# Package 'rnnmf'

July 23, 2025

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Version 0.3.0

Date 2024-10-30

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Title Regularized Non-Negative Matrix Factorization

#### BugReports https://github.com/shabbychef/rnnmf/issues

#### Description

A proof of concept implementation of regularized non-negative matrix factorization optimization. A non-negative matrix factorization factors nonnegative matrix Y approximately as L R, for non-negative matrices L and R of reduced rank. This package supports such factorizations with weighted objective and regularization penalties. Allowable regularization penalties include L1 and L2 penalties on L and R, as well as nonorthogonality penalties. This package provides multiplicative update algorithms, which are a modification of the algorithm of Lee and Seung (2001) <http://papers.nips.cc/paper/ 1861-algorithms-for-non-negative-matrix-factorization.pdf>, as well as an additive update derived from that multiplicative update. See also Pay (2004) <doi:10.48550/arXiv.2410.22698>.

#### **Depends** R (>= 3.0.2)

#### **Imports** Matrix

Suggests testthat, dplyr, ggplot2, scales, viridis, knitr

#### URL https://github.com/shabbychef/rnnmf

#### VignetteBuilder knitr

Collate 'aurnmf.r' 'gaurnmf.r' 'giqpm.r' 'murnmf.r' 'rnnmf-package.r'

RoxygenNote 7.3.2

NeedsCompilation no

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#### aurnmf

Repository CRAN Date/Publication 2024-11-04 10:40:02 UTC

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nmf.

# Description

Additive update Non-negative matrix factorization with regularization.

# Usage

```
aurnmf(
 Υ,
 L,
 R,
 W_{OR} = NULL,
 W_{OC} = NULL,
 lambda_1L = 0,
 lambda_1R = 0,
 lambda_2L = 0,
 lambda_2R = 0,
 gamma_{2L} = 0,
  gamma_2R = 0,
  tau = 0.1,
  annealing_rate = 0.01,
  check_optimal_step = TRUE,
  zero_tolerance = 1e-12,
 max_iterations = 1000L,
 min_xstep = 1e-09,
 on_iteration_end = NULL,
  verbosity = 0
)
```

# aurnmf

# Arguments

Y	an $r \times c$ matrix to be decomposed. Should have non-negative elements; an error is thrown otherwise.
L	an $r \times d$ matrix of the initial estimate of L. Should have non-negative elements; an error is thrown otherwise.
R	an $d \times c$ matrix of the initial estimate of R. Should have non-negative elements; an error is thrown otherwise.
W_0R	the row space weighting matrix. This should be a positive definite non-negative symmetric $r \times r$ matrix. If omitted, it defaults to the properly sized identity matrix.
W_0C	the column space weighting matrix. This should be a positive definite non- negative symmetric $c \times c$ matrix. If omitted, it defaults to the properly sized identity matrix.
lambda_1L	the scalar $\ell_1$ penalty for the matrix L. Defaults to zero.
lambda_1R	the scalar $\ell_1$ penalty for the matrix R. Defaults to zero.
lambda_2L	the scalar $\ell_2$ penalty for the matrix L. Defaults to zero.
lambda_2R	the scalar $\ell_2$ penalty for the matrix R. Defaults to zero.
gamma_2L	the scalar $\ell_2$ penalty for non-orthogonality of the matrix L. Defaults to zero.
gamma_2R	the scalar $\ell_2$ penalty for non-orthogonality of the matrix R. Defaults to zero.
tau	the starting shrinkage factor applied to the step length. Should be a value in $(0,1)$ .
annealing_rate	the rate at which we scale the shrinkage factor towards 1. Should be a value in $[0, 1)$ .
check_optimal_s	tep
	if TRUE, we attempt to take the optimal step length in the given direction. If not, we merely take the longest feasible step in the step direction.
zero_tolerance	values of $x$ less than this will be 'snapped' to zero. This happens at the end of the iteration and does not affect the measurement of convergence.
<pre>max_iterations</pre>	the maximum number of iterations to perform.
min_xstep	the minimum L-infinity norm of the step taken. Once the step falls under this value, we terminate.
on_iteration_er	nd
	an optional function that is called at the end of each iteration. The function is called as on_iteration_end(iteration=iteration, Y=Y, L=L, R=R, Lstep=Lstep, Rstep=Rstep,)
verbosity	controls whether we print information to the console.

