = trt01,
                       propensity.func = prop.func,
                       loss = "logistic_loss_lasso",
                       type.measure = "auc",  # option for cv.glmnet
                       nfolds = 3)
                                            # option for cv.glmnet
subgrp.model.bin
# use poisson loss for count/poisson outcomes
subgrp.model.poisson \leftarrow fit.subgroup(x = x, y = y.count,
                       trt = trt01,
```

```
propensity.func = prop.func,
                        loss = "poisson_loss_lasso",
                        type.measure = "mse",  # option for cv.glmnet
                        nfolds = 3)
                                             # option for cv.glmnet
subgrp.model.poisson
library(survival)
subgrp.model.cox <- fit.subgroup(x = x, y = Surv(y.time.to.event, status),</pre>
                        trt = trt01,
                        propensity.func = prop.func,
                        loss = "cox_loss_lasso",
                        nfolds = 3) # option for cv.glmnet
subgrp.model.cox
## Use custom loss function for binary outcomes
fit.custom.loss.bin <- function(x, y, weights, offset, ...) {</pre>
   df <- data.frame(y = y, x)
   # minimize logistic loss with NO lasso penalty
   # with allowance for efficiency augmentation
   glmf \leftarrow glm(y \sim x - 1, weights = weights,
              offset = offset, # offset term allows for efficiency augmentation
              family = binomial(), ...)
   # save coefficients
   cfs = coef(glmf)
   # create prediction function.
   prd = function(x, type = "response") {
        dfte <- cbind(1, x)
        colnames(dfte) <- names(cfs)</pre>
        ## predictions must be returned on the scale
        ## of the linear predictor
        predict(glmf, data.frame(dfte), type = "link")
   # return lost of required components
   list(predict = prd, model = glmf, coefficients = cfs)
}
subgrp.model.bin.cust <- fit.subgroup(x = x, y = y.binary,
                             trt = trt01,
```

LaLonde 19

```
propensity.func = prop.func,
                                  fit.custom.loss = fit.custom.loss.bin)
subgrp.model.bin.cust
## try exponential loss for
## positive outcomes
fit.expo.loss <- function(x, y, weights, ...)</pre>
    expo.loss <- function(beta, x, y, weights) {</pre>
        sum(weights * y * exp(-drop(x %*% beta)))
    }
    # use optim() to minimize loss function
    opt <- optim(rep(0, NCOL(x)), fn = expo.loss, x = x, y = y, weights = weights)
    coefs <- opt$par</pre>
   pred <- function(x, type = "response") {</pre>
        tcrossprod(cbind(1, x), t(coefs))
    # return list of required components
    list(predict = pred, model = opt, coefficients = coefs)
}
# use exponential loss for positive outcomes
subgrp.model.expo <- fit.subgroup(x = x, y = y.count,
                                   trt = trt01,
                                   propensity.func = prop.func,
                                   fit.custom.loss = fit.expo.loss)
subgrp.model.expo
```

LaLonde

National Supported Work Study Data

# Description

The LaLonde dataset comes from the National Supported Work Study, which sought to evaluate the effectiveness of an employment trainining program on wage increases.

20 LaLonde

## **Usage**

LaLonde

#### **Format**

```
A data frame with 722 observations and 12 variables:

outcome whether earnings in 1978 are larger than in 1975; 1 for yes, 0 for no

treat whether the individual received the treatment; "Yes" or "No"

age age in years

educ education in years

black black or not; factor with levels "Yes" or "No"

hisp hispanic or not; factor with levels "Yes" or "No"

white white or not; factor with levels "Yes" or "No"

marr married or not; factor with levels "Yes" or "No"

nodegr No high school degree; factor with levels "Yes" (for no HS degree) or "No"

log.re75 log of earnings in 1975

u75 unemployed in 1975; factor with levels "Yes" or "No"

wts.extrap extrapolation weights to the 1978 Panel Study for Income Dynamics dataset
```

#### Source

The National Supported Work Study.

#### References

LaLonde, R.J. 1986. "Evaluating the econometric evaulations of training programs with experimental data." American Economic Review, Vol.76, No.4, pp. 604-620.

Egami N, Ratkovic M, Imai K (2017). **"FindIt**: Finding Heterogeneous Treatment Effects." R package version 1.1.2, https://CRAN.R-project.org/package=FindIt.

plot.subgroup\_fitted 21

```
const.propens <- function(x, trt)
{
    mean.trt <- mean(trt == "Trt")
    rep(mean.trt, length(trt))
}
subgrp_fit_w <- fit.subgroup(x = x, y = y, trt = trt,
    loss = "logistic_loss_lasso",
    propensity.func = const.propens,
    cutpoint = 0,
    type.measure = "auc",
    nfolds = 10)
summary(subgrp_fit_w)</pre>
```

plot.subgroup\_fitted Plotting results for fitted subgroup identification models

## Description

Plots results for estimated subgroup treatment effects

Plots validation results for estimated subgroup treatment effects

#### Usage

