

Package ‘robslopes’

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Title Fast Algorithms for Robust Slopes

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Description Fast algorithms for the Theil-Sen estimator, Siegel's repeated median slope estimator, and Passing-Bablok regression. The implementation is based on algorithms by Dillencourt et. al (1992) <doi:10.1142/S0218195992000020> and Matousek et. al (1998) <doi:10.1007/PL00009190>. The implementations are detailed in Raymaekers (2023) <doi:10.32614/RJ-2023-012> and Raymaekers J., Dufey F. (2022) <doi:10.48550/arXiv.2202.08060>. All algorithms run in quasilinear time.

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Contents

PassingBablok	2
RepeatedMedian	3
robslope	5
robslope.fit	7
TheilSen	9

Index	12
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PassingBablok

Passing-Bablok slope and intercept estimator.

Description

Computes the equivariant Passing-Bablok regression. The implemented algorithm was proposed by Raymaekers and Dufey (2022) and runs in an expected $O(n \log n)$ time while requiring $O(n)$ storage.

Usage

```
PassingBablok(x, y, alpha = NULL, verbose = TRUE)
```

Arguments

x	A vector of predictor values.
y	A vector of response values.
alpha	Determines the order statistic of the target slope, which is equal to $\lceil \alpha * n * (n - 1) \rceil$, where n denotes the sample size. Defaults to NULL, which corresponds with the (upper) median.
verbose	Whether or not to print out the progress of the algorithm. Defaults to TRUE.

Details

Given two input vectors x and y of length n , the equivariant Passing-Bablok estimator is computed as $med_{ij} |(y_i - y_j) / (x_i - x_j)|$. By default, the median in this expression is the upper median, defined as $\lfloor (n + 2) / 2 \rfloor$. By changing α , other order statistics of the slopes can be computed.

Value

A list with elements:

intecept	The estimate of the intercept.
slope	The Theil-Sen estimate of the slope.

Author(s)

Jakob Raymaekers

References

Passing, H., Bablok, W. (1983). A new biometrical procedure for testing the equality of measurements from two different analytical methods. Application of linear regression procedures for method comparison studies in clinical chemistry, Part I, *Journal of clinical chemistry and clinical biochemistry*, **21**,709-720.

Bablok, W., Passing, H., Bender, R., Schneider, B. (1988). A general regression procedure for method transformation. Application of linear regression procedures for method comparison studies in clinical chemistry, Part III. *Journal of clinical chemistry and clinical biochemistry*, **26**,783-790.

Raymaekers J., Dufey F. (2022). Equivariant Passing-Bablok regression in quasilinear time. ([link to open access pdf](#))

Examples

We compare the implemented algorithm against a naive brute-force approach.

```
bruteForcePB <- function(x, y) {

  n <- length(x)
  medind1 <- floor(((n * (n - 1)) / 2 + 2) / 2) # upper median
  medind2 <- floor((n + 2) / 2)
  temp <- t(sapply(1:n, function(z) apply(cbind(x, y), 1,
                                         function(k) (k[2] - y[z]) /
                                                         (k[1] - x[z])))))
  PBslope <- sort(abs(as.vector(temp[lower.tri(temp)])))[medind1]
  PBintercept <- sort(y - x * PBslope)[medind2]
  return(list(intercept = PBintercept, slope = PBslope))
}

n = 100
set.seed(2)
x = rnorm(n)
y = x + rnorm(n)

t0 <- proc.time()
PB.fast <- PassingBablok(x, y, NULL, FALSE)
t1 <- proc.time()
t1 - t0

t0 <- proc.time()
PB.naive <- bruteForcePB(x, y)
t1 <- proc.time()
t1 - t0

PB.fast$slope - PB.naive$slope
```

RepeatedMedian

Siegel's repeated median slope and intercept estimator.

Description

Computes the repeated median slope proposed by Siegel (1982) using the algorithm by Matousek et. al (1998). The algorithm runs in an expected $O(n(\log n)^2)$ time, which is typically significantly faster than the $O(n^2)$ computational cost of the naive algorithm, and requires $O(n)$ storage.

Usage

```
RepeatedMedian(x, y, alpha = NULL, beta = NULL, verbose = TRUE)
```

Arguments

x	A vector of predictor values.
y	A vector of response values.
alpha	Determines the outer order statistic, which is equal to $\lceil \alpha * n \rceil$, where n denotes the sample size. Defaults to NULL, which corresponds with the (upper) median.
beta	Determines the inner order statistic, which is equal to $\lceil \beta * (n - 1) \rceil$, where n denotes the sample size. Defaults to NULL, which corresponds with the (upper) median.
verbose	Whether or not to print out the progress of the algorithm. Defaults to TRUE.