# Details

Attempts to factor given non-negative matrix Y as the product LR of two non-negative matrices. The objective function is Frobenius norm with  $\ell_1$  and  $\ell_2$  regularization terms. We seek to minimize the objective

$$\frac{1}{2}tr((Y-LR)'W_{0R}(Y-LR)W_{0C}) + \lambda_{1L}|L| + \lambda_{1R}|R| + \frac{\lambda_{2L}}{2}tr(L'L) + \frac{\lambda_{2R}}{2}tr(R'R) + \frac{\gamma_{2L}}{2}tr((L'L)(11'-I)) + \frac{\gamma_{2R}}{2}tr((R'R) + \frac{\lambda_{2R}}{2}tr((R'R) + \frac{\lambda_{2R}}{2}tr((R'R)$$

subject to  $L \ge 0$  and  $R \ge 0$  elementwise, where |A| is the sum of the elements of A and tr(A) is the trace of A.

The code starts from initial estimates and iteratively improves them, maintaining non-negativity. This implementation uses the Lee and Seung step direction, with a correction to avoid divide-by-zero. The iterative step is optionally re-scaled to take the steepest descent in the step direction.

# Value

a list with the elements

L The final estimate of L.

**R** The final estimate of R.

Lstep The infinity norm of the final step in L.

**Rstep** The infinity norm of the final step in R.

iterations The number of iterations taken.

converged Whether convergence was detected.

#### Note

This package provides proof of concept code which is unlikely to be fast or robust, and may not solve the optimization problem at hand. User assumes all risk.

#### Author(s)

Steven E. Pav <shabbychef@gmail.com>

#### References

Merritt, Michael, and Zhang, Yin. "Interior-point Gradient Method for Large-Scale Totally Nonnegative Least Squares Problems." Journal of Optimization Theory and Applications 126, no 1 (2005): 191–202. https://scholarship.rice.edu/bitstream/handle/1911/102020/TR04-08.pdf

Pav, S. E. "An Iterative Algorithm for Regularized Non-negative Matrix Factorizations." Forthcoming. (2024)

Lee, Daniel D. and Seung, H. Sebastian. "Algorithms for Non-negative Matrix Factorization." Advances in Neural Information Processing Systems 13 (2001): 556–562. http://papers.nips. cc/paper/1861-algorithms-for-non-negative-matrix-factorization.pdf

#### See Also

gaurnmf, murnmf.

# Examples

nr <- 100 nc <- 20 dm <- 4

randmat <- function(nr,nc,...) { matrix(pmax(0,runif(nr\*nc,...)),nrow=nr) }</pre>

#### gaurnmf

```
set.seed(1234)
 real_L <- randmat(nr,dm)</pre>
real_R <- randmat(dm,nc)</pre>
Y <- real_L %*% real_R
# without regularization
 objective <- function(Y, L, R) { sum((Y - L %*% R)^2) }</pre>
 objective(Y,real_L,real_R)
L_0 <- randmat(nr,dm)</pre>
R_0 <- randmat(dm,nc)</pre>
 objective(Y,L_0,R_0)
out1 <- aurnmf(Y, L_0, R_0, max_iterations=5e3L, check_optimal_step=FALSE)</pre>
objective(Y,out1$L,out1$R)
# with L1 regularization on one side
out2 <- aurnmf(Y, L_0, R_0, lambda_1L=0.1, max_iterations=5e3L,check_optimal_step=FALSE)</pre>
# objective does not suffer because all mass is shifted to R
objective(Y,out2$L,out2$R)
list(L1=sum(out1$L),R1=sum(out1$R),L2=sum(out2$L),R2=sum(out2$R))
sum(out2$L)
# with L1 regularization on both sides
out3 <- aurnmf(Y, L_0, R_0, lambda_1L=0.1,lambda_1R=0.1,</pre>
     max_iterations=5e3L, check_optimal_step=FALSE)
# with L1 regularization on both sides, raw objective suffers
objective(Y,out3$L,out3$R)
list(L1=sum(out1$L),R1=sum(out1$R),L3=sum(out3$L),R3=sum(out3$R))
# example showing how to use the on_iteration_end callback to save iterates.
max_iterations <- 5e3L</pre>
it_history <<- rep(NA_real_, max_iterations)</pre>
quadratic_objective <- function(Y, L, R) { sum((Y - L %*% R)^2) }</pre>
on_iteration_end <- function(iteration, Y, L, R, ...) {</pre>
 it_history[iteration] <<- quadratic_objective(Y,L,R)</pre>
}
out1b <- aurnmf(Y, L_0, R_0, max_iterations=max_iterations, on_iteration_end=on_iteration_end)
# should work on sparse matrices too.
```

```
if (require(Matrix)) {
  real_L <- randmat(nr,dm,min=-1)
  real_R <- randmat(dm,nc,min=-1)
  Y <- as(real_L %*% real_R, "sparseMatrix")
  L_0 <- as(randmat(nr,dm,min=-0.5), "sparseMatrix")
  R_0 <- as(randmat(dm,nc,min=-0.5), "sparseMatrix")
  out1 <- aurnmf(Y, L_0, R_0, max_iterations=1e2L,check_optimal_step=TRUE)
}</pre>
```