```
## S3 method for class 'subgroup_fitted'
plot(
    x,
    type = c("boxplot", "density", "interaction", "conditional"),
    avg.line = TRUE,
    ...
)

## S3 method for class 'subgroup_validated'
plot(
    x,
    type = c("boxplot", "density", "interaction", "conditional", "stability"),
    avg.line = TRUE,
    ...
)
```

#### **Arguments**

x type fitted object returned by validate.subgroup() or fit.subgroup() function type of plot. "density" results in a density plot for the results across all observations (if x is from fit.subgroup()) or if x is from validate.subgroup() across iterations of either the bootstrap or training/test re-fitting. For the latter case the test results will be plotted. "boxplot" results in boxplots across all

22 plot.subgroup\_fitted

observations/iterations of either the bootstrap or training/test re-fitting. For the latter case the test results will be plotted. "interaction" creates an interaction plot for the different subgroups (crossing lines here means a meaningful subgroup). For the interaction plot, the intervals around each point represent +1 one SE "conditional" For subgroup\_fitted objects, plots smoothed (via a GAM smoother) means of the outcomes as a function of the estimated benefit score separately for the treated and untreated groups. For subgroup\_validated objects, boxplots of summary statistics within subgroups will be plotted as subgroups are defined by different cutoffs of the benefit scores. These cutoffs can be specified via the benefit.score.quantiles argument of validate.subgroup.

avg.line

boolean value of whether or not to plot a line for the average value in addition to the density (only valid for type = "density")

. . . not used

#### See Also

fit. subgroup for function which fits subgroup identification models.

validate.subgroup for function which creates validation results and fit.subgroup for function which fits subgroup identification models.

```
library(personalized)
set.seed(123)
n.obs <- 250
n.vars <- 15
x \leftarrow matrix(rnorm(n.obs * n.vars, sd = 3), n.obs, n.vars)
# simulate non-randomized treatment
xbetat <-0.5 + 0.5 * x[,11] - 0.5 * x[,13]
trt.prob <- exp(xbetat) / (1 + exp(xbetat))</pre>
         <- rbinom(n.obs, 1, prob = trt.prob)
trt01
trt
         <- 2 * trt01 - 1
# simulate response
delta <- 2 * (0.5 + x[,2] - x[,3] - x[,11] + x[,1] * x[,12])
xbeta \leftarrow x[,1] + x[,11] - 2 * x[,12]^2 + x[,13]
xbeta <- xbeta + delta * trt
# continuous outcomes
y \leftarrow drop(xbeta) + rnorm(n.obs, sd = 2)
# create function for fitting propensity score model
prop.func <- function(x, trt)</pre>
{
    # fit propensity score model
    propens.model <- cv.glmnet(y = trt,</pre>
```

plotCompare 23

```
x = x, family = "binomial")
   pi.x <- predict(propens.model, s = "lambda.min",</pre>
                    newx = x, type = "response")[,1]
   pi.x
}
subgrp.model \leftarrow fit.subgroup(x = x, y = y,
                           trt = trt01,
                           propensity.func = prop.func,
                           loss = "sq_loss_lasso",
                           # option for cv.glmnet,
                           # better to use 'nfolds=10'
                           nfolds = 3)
                                                     # option for cv.glmnet
subgrp.model$subgroup.trt.effects
plot(subgrp.model)
plot(subgrp.model, type = "boxplot")
plot(subgrp.model, type = "interaction")
plot(subgrp.model, type = "conditional")
valmod <- validate.subgroup(subgrp.model, B = 3,</pre>
                          method = "training_test",
                          benefit.score.quantiles = c(0.25, 0.5, 0.75),
                          train.fraction = 0.75)
plot(valmod)
plot(valmod, type = "interaction")
# see how summary statistics of subgroups change
# when the subgroups are defined based on different cutoffs
# (25th quantile of bene score, 50th, and 75th)
plot(valmod, type = "conditional")
# visualize the frequency of particular variables
# of being selected across the resampling iterations with
# 'type = "stability"'
# not run:
# plot(valmod, type = "stability")
```

plotCompare

Plot a comparison results for fitted or validated subgroup identification models 24 plotCompare

## **Description**

Plots comparison of results for estimated subgroup treatment effects

#### Usage