Details

Given two input vectors x and y of length n , the repeated median is computed as $med_i med_j (y_i - y_j) / (x_i - x_j)$. The default "outer" median is the $\lfloor (n+2)/2 \rfloor$ largest element in the ordered median slopes. The inner median, which for each observation is calculated as the median of the slopes connected to this observation, is the $\lfloor (n+1)/2 \rfloor$ largest element in the ordered slopes. By changing alpha and beta, other repeated order statistics of the slopes can be computed.

Value

A list with elements:

intecept	The estimate of the intercept.
slope	The Theil-Sen estimate of the slope.

Author(s)

Jakob Raymaekers

References

- Siegel, A. F. (1982). Robust regression using repeated medians. *Biometrika*, **69**(1), 242-244.
- Matousek, J., Mount, D. M., & Netanyahu, N. S. (1998). Efficient randomized algorithms for the repeated median line estimator. *Algorithmica*, **20**(2), 136-150.
- Raymaekers (2023). "The R Journal: robslopes: Efficient Computation of the (Repeated) Median Slope", The R Journal. ([link to open access pdf](#))

See Also

[TheilSen](#)

Examples

```
# We compare the implemented algorithm against a naive brute-force approach.

bruteForceRM <- function(x, y) {

  n <- length(x)
  medind1 <- floor((n+2) / 2)
  medind2 <- floor((n+1) / 2)
  temp <- t(sapply(1:n, function(z) sort(apply(cbind(x, y), 1 ,
                                          function(k) (k[2] - y[z]) /
                                          (k[1] - x[z])))))

  RMSlope <- sort(temp[, medind2])[medind1]
  RMintercept <- sort(y - x * RMSlope)[medind1]
  return(list(intercept = RMintercept, slope = RMSlope))
}

n = 100
set.seed(2)
x = rnorm(n)
y = x + rnorm(n)

t0 <- proc.time()
RM.fast <- RepeatedMedian(x, y, NULL, NULL, FALSE)
t1 <- proc.time()
t1 - t0

t0 <- proc.time()
RM.naive <- bruteForceRM(x, y)
t1 <- proc.time()
t1 - t0

RM.fast$slope - RM.naive$slope
```

robslope

Robust slope estimator

Description

Computes the Theil-Sen median slope, Siegel's repeated median slope or the equivariant Passing-Bablok slope. The algorithms run in an expected linearithmic time while requiring $O(n)$ storage. They are based on Dillencourt et. al (1992), Matousek et. al (1998) and Raymaekers and Dufey (2022).

Usage

```
robslope(formula, data, subset, weights, na.action,
         type = c("TheilSen", "RepeatedMedian", "PassingBablok"),
         alpha = NULL, beta = NULL, verbose = TRUE)
```

Arguments

formula	an object of class " formula " (or one that can be coerced to that class): a symbolic description of the model to be fitted. The details of model specification are given under 'Details'.
data	an optional data frame, list or environment (or object coercible by as.data.frame to a data frame) containing the variables in the model. If not found in data, the variables are taken from <code>environment(formula)</code> , typically the environment from which <code>robslope</code> is called.
subset	an optional vector specifying a subset of observations to be used in the fitting process.
weights	an optional vector of weights to be used in the fitting process. Currently not supported.
na.action	a function which indicates what should happen when the data contain NAs. The default na.exclude is applied and an informative message is given in case NAs were removed.
type	the type of robust slope estimator. Should be one of "TheilSen" (default), "RepeatedMedian" or "PassingBablok".
alpha	Determines the order statistic of the target slope. Defaults to the upper median. See below for details.
beta	Determines the inner order statistic. Only used when <code>type = "RepeatedMedian"</code> . See below for details.
verbose	Whether or not to print out the progress of the algorithm. Defaults to TRUE.

Details

This function provides a wrapper around [robslope.fit](#), which in turn calls the individual functions [TheilSen](#), [RepeatedMedian](#) or [PassingBablok](#). The details on changing the parameters `alpha` and `beta` can be found in the documentation of those respective functions.

Value

`robslope` returns an object of class "[lm](#)".

The generic accessor functions `coefficients`, `fitted.values` and `residuals` extract various useful features of the value returned by `lm`.

Author(s)

Jakob Raymaekers

References

- Theil, H. (1950), A rank-invariant method of linear and polynomial regression analysis (Parts 1-3), *Ned. Akad. Wetensch. Proc. Ser. A*, **53**, 386-392, 521-525, 1397-1412.
- Sen, P. K. (1968). Estimates of the regression coefficient based on Kendall's tau. *Journal of the American statistical association*, **63**(324), 1379-1389.