gaurnmf

# Description

Additive update Non-negative matrix factorization with regularization, general form.

# Usage

```
gaurnmf(
 Υ,
 L,
 R,
 W_{OR} = NULL,
 W_{OC} = NULL,
 W_{1L} = 0,
 W_{1R} = 0,
 W_2RL = 0,
 W_{2CL} = 0,
 W_2RR = 0,
 W_2CR = 0,
  tau = 0.1,
  annealing_rate = 0.01,
 check_optimal_step = TRUE,
  zero_tolerance = 1e-12,
 max_iterations = 1000L,
 min_xstep = 1e-09,
 on_iteration_end = NULL,
  verbosity = 0
```

# Arguments

)

Y	an $r \times c$ matrix to be decomposed. Should have non-negative elements; an error is thrown otherwise.
L	an $r \times d$ matrix of the initial estimate of L. Should have non-negative elements; an error is thrown otherwise.
R	an $d\times c$ matrix of the initial estimate of R. Should have non-negative elements; an error is thrown otherwise.
W_0R	the row space weighting matrix. This should be a positive definite non-negative symmetric $r \times r$ matrix. If omitted, it defaults to the properly sized identity matrix.
W_0C	the column space weighting matrix. This should be a positive definite non-negative symmetric $c \times c$ matrix. If omitted, it defaults to the properly sized identity matrix.
W_1L	the $\ell_1$ penalty matrix for the matrix $R$ . If a scalar, corresponds to that scalar times the all-ones matrix. Defaults to all-zeroes matrix, which is no penalty term.
W_1R	the $\ell_1$ penalty matrix for the matrix <i>L</i> . If a scalar, corresponds to that scalar times the all-ones matrix. Defaults to all-zeroes matrix, which is no penalty term.

# gaurnmf

W_2RL	the $\ell_2$ row penalty matrix for the matrix L. If a scalar, corresponds to that scalar times the identity matrix. Can also be a list, in which case W_2CL must be a list of the same length. The list should consist of $\ell_2$ row penalty matrices. Defaults to all-zeroes matrix, which is no penalty term.
W_2CL	the $\ell_2$ column penalty matrix for the matrix $L$ . If a scalar, corresponds to that scalar times the identity matrix. Can also be a list, in which case W_2RL must be a list of the same length. The list should consist of $\ell_2$ column penalty matrices. Defaults to all-zeroes matrix, which is no penalty term.
W_2RR	the $\ell_2$ row penalty matrix for the matrix $R$ . If a scalar, corresponds to that scalar times the identity matrix. Can also be a list, in which case W_2CR must be a list of the same length. The list should consist of $\ell_2$ row penalty matrices. Defaults to all-zeroes matrix, which is no penalty term.
W_2CR	the $\ell_2$ column penalty matrix for the matrix $R$ . If a scalar, corresponds to that scalar times the identity matrix. Can also be a list, in which case W_2RR must be a list of the same length. The list should consist of $\ell_2$ column penalty matrices. Defaults to all-zeroes matrix, which is no penalty term.
tau	the starting shrinkage factor applied to the step length. Should be a value in $(0,1)$ .
annealing_rate	the rate at which we scale the shrinkage factor towards 1. Should be a value in $[0, 1)$ .
check_optimal_s	itep
	if TRUE, we attempt to take the optimal step length in the given direction. If not, we merely take the longest feasible step in the step direction.
zero_tolerance	values of $x$ less than this will be 'snapped' to zero. This happens at the end of the iteration and does not affect the measurement of convergence.
<pre>max_iterations</pre>	the maximum number of iterations to perform.
<pre>min_xstep</pre>	the minimum L-infinity norm of the step taken. Once the step falls under this value, we terminate.
on_iteration_er	nd
	an optional function that is called at the end of each iteration. The function is called as on_iteration_end(iteration=iteration, Y=Y, L=L, R=R, Lstep=Lstep, Rstep=Rstep,)
verbosity	controls whether we print information to the console.