```
plotCompare(
    ...,
    type = c("boxplot", "density", "interaction", "conditional"),
    avg.line = TRUE
)
```

#### **Arguments**

the fitted (model or validation) objects to be plotted. Must be either objects returned from fit.subgroup() or validate.subgroup()

type

type of plot. "density" results in a density plot for the results across all observations (if x is from fit.subgroup()) or if x is from validate.subgroup() across iterations of either the bootstrap or training/test re-fitting. For the latter case the test results will be plotted. "boxplot" results in boxplots across all observations/iterations of either the bootstrap or training/test re-fitting. For the latter case the test results will be plotted. "interaction" creates an interaction plot for the different subgroups (crossing lines here means a meaningful subgroup). "conditional" plots smoothed (via a GAM smoother) means of the outcomes as a function of the estimated benefit score separately for the treated and untreated groups.

avg.line

boolean value of whether or not to plot a line for the average value in addition to the density (only valid for type = "density")

## See Also

fit.subgroup for function which fits subgroup identification models and validate.subgroup for function which creates validation results.

```
library(personalized)

set.seed(123)
n.obs <- 100
n.vars <- 15
x <- matrix(rnorm(n.obs * n.vars, sd = 3), n.obs, n.vars)

# simulate non-randomized treatment
xbetat <- 0.5 + 0.5 * x[,1] - 0.5 * x[,4]
trt.prob <- exp(xbetat) / (1 + exp(xbetat))
trt01 <- rbinom(n.obs, 1, prob = trt.prob)

trt <- 2 * trt01 - 1</pre>
```

predict.subgroup\_fitted

```
# simulate response
delta <- 2 * (0.5 + x[,2] - x[,3] - x[,11] + x[,1] * x[,12])
xbeta \leftarrow x[,1] + x[,11] - 2 * x[,12]^2 + x[,13]
xbeta <- xbeta + delta * trt</pre>
# continuous outcomes
y \leftarrow drop(xbeta) + rnorm(n.obs, sd = 2)
# create function for fitting propensity score model
prop.func <- function(x, trt)</pre>
    # fit propensity score model
    propens.model <- cv.glmnet(y = trt,</pre>
                                x = x, family = "binomial")
    pi.x <- predict(propens.model, s = "lambda.min",</pre>
                     newx = x, type = "response")[,1]
    pi.x
}
subgrp.model \leftarrow fit.subgroup(x = x, y = y,
                             trt = trt01,
                             propensity.func = prop.func,
                            loss = "sq_loss_lasso",
                             # option for cv.glmnet,
                             # better to use 'nfolds=10'
                             nfolds = 3)
                                                       # option for cv.glmnet
subgrp.model.o \leftarrow fit.subgroup(x = x, y = y,
                            trt = trt01,
                             propensity.func = prop.func,
                             # option for cv.glmnet,
                             # better to use 'nfolds=10'
                             loss = "owl_logistic_flip_loss_lasso",
                             nfolds = 3)
plotCompare(subgrp.model, subgrp.model.o)
```

predict.subgroup\_fitted

Function to predict either benefit scores or treatment recommendations

#### **Description**

Predicts benefit scores or treatment recommendations based on a fitted subgroup identification model

Function to obtain predictions for weighted ksvm objects

#### Usage

```
## S3 method for class 'subgroup_fitted'
predict(
  object,
  newx,
  type = c("benefit.score", "trt.group"),
  cutpoint = 0,
  ...
)

## S3 method for class 'wksvm'
predict(object, newx, type = c("class", "linear.predictor"), ...)
```

## **Arguments**

object fitted object returned by validate.subgrp() function.

For predict.wksvm(), this should be a fitted wksvm object from the weighted.ksvm()

function

newx new design matrix for which predictions will be made

type type of prediction. type = "benefit.score" results in predicted benefit scores

and type = "trt.group" results in prediction of recommended treatment group.

For predict.wksvm(), type = 'class' yields predicted class and type = 'linear.predictor'

yields estimated function (the sign of which is the estimated class)

cutpoint numeric value for patients with benefit scores above which (or below which if

larger.outcome.better = FALSE) will be recommended to be in the treatment group. Can also set cutpoint = "median", which will use the median value of the benefit scores as the cutpoint or can set specific quantile values via "quantx" where "x" is a number between 0 and 100 representing the quantile value; e.g. cutpoint = "quant75" will use the 75th perent upper quantile of the benefit

scores as the quantile.

... not used

## See Also

fit.subgroup for function which fits subgroup identification models. weighted.ksvm for fitting weighted.ksvm objects

```
library(personalized)
set.seed(123)
n.obs <- 500
n.vars <- 15
x <- matrix(rnorm(n.obs * n.vars, sd = 3), n.obs, n.vars)</pre>
```