Dillencourt, M. B., Mount, D. M., & Netanyahu, N. S. (1992). A randomized algorithm for slope selection. *International Journal of Computational Geometry & Applications*, **2**(01), 1-27.

Siegel, A. F. (1982). Robust regression using repeated medians. *Biometrika*, **69**(1), 242-244.

Matousek, J., Mount, D. M., & Netanyahu, N. S. (1998). Efficient randomized algorithms for the repeated median line estimator. *Algorithmica*, **20**(2), 136-150.

Passing, H., Bablok, W. (1983). A new biometrical procedure for testing the equality of measurements from two different analytical methods. Application of linear regression procedures for method comparison studies in clinical chemistry, Part I, *Journal of clinical chemistry and clinical biochemistry*, **21**,709-720.

Bablok, W., Passing, H., Bender, R., Schneider, B. (1988). A general regression procedure for method transformation. Application of linear regression procedures for method comparison studies in clinical chemistry, Part III. *Journal of clinical chemistry and clinical biochemistry*, **26**,783-790.

Raymaekers J., Dufey F. (2022). Equivariant Passing-Bablok regression in quasilinear time. ([link to open access pdf](#))

Raymaekers (2023). "The R Journal: robslopes: Efficient Computation of the (Repeated) Median Slope", The R Journal. ([link to open access pdf](#))

See Also

[robslope.fit TheilSen RepeatedMedian PassingBablok](#)

Examples

```
set.seed(123)
df <- data.frame(cbind(rnorm(20), rnorm(20)))
colnames(df) <- c("x", "y")

robslope.out <- robslope(y~x, data = df,
type = "RepeatedMedian", verbose = TRUE)

coef(robslope.out)
plot(fitted.values(robslope.out))

robslope.out <- robslope(y~x, data = df,
type = "TheilSen", verbose = TRUE)

plot(residuals(robslope.out))
```

robslope.fit

Robust slope estimator

Description

This is the underlying computing engine called by [robslope](#) used to fit robust slopes. It wraps around the individual functions [TheilSen](#), [RepeatedMedian](#) or [PassingBablok](#). These should usually *not* be used directly unless by experienced users.

Usage

```
robslope.fit(x, y, weights, type, alpha = NULL, beta = NULL, verbose = TRUE)
```

Arguments

x	design matrix of dimension $n \times p$.
y	vector of observations of length n , or a matrix with n rows.
type	the type of robust slope estimator. Should be one of "TheilSen" (default), "RepeatedMedian" or "PassingBablok".
weights	vector of weights. Currently not in use.
alpha	Determines the order statistic of the target slope. Defaults to the upper median. See below for details.
beta	Determines the inner order statistic. Only used when <code>type = "RepeatedMedian"</code> . See below for details.
verbose	Whether or not to print out the progress of the algorithm. Defaults to TRUE.

Details

This function provides a wrapper around the individual functions [TheilSen](#), [RepeatedMedian](#) or [PassingBablok](#). The details on changing the parameters `alpha` and `beta` can be found in the documentation of those respective functions.

Value

[list](#) with components

coefficients	p vector
residuals	n vector or matrix
fitted.values	n vector or matrix

Author(s)

Jakob Raymaekers

References

- Theil, H. (1950), A rank-invariant method of linear and polynomial regression analysis (Parts 1-3), *Ned. Akad. Wetensch. Proc. Ser. A*, **53**, 386-392, 521-525, 1397-1412.
- Sen, P. K. (1968). Estimates of the regression coefficient based on Kendall's tau. *Journal of the American statistical association*, **63**(324), 1379-1389.
- Dillencourt, M. B., Mount, D. M., & Netanyahu, N. S. (1992). A randomized algorithm for slope selection. *International Journal of Computational Geometry & Applications*, **2**(01), 1-27.
- Siegel, A. F. (1982). Robust regression using repeated medians. *Biometrika*, **69**(1), 242-244.
- Matousek, J., Mount, D. M., & Netanyahu, N. S. (1998). Efficient randomized algorithms for the repeated median line estimator. *Algorithmica*, **20**(2), 136-150.

Passing, H., Bablok, W. (1983). A new biometrical procedure for testing the equality of measurements from two different analytical methods. Application of linear regression procedures for method comparison studies in clinical chemistry, Part I, *Journal of clinical chemistry and clinical biochemistry*, **21**,709-720.

Bablok, W., Passing, H., Bender, R., Schneider, B. (1988). A general regression procedure for method transformation. Application of linear regression procedures for method comparison studies in clinical chemistry, Part III. *Journal of clinical chemistry and clinical biochemistry*, **26**,783-790.

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Raymaekers (2023). "The R Journal: robslopes: Efficient Computation of the (Repeated) Median Slope", The R Journal. ([link