#### Details

Attempts to factor given non-negative matrix Y as the product LR of two non-negative matrices. The objective function is Frobenius norm with  $\ell_1$  and  $\ell_2$  regularization terms. We seek to minimize the objective

$$\frac{1}{2}tr((Y-LR)'W_{0R}(Y-LR)W_{0C}) + tr(W_{1L}'L) + tr(W_{1R}'R) + \frac{1}{2}\sum_{j}tr(L'W_{2RLj}LW_{2CLj}) + tr(R'W_{2RRj}RW_{2CRj}) + tr(W_{1L}'L) + tr(W_{1R}'R) + \frac{1}{2}\sum_{j}tr(L'W_{2RLj}LW_{2CLj}) + tr(R'W_{2RRj}RW_{2CRj}) + tr(R'W_{2RRj}RW_{2CRj}RW_{2CRj}) + tr(R'W_{2RRj}RW_{2CRj}RW_{2CRj}RW_{2CRj}RW_{2CRj}) + tr(R'W_{2RRj}RW_{2CRj$$

subject to  $L \ge 0$  and  $R \ge 0$  elementwise, where tr(A) is the trace of A.

The code starts from initial estimates and iteratively improves them, maintaining non-negativity. This implementation uses the Lee and Seung step direction, with a correction to avoid divide-by-zero. The iterative step is optionally re-scaled to take the steepest descent in the step direction.

#### gaurnmf

#### Value

a list with the elements

L The final estimate of L.

**R** The final estimate of R.

Lstep The infinity norm of the final step in L.

**Rstep** The infinity norm of the final step in R.

iterations The number of iterations taken.

converged Whether convergence was detected.

#### Note

This package provides proof of concept code which is unlikely to be fast or robust, and may not solve the optimization problem at hand. User assumes all risk.

#### Author(s)

Steven E. Pav <shabbychef@gmail.com>

#### References

Merritt, Michael, and Zhang, Yin. "Interior-point Gradient Method for Large-Scale Totally Nonnegative Least Squares Problems." Journal of Optimization Theory and Applications 126, no 1 (2005): 191–202. https://scholarship.rice.edu/bitstream/handle/1911/102020/TR04-08.pdf

Pav, S. E. "An Iterative Algorithm for Regularized Non-negative Matrix Factorizations." Forthcoming. (2024)

Lee, Daniel D. and Seung, H. Sebastian. "Algorithms for Non-negative Matrix Factorization." Advances in Neural Information Processing Systems 13 (2001): 556–562. http://papers.nips.cc/paper/1861-algorithms-for-non-negative-matrix-factorization.pdf

#### See Also

aurnmf

#### Examples

```
nr <- 20
nc <- 5
dm <- 2
randmat <- function(nr,nc,...) { matrix(pmax(0,runif(nr*nc,...)),nrow=nr) }
set.seed(1234)
real_L <- randmat(nr,dm+2)
real_R <- randmat(ncol(real_L),nc)
Y <- real_L %*% real_R
gram_it <- function(G) { t(G) %*% G }
W_0R <- gram_it(randmat(nr+5,nr))
W_0C <- gram_it(randmat(nc+5,nc))</pre>
```