```
# simulate non-randomized treatment
xbetat <-0.5 + 0.5 * x[,11] - 0.5 * x[,3]
trt.prob <- exp(xbetat) / (1 + exp(xbetat))</pre>
       <- rbinom(n.obs, 1, prob = trt.prob)
trt
         <- 2 * trt01 - 1
# simulate response
delta <- 2 * (0.5 + x[,2] - x[,3] - x[,11] + x[,1] * x[,12])
xbeta \leftarrow x[,1] + x[,11] - 2 * x[,12]^2 + x[,13]
xbeta <- xbeta + delta * trt
# continuous outcomes
y \leftarrow drop(xbeta) + rnorm(n.obs, sd = 2)
# create function for fitting propensity score model
prop.func <- function(x, trt)</pre>
{
    # fit propensity score model
    propens.model <- cv.glmnet(y = trt,</pre>
                               x = x, family = "binomial")
   pi.x <- predict(propens.model, s = "lambda.min",</pre>
                    newx = x, type = "response")[,1]
    pi.x
}
subgrp.model \leftarrow fit.subgroup(x = x, y = y,
                             trt = trt01,
                             propensity.func = prop.func,
                             loss = "sq_loss_lasso",
                             nfolds = 3)
                                                        # option for cv.glmnet
subgrp.model$subgroup.trt.effects
benefit.scores <- predict(subgrp.model, newx = x, type = "benefit.score")</pre>
rec.trt.grp <- predict(subgrp.model, newx = x, type = "trt.group")</pre>
```

```
print.individual_treatment_effects
```

Printing individualized treatment effects

## **Description**

Prints results for estimated subgroup treatment effects

#### Usage

```
## S3 method for class 'individual_treatment_effects'
print(x, digits = max(getOption("digits") - 3, 3), ...)
```

## Arguments

```
    x a fitted object from either treat.effects or treatment.effects
    digits minimal number of significant digits to print.
    ... further arguments passed to or from print.default.
```

print.subgroup\_fitted Printing results for fitted subgroup identification models

## Description

Prints results for estimated subgroup treatment effects
Prints summary results for estimated subgroup treatment effects

## Usage

```
## S3 method for class 'subgroup_fitted'
print(x, digits = max(getOption("digits") - 3, 3), ...)

## S3 method for class 'subgroup_validated'
print(
    x,
    digits = max(getOption("digits") - 3, 3),
    sample.pct = FALSE,
    which.quant = NULL,
    ...
)

## S3 method for class 'subgroup_summary'
print(x, p.value = 0.001, digits = max(getOption("digits") - 3, 3), ...)
```

#### **Arguments**

a fitted object from either fit.subgroup, validate.subgroup, or summarize.subgroups() Χ digits minimal number of significant digits to print. further arguments passed to or from print.default. sample.pct boolean variable of whether to print the percent of the test sample within each subgroup. If false the sample size itself, not the percent is printed. This may not be informative if the test sample size is much different from the total sample size when validate.subgroup() is called with a vector of quantile values specified which.quant for benefit.score.quantiles, i.e. benefit.score.quantiles = c(0.25,0.5, 0.75), the argument which quant can be a vector of indexes specifying which quantile cutoff value validation results to display, i.e. which quant = c(1,3) in the above example results in the display of validation results for subgroups defined by cutoff values of the benefit score defined by the 25th abnd 75th quantiles of the benefit score

subgroup.effects 29

p.value

a p-value threshold for mean differences below which covariates will be displayed. P-values are adjusted for multiple comparisons by the Hommel approach. For example, setting p.value = 0.05 will display all covariates that have a significant difference between subgroups with p-value less than 0.05. Defaults to 0.001.

#### See Also

validate.subgroup for function which creates validation results and fit.subgroup for function which fits subgroup identification models.

summarize. subgroups for function which summarizes subgroup covariate values

subgroup.effects

Computes treatment effects within various subgroups

## Description

Computes treatment effects within various subgroups to estimate subgroup treatment effects

## Usage

```
subgroup.effects(
  benefit.scores,
  y,
  trt,
  pi.x,
  cutpoint = 0,
  larger.outcome.better = TRUE,
  reference.trt = NULL
)
```

#### Arguments

benefit.scores vector of estimated benefit scores

y The response vector

trt treatment vector with each element equal to a 0 or a 1, with 1 indicating treat-

ment status is active.

pi.x The propensity score for each observation

cutpoint numeric value for patients with benefit scores above which (or below which if

larger.outcome.better = FALSE) will be recommended to be in the treatment group. Can also set cutpoint = "median", which will use the median value of the benefit scores as the cutpoint or can set specific quantile values via "quantx" where "x" is a number between 0 and 100 representing the quantile value; e.g. cutpoint = "quant75" will use the 75th perent upper quantile of the benefit

scores as the quantile.

30 summarize.subgroups

larger.outcome.better

boolean value of whether a larger outcome is better. Set to TRUE if a larger outcome is better and set to FALSE if a smaller outcome is better. Defaults to TRUE.

reference.trt

index of which treatment is the reference (in the case of multiple treatments). This should be known already, as for a trt with K-levels, there will be K-1 benefit scores (1 per column) of benefit.scores, where each column is a comparison of each K-1 treatments with the reference treatment. The default is the last level of trt if it is a factor.

#### See Also

fit.subgroup for function which fits subgroup identification models which generate benefit scores.

summarize.subgroups

Summarizing covariates within estimated subgroups

## **Description**

Summarizes covariate values within the estimated subgroups

# Usage

```
summarize.subgroups(x, ...)
## Default S3 method:
summarize.subgroups(x, subgroup, ...)
## S3 method for class 'subgroup_fitted'
summarize.subgroups(x, ...)
```

#### **Arguments**

x a fitted object from fit.subgroup() or a matrix of covariate values

... optional arguments to summarize. subgroups methods

subgroup

vector of indicators of same length as the number of rows in x if x is a matrix. A value of 1 in the ith position of subgroup indicates patient i is in the subgroup of patients recommended the treatment and a value of 0 in the ith position of subgroup indicates patient i is in the subgroup of patients recommended the control. If x is a fitted object returned by fit.subgroup(), subgroup is not needed.

# Details

The p-values shown are raw p-values and are not adjusted for multiple comparisons.

summarize.subgroups 31

## See Also

fit.subgroup for function which fits subgroup identification models and print.subgroup\_summary for arguments for printing options for summarize.subgroups().

```
library(personalized)
set.seed(123)
n.obs <- 1000
n.vars <- 50
x <- matrix(rnorm(n.obs * n.vars, sd = 3), n.obs, n.vars)</pre>
# simulate non-randomized treatment
xbetat <-0.5 + 0.5 * x[,21] - 0.5 * x[,41]
trt.prob <- exp(xbetat) / (1 + exp(xbetat))</pre>
        <- rbinom(n.obs, 1, prob = trt.prob)
trt
         <- 2 * trt01 - 1
# simulate response
delta <- 2 * (0.5 + x[,2] - x[,3] - x[,11] + x[,1] * x[,12])
xbeta \leftarrow x[,1] + x[,11] - 2 * x[,12]^2 + x[,13]
xbeta <- xbeta + delta * trt
# continuous outcomes
y \leftarrow drop(xbeta) + rnorm(n.obs, sd = 2)
# create function for fitting propensity score model
prop.func <- function(x, trt)</pre>
    # fit propensity score model
    propens.model <- cv.glmnet(y = trt,</pre>
                                x = x, family = "binomial")
    pi.x <- predict(propens.model, s = "lambda.min",</pre>
                    newx = x, type = "response")[,1]
    pi.x
}
subgrp.model \leftarrow fit.subgroup(x = x, y = y,
                              trt = trt01,
                              propensity.func = prop.func,
                              loss = "sq_loss_lasso",
                              nfolds = 5)
                                            # option for cv.glmnet
comp <- summarize.subgroups(subgrp.model)</pre>
print(comp, p.value = 0.01)
# or we can simply supply the matrix x and the subgroups
comp2 <- summarize.subgroups(x, subgroup = 1 * (subgrp.model$benefit.scores > 0))
```

32 treatment.effects

```
print(comp2, p.value = 0.01)
```

```
summary.subgroup_fitted
```

Summary of results for fitted subgroup identification models

## **Description**

Prints summary of results for estimated subgroup treatment effects

Prints summary of results for estimated weighted ksvm

## Usage

```
## S3 method for class 'subgroup_fitted'
summary(object, digits = max(getOption("digits") - 3, 3), ...)
## S3 method for class 'wksvm'
summary(object, digits = max(getOption("digits") - 3, 3), ...)
```

## Arguments

```
object a fitted object from either fit.subgroup or validate.subgroup digits minimal number of significant digits to print.
... further arguments passed to or from print.default.
```

#### See Also

validate.subgroup for function which creates validation results and fit.subgroup for function which fits subgroup identification models.

treatment.effects

Calculation of covariate-conditional treatment effects

#### **Description**

Calculates covariate conditional treatment effects using estimated benefit scores

treatment.effects 33

#### Usage