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#### giqpm

```
wt_objective <- function(Y, L, R, W_0R, W_0C) {</pre>
   err <- Y - L %*% R
   0.5 * sum((err %*% W_0C) * (t(W_0R) %*% err))
 }
 matrix_trace <- function(G) {</pre>
   sum(diag(G))
 }
wt_objective(Y,real_L,real_R,W_0R,W_0C)
L_0 <- randmat(nr,dm)</pre>
R_0 <- randmat(dm,nc)</pre>
 wt_objective(Y,L_0,R_0,W_0R,W_0C)
 out1 <- gaurnmf(Y, L_0, R_0, W_0R=W_0R, W_0C=W_0C,</pre>
         max_iterations=1e4L,check_optimal_step=FALSE)
 wt_objective(Y,out1$L,out1$R,W_0R,W_0C)
W_1L <- randmat(nr,dm)</pre>
 out2 <- gaurnmf(Y, out1$L, out1$R, W_0R=W_0R, W_0C=W_0C, W_1L=W_1L,</pre>
         max_iterations=1e4L,check_optimal_step=FALSE)
 wt_objective(Y,out2$L,out2$R,W_0R,W_0C)
W_1R <- randmat(dm,nc)</pre>
 out3 <- gaurnmf(Y, out2$L, out2$R, W_0R=W_0R, W_0C=W_0C, W_1R=W_1R,</pre>
         max_iterations=1e4L, check_optimal_step=FALSE)
 wt_objective(Y,out3$L,out3$R,W_0R,W_0C)
# example showing how to use the on_iteration_end callback to save iterates.
max_iterations <- 1e3L</pre>
 it_history <<- rep(NA_real_, max_iterations)</pre>
 on_iteration_end <- function(iteration, Y, L, R, ...) {</pre>
   it_history[iteration] <<- wt_objective(Y,L,R,W_0R,W_0C)</pre>
 }
out1b <- gaurnmf(Y, L_0, R_0, W_0R=W_0R, W_0C=W_0C,</pre>
 max_iterations=max_iterations, on_iteration_end=on_iteration_end, check_optimal_step=FALSE)
# should work on sparse matrices too.
if (require(Matrix)) {
real_L <- randmat(nr,dm,min=-1)</pre>
real_R <- randmat(dm,nc,min=-1)</pre>
Y <- as(real_L %*% real_R, "sparseMatrix")</pre>
L_0 <- as(randmat(nr,dm,min=-0.5), "sparseMatrix")</pre>
R_0 <- as(randmat(dm,nc,min=-0.5), "sparseMatrix")</pre>
out1 <- gaurnmf(Y, L_0, R_0, max_iterations=1e2L,check_optimal_step=TRUE)</pre>
}
```

giqpm

giqpm .

# Description

Generalized Iterative Quadratic Programming Method for non-negative quadratic optimization.

# Usage

```
giqpm(
Gmat,
dvec,
x0 = NULL,
tau = 0.5,
annealing_rate = 0.25,
check_optimal_step = TRUE,
mult_func = NULL,
grad_func = NULL,
step_func = NULL,
zero_tolerance = 1e-09,
max_iterations = 1000L,
min_xstep = 1e-09,
verbosity = 0
)
```

# Arguments

Gmat	a representation of the matrix G.
dvec	a representation of the vector d.
x0	the initial iterate. If none given, we spawn one of the same size as dvec.
tau	the starting shrinkage factor applied to the step length. Should be a value in $(0,1). \label{eq:constraint}$
annealing_rate	the rate at which we scale the shrinkage factor towards 1. Should be a value in $[0, 1)$ .
check_optimal_s	tep
	if TRUE, we attempt to take the optimal step length in the given direction. If not, we merely take the longest feasible step in the step direction.
mult_func	a function which takes matrix and vector and performs matrix multiplication. The default does this on matrix and vector input, but the user can implement this for some implicit versions of the problem.
grad_func	a function which takes matrix $G$ , vector $d$ , the current iterate $x$ and the product $Gx$ and is supposed to compute $Gx + d$ . The default does this on matrix and vector input, but the user can implement this for some implicit versions of the problem.
step_func	a function which takes the vector gradient, the product $Gx$ , the matrix $G$ , vector $d$ , vector $x$ and the mult_func and produces a step vector. By default this step vector is the Lee-Seung step vector, namely $-(Gx + d) * x/d$ , with Hadamard product and division.
zero_tolerance	values of $x$ less than this will be 'snapped' to zero. This happens at the end of the iteration and does not affect the measurement of convergence.

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#### giqpm

<pre>max_iterations</pre>	the maximum number of iterations to perform.
min_xstep	the minimum L-infinity norm of the step taken. Once the step falls under this value, we terminate.
verbosity	controls whether we print information to the console.

# Details

Iteratively solves the problem

$$\min_{x} \frac{1}{2} x^{\top} G x + d^{\top} x$$

subject to the elementwise constraint  $x \ge 0$ .

This implementation allows the user to specify methods to perform matrix by vector multiplication, computation of the gradient (which should be Gx + d), and computation of the step direction. By default we compute the optimal step in the given step direction.