```
treatment.effects(x, ...)
## Default S3 method:
treatment.effects(x, ...)
treat.effects(
 benefit.scores,
 loss = c("sq_loss_lasso", "logistic_loss_lasso", "poisson_loss_lasso",
   "cox_loss_lasso", "owl_logistic_loss_lasso", "owl_logistic_flip_loss_lasso",
    "owl_hinge_loss", "owl_hinge_flip_loss", "sq_loss_lasso_gam",
    "poisson_loss_lasso_gam", "logistic_loss_lasso_gam", "sq_loss_gam",
    "poisson_loss_gam", "logistic_loss_gam", "owl_logistic_loss_gam",
    "owl_logistic_flip_loss_gam", "owl_logistic_loss_lasso_gam",
    "owl_logistic_flip_loss_lasso_gam", "sq_loss_xgboost", "custom"),
 method = c("weighting", "a_learning"),
 pi.x = NULL,
)
## S3 method for class 'subgroup_fitted'
treatment.effects(x, ...)
```

#### **Arguments**

X	a fitted object from fit.subgroup()
	not used
benefit.scores	vector of estimated benefit scores
loss	loss choice USED TO CALCULATE benefit.scores of both the M function from Chen, et al (2017) and potentially the penalty used for variable selection. See fit.subgroup for more details.
method	method choice USED TO CALCULATE benefit.scores. Either the "weighting" method or "a_learning" method. See fit.subgroup for more details
pi.x	The propensity score for each observation

# Value

```
A List with elements delta (if the treatment effects are a difference/contrast, i.e. E[Y|T=1,X]-E[Y|T=-1,X]) and gamma (if the treatment effects are a ratio, i.e. E[Y|T=1,X]/E[Y|T=-1,X])
```

#### See Also

fit. subgroup for function which fits subgroup identification models.

print.individual\_treatment\_effects for printing of objects returned by treat.effects or treatment.effects 34 treatment.effects

```
library(personalized)
set.seed(123)
n.obs <- 500
n.vars <- 25
x \leftarrow matrix(rnorm(n.obs * n.vars, sd = 3), n.obs, n.vars)
# simulate non-randomized treatment
xbetat <-0.5 + 0.5 * x[,21] - 0.5 * x[,11]
trt.prob <- exp(xbetat) / (1 + exp(xbetat))</pre>
trt01 <- rbinom(n.obs, 1, prob = trt.prob)</pre>
         <- 2 * trt01 - 1
trt
# simulate response
delta <- 2 * (0.5 + x[,2] - x[,3] - x[,11] + x[,1] * x[,12])
xbeta \leftarrow x[,1] + x[,11] - 2 * x[,12]^2 + x[,13]
xbeta <- xbeta + delta * trt
# continuous outcomes
y \leftarrow drop(xbeta) + rnorm(n.obs, sd = 2)
# time-to-event outcomes
surv.time \leftarrow \exp(-20 - xbeta + rnorm(n.obs, sd = 1))
cens.time <- exp(rnorm(n.obs, sd = 3))
y.time.to.event <- pmin(surv.time, cens.time)</pre>
                  <- 1 * (surv.time <= cens.time)
status
# create function for fitting propensity score model
prop.func <- function(x, trt)</pre>
{
    # fit propensity score model
    propens.model <- cv.glmnet(y = trt,</pre>
                                x = x, family = "binomial")
    pi.x <- predict(propens.model, s = "lambda.min",</pre>
                    newx = x, type = "response")[,1]
    pi.x
}
subgrp.model \leftarrow fit.subgroup(x = x, y = y,
                              trt = trt01,
                               propensity.func = prop.func,
                               loss = "sq_loss_lasso",
                               nfolds = 3) # option for cv.glmnet
trt_eff <- treatment.effects(subgrp.model)</pre>
str(trt_eff)
trt_eff
```

validate.subgroup

Validating fitted subgroup identification models

#### Description

Validates subgroup treatment effects for fitted subgroup identification model class of Chen, et al (2017)

## Usage