#### Value

a list with the elements

**x** The final iterate.

iterations The number of iterations taken.

converged Whether convergence was detected.

#### Note

This package provides proof of concept code which is unlikely to be fast or robust, and may not solve the optimization problem at hand. User assumes all risk.

#### Author(s)

Steven E. Pav <shabbychef@gmail.com>

#### References

Pav, S. E. "An Iterative Algorithm for Regularized Non-negative Matrix Factorizations." Forthcoming. (2024)

Merritt, Michael, and Zhang, Yin. "Interior-point Gradient Method for Large-Scale Totally Nonnegative Least Squares Problems." Journal of Optimization Theory and Applications 126, no 1 (2005): 191-202. https://scholarship.rice.edu/bitstream/handle/1911/102020/TR04-08.pdf

#### Examples

```
set.seed(1234)
ssiz <- 100
preG <- matrix(runif(ssiz*(ssiz+20)),nrow=ssiz)</pre>
G <- preG %*% t(preG)</pre>
d <- - runif(ssiz)</pre>
y1 \le giqpm(G, d)
objective <- function(G, d, x) { as.numeric(0.5 * t(x) %*% (G %*% x) + t(x) %*% d) }
```

```
# this does not converge to an actual solution!
steepest_step_func <- function(gradf, ...) { return(-gradf) }
y2 <- giqpm(G, d, step_func = steepest_step_func)
scaled_step_func <- function(gradf, Gx, Gmat, dvec, x0, ...) { return(-gradf * abs(x0)) }
y3 <- giqpm(G, d, step_func = scaled_step_func)
sqrt_step_func <- function(gradf, Gx, Gmat, dvec, x0, ...) { return(-gradf * abs(sqrt(x0))) }
y4 <- giqpm(G, d, step_func = sqrt_step_func)
complementarity_stepfunc <- function(gradf, Gx, Gmat, dvec, x0, ...) { return(-gradf * x0) }
y5 <- giqpm(G, d, step_func = complementarity_stepfunc)
objective(G, d, y1$x)
objective(G, d, y2$x)
objective(G, d, y4$x)
objective(G, d, y5$x)
```

murnmf

murnmf.

#### Description

Multiplicative update Non-negative matrix factorization with regularization.

#### Usage

```
murnmf(
 Υ,
 L,
 R,
 W_{OR} = NULL,
 W_{OC} = NULL,
 lambda_1L = 0,
  lambda_1R = 0,
  lambda_2L = 0,
  lambda_2R = 0,
  gamma_{2L} = 0,
  gamma_2R = 0,
  epsilon = 1e-07,
 max_iterations = 1000L,
 min_xstep = 1e-09,
 on_iteration_end = NULL,
  verbosity = 0
)
```

#### murnmf

#### Arguments

Y	an $r \times c$ matrix to be decomposed. Should have non-negative elements; an error is thrown otherwise.
L	an $r \times d$ matrix of the initial estimate of L. Should have non-negative elements; an error is thrown otherwise.
R	an $d \times c$ matrix of the initial estimate of R. Should have non-negative elements; an error is thrown otherwise.
W_0R	the row space weighting matrix. This should be a positive definite non-negative symmetric $r \times r$ matrix. If omitted, it defaults to the properly sized identity matrix.
W_0C	the column space weighting matrix. This should be a positive definite non- negative symmetric $c \times c$ matrix. If omitted, it defaults to the properly sized identity matrix.
lambda_1L	the scalar $\ell_1$ penalty for the matrix L. Defaults to zero.
lambda_1R	the scalar $\ell_1$ penalty for the matrix R. Defaults to zero.
lambda_2L	the scalar $\ell_2$ penalty for the matrix L. Defaults to zero.
lambda_2R	the scalar $\ell_2$ penalty for the matrix R. Defaults to zero.
gamma_2L	the scalar $\ell_2$ penalty for non-orthogonality of the matrix L. Defaults to zero.
gamma_2R	the scalar $\ell_2$ penalty for non-orthogonality of the matrix R. Defaults to zero.
epsilon	the numerator clipping value.
<pre>max_iterations</pre>	the maximum number of iterations to perform.
min_xstep	the minimum L-infinity norm of the step taken. Once the step falls under this value, we terminate.
on_iteration_en	ıd
	an optional function that is called at the end of each iteration. The function is called as on_iteration_end(iteration=iteration, Y=Y, L=L, R=R, Lstep=Lstep, Rstep=Rstep,)
verbosity	controls whether we print information to the console.