```
validate.subgroup(
  model,
  B = 50L,
  method = c("training_test_replication", "boot_bias_correction"),
  train.fraction = 0.75,
  benefit.score.quantiles = c(0.1666667, 0.3333333, 0.5, 0.6666667, 0.8333333),
  parallel = FALSE
)
```

## **Arguments**

model fitted model object returned by fit.subgroup() function

B integer. number of bootstrap replications or refitting replications.

method validation method. "boot\_bias\_correction" for the bootstrap bias correction

method of Harrell, et al (1996) or "training\_test\_replication" for repeated training and test splitting of the data (train.fraction should be specified for

this option)

 $train.fraction \ \ fraction \ \ (between \ 0 \ and \ 1) \ of \ samples \ to \ be \ used \ for \ training \ in \ training/test$ 

replication. Only used for method = "training\_test\_replication"

benefit.score.quantiles

a vector of quantiles (between 0 and 1) of the benefit score values for which to return bootstrapped information about the subgroups. ie if one of the quantile values is 0.5, the median value of the benefit scores will be used as a cutoff to

determine subgroups and summary statistics will be returned about these subgroups

parallel

Should the loop over replications be parallelized? If FALSE, then no, if TRUE, then yes. If user sets parallel = TRUE and the fitted fit.subgroup() object uses the parallel version of an internal model, say for cv.glmnet(), then the internal parallelization will be overridden so as not to create a conflict of parallelism

#### **Details**

Estimates of various quantities conditional on subgroups and treatment statuses are provided and displayed via the print.subgroup\_validated function:

- "Conditional expected outcomes" The first results shown when printing a subgroup\_validated object are estimates of the expected outcomes conditional on the estimated subgroups (i.e. which subgroup is 'recommended' by the model) and conditional on treatment/intervention status. If there are two total treatment options, this results in a 2x2 table of expected conditional outcomes.
- 2. "Treatment effects conditional on subgroups" The second results shown when printing a subgroup\_validated object are estimates of the expected outcomes conditional on the estimated subgroups. If the treatment takes levels  $j \in \{1, \ldots, K\}$ , a total of K conditional treatment effects will be shown. For example, of the outcome is continuous, the jth conditional treatment effect is defined as E(Y|Trt=j,Subgroup=j)-E(Y|Trt=j,Subgroup=j), where Subgroup=j if treatment j is recommended, i.e. treatment j results in the largest/best expected potential outcomes given the fitted model.
- 3. "Overall treatment effect conditional on subgroups" The third quantity displayed shows the overall improvement in outcomes resulting from all treatment recommendations. This is essentially an average over all of the conditional treatment effects weighted by the proportion of the population recommended each respective treatment level.

#### Value

An object of class "subgroup\_validated"

avg.results

Estimates of average conditional treatment effects when subgroups are determined based on the provided cutoff value for the benefit score. For example, if  $cutoff = \emptyset$  and there is a treatment and control only, then the treatment is recommended if the benefit score is greater than 0.

se.results

Standard errors of the estimates from avg.estimates

boot.results

Contains the individual results for each replication. avg.results is comprised of averages of the values from boot.results

avg.quantile.results

Estimates of average conditional treatment effects when subgroups are determined based on different quntile cutoff values for the benefit score. For example, if benefit.score.quantiles = 0.75 and there is a treatment and control only, then the treatment is recommended if the benefit score is greater than the 75th upper quantile of all benefit scores. If multiple quantile values are provided, e.g. benefit.score.quantiles = c(0.15, 0.5, 0.85), then results will be provided for all quantile levels.

se.quantile.results

Standard errors corresponding to avg.quantile.results

boot.results.quantiles

Contains the individual results for each replication. avg.quantile.results is

comprised of averages of the values from boot.results.quantiles

family Family of the outcome. For example, "gaussian" for continuous outcomes method Method used for subgroup identification model. Weighting or A-learning

We find a sea for subgroup rachimeteror model. We griding of 11 reals

n.trts The number of treatment levels

comparison.trts

All treatment levels other than the reference level

reference.trt The reference level for the treatment. This should usually be the control group/level

larger.outcome.better

If larger outcomes are preferred for this model

cutpoint Benefit score cutoff value used for determining subgroups

val.method Method used for validation

iterations Number of replications used in the validation process

Number of observations in x provided to fit.subgroup

Number of variables in x provided to fit.subgroup

#### References

Chen, S., Tian, L., Cai, T. and Yu, M. (2017), A general statistical framework for subgroup identification and comparative treatment scoring. Biometrics. doi:10.1111/biom.12676

Harrell, F. E., Lee, K. L., and Mark, D. B. (1996). Tutorial in biostatistics multivariable prognostic models: issues in developing models, evaluating assumptions and adequacy, and measuring and reducing errors. Statistics in medicine, 15, 361-387. doi:10.1002/(SICI)1097-0258(19960229)15:4<361::AID-SIM168>3.0.CO;2-4

Huling. J.D. and Yu, M. (2021), Subgroup Identification Using the personalized Package. Journal of Statistical Software 98(5), 1-60. doi:10.18637/jss.v098.i05

### See Also

fit.subgroup for function which fits subgroup identification models, plot.subgroup\_validated for plotting of validation results, and print.subgroup\_validated for arguments for printing options for validate.subgroup().