# Details

This function uses multiplicative updates only, and may not optimize the nominal objective. It is also unlikely to achieve optimality. This code is for reference purposes and is not suited for usage other than research and experimentation.

# Value

a list with the elements

L The final estimate of L.

**R** The final estimate of R.

Lstep The infinity norm of the final step in L.

**Rstep** The infinity norm of the final step in R.

iterations The number of iterations taken.

converged Whether convergence was detected.

This package provides proof of concept code which is unlikely to be fast or robust, and may not solve the optimization problem at hand. User assumes all risk.

#### Author(s)

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#### References

Merritt, Michael, and Zhang, Yin. "Interior-point Gradient Method for Large-Scale Totally Nonnegative Least Squares Problems." Journal of Optimization Theory and Applications 126, no 1 (2005): 191–202. https://scholarship.rice.edu/bitstream/handle/1911/102020/TR04-08.pdf

Pav, S. E. "An Iterative Algorithm for Regularized Non-negative Matrix Factorizations." Forthcoming. (2024)

Lee, Daniel D. and Seung, H. Sebastian. "Algorithms for Non-negative Matrix Factorization." Advances in Neural Information Processing Systems 13 (2001): 556–562. http://papers.nips. cc/paper/1861-algorithms-for-non-negative-matrix-factorization.pdf

#### See Also

aurnmf, gaurnmf

#### Examples

```
nr <- 100
nc <- 20
dm <- 4
randmat <- function(nr,nc,...) { matrix(pmax(0,runif(nr*nc,...)),nrow=nr) }</pre>
set.seed(1234)
real_L <- randmat(nr,dm)</pre>
real_R <- randmat(dm,nc)</pre>
Y <- real_L %*% real_R
# without regularization
objective <- function(Y, L, R) { sum((Y - L %*% R)<sup>2</sup>) }
objective(Y,real_L,real_R)
L_0 <- randmat(nr,dm)</pre>
R_0 <- randmat(dm,nc)</pre>
objective(Y,L_0,R_0)
out1 <- murnmf(Y, L_0, R_0, max_iterations=5e3L)</pre>
objective(Y,out1$L,out1$R)
# with L1 regularization on one side
out2 <- murnmf(Y, L_0, R_0, max_iterations=5e3L,lambda_1L=0.1)</pre>
# objective does not suffer because all mass is shifted to R
objective(Y,out2$L,out2$R)
list(L1=sum(out1$L),R1=sum(out1$R),L2=sum(out2$L),R2=sum(out2$R))
sum(out2$L)
# with L1 regularization on both sides
```

#### rnnmf-NEWS

```
out3 <- murnmf(Y, L_0, R_0, max_iterations=5e3L,lambda_1L=0.1,lambda_1R=0.1)
# with L1 regularization on both sides, raw objective suffers
objective(Y,out3$L,out3$R)
list(L1=sum(out1$L),R1=sum(out1$R),L3=sum(out3$L),R3=sum(out3$R))
# example showing how to use the on_iteration_end callback to save iterates.
max_iterations <- 1e3L</pre>
it_history <<- rep(NA_real_, max_iterations)</pre>
quadratic_objective <- function(Y, L, R) { sum((Y - L %*% R)^2) }</pre>
on_iteration_end <- function(iteration, Y, L, R, ...) {</pre>
  it_history[iteration] <<- quadratic_objective(Y,L,R)</pre>
}
out1b <- murnmf(Y, L_0, R_0, max_iterations=max_iterations, on_iteration_end=on_iteration_end)
# should work on sparse matrices too, but beware zeros in the initial estimates
if (require(Matrix)) {
 real_L <- randmat(nr,dm,min=-1)</pre>
 real_R <- randmat(dm,nc,min=-1)</pre>
 Y <- as(real_L %*% real_R, "sparseMatrix")</pre>
 L_0 <- randmat(nr,dm)</pre>
 R_0 <- randmat(dm,nc)</pre>
out1 <- murnmf(Y, L_0, R_0, max_iterations=1e2L)</pre>
}
```

rnnmf-NEWS

#### News for package 'rnnmf':

# Description

News for package 'rnnmf'

#### rnnmf Initial Version 0.3.0 (2024-10-30)

- first CRAN release.
- changed name from rnmf to rnnmf.

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