```
library(personalized)
set.seed(123)
n.obs <- 500
n.vars <- 20
x <- matrix(rnorm(n.obs * n.vars, sd = 3), n.obs, n.vars)</pre>
```

```
# simulate non-randomized treatment
xbetat <-0.5 + 0.5 * x[,11] - 0.5 * x[,13]
trt.prob <- exp(xbetat) / (1 + exp(xbetat))</pre>
        <- rbinom(n.obs, 1, prob = trt.prob)
trt
         <- 2 * trt01 - 1
# simulate response
delta <- 2 * (0.5 + x[,2] - x[,3] - x[,11] + x[,1] * x[,12])
xbeta \leftarrow x[,1] + x[,11] - 2 * x[,12]^2 + x[,13]
xbeta <- xbeta + delta * trt
# continuous outcomes
y \leftarrow drop(xbeta) + rnorm(n.obs, sd = 2)
# create function for fitting propensity score model
prop.func <- function(x, trt)</pre>
{
    # fit propensity score model
    propens.model <- cv.glmnet(y = trt,</pre>
                                x = x, family = "binomial")
    pi.x <- predict(propens.model, s = "lambda.min",</pre>
                    newx = x, type = "response")[,1]
    pi.x
}
subgrp.model \leftarrow fit.subgroup(x = x, y = y,
                              trt = trt01,
                              propensity.func = prop.func,
                              loss = "sq_loss_lasso",
                              # option for cv.glmnet,
                              # better to use 'nfolds=10'
                              nfolds = 3)
x.test \leftarrow matrix(rnorm(10 * n.obs * n.vars, sd = 3), 10 * n.obs, n.vars)
# simulate non-randomized treatment
xbetat.test <- 0.5 + 0.5 * x.test[,11] - 0.5 * x.test[,13]
trt.prob.test <- exp(xbetat.test) / (1 + exp(xbetat.test))</pre>
trt01.test <- rbinom(10 * n.obs, 1, prob = trt.prob.test)</pre>
              <- 2 * trt01.test - 1
trt.test
# simulate response
delta.test <- 2 * (0.5 + x.test[,2] - x.test[,3] - x.test[,11] + x.test[,1] * x.test[,12])
xbeta.test <- x.test[,1] + x.test[,11] - 2 * x.test[,12]^2 + x.test[,13]
xbeta.test <- xbeta.test + delta.test * trt.test</pre>
y.test <- drop(xbeta.test) + rnorm(10 * n.obs, sd = 2)
valmod <- validate.subgroup(subgrp.model, B = 2,</pre>
```

weighted.ksvm 39

weighted.ksvm

Fit weighted kernel svm model.

# Description

Fits weighted kernel SVM. To be used for OWL with hinge loss (but can be used more generally)

# Usage

```
weighted.ksvm(
   y,
   x,
   weights,
   C = c(0.1, 0.5, 1, 2, 10),
   kernel = "rbfdot",
   kpar = "automatic",
   nfolds = 10,
   foldid = NULL,
   eps = 1e-08,
   ...
)
```

# Arguments

У	The response vector (either a character vector, factor vector, or numeric vector with values in -1, 1)
x	The design matrix (not including intercept term)
weights	vector of sample weights for weighted SVM
С	cost of constraints violation, see ksvm
kernel	kernel function used for training and prediction. See ksvm and kernels
kpar	list of hyperparameters for the kernel function. See ksvm
nfolds	number of cross validation folds for selecting value of C
foldid	optional vector of values between 1 and nfolds specifying which fold each observation is in. If specified, it will override the nfolds argument.
eps	penalty nugget parameter. Defaults to 1e-8
	extra arguments to be passed to ipop from the kernlab package

40 weighted.ksvm

## See Also

predict.wksvm for predicting from fitted weighted.ksvm objects

# **Index**

```
* datasets
                                                summarize.subgroups, 29, 30
    LaLonde, 19
                                                 summary.subgroup_fitted, 32
                                                 summary.wksvm
check.overlap, 2
                                                         (summary.subgroup_fitted), 32
create.augmentation.function,4
create.propensity.function, 5, 6, 7
                                                 treat.effects, 14, 28
                                                treat.effects (treatment.effects), 32
cv.glmnet, 5, 7, 13
                                                 treatment.effects, 28, 32
fit.subgroup, 5, 7, 8, 22, 24, 26, 29–33, 37
                                                validate.subgroup, 15, 22, 24, 29, 32, 35
gam, 14
                                                weighted.ksvm, 14, 26, 39
glmnet, 5, 7
                                                xgb.train, 9
ipop, 14, 39
kernels, 39
ksvm, 39
LaLonde, 19
plot.subgroup_fitted, 15, 21
plot.subgroup_validated, 37
plot.subgroup_validated
        (plot.subgroup_fitted), 21
plotCompare, 23
predict.subgroup_fitted, 15, 25
predict.wksvm, 40
predict.wksvm
        (predict.subgroup_fitted), 25
print.default, 28, 32
print.individual_treatment_effects, 27,
        33
print.subgroup_fitted, 15, 28
print.subgroup_summary, 31
print.subgroup_summary
        (print.subgroup_fitted), 28
print.subgroup_validated, 36, 37
print.subgroup_validated
        (print.subgroup_fitted), 28
subgroup.effects, 29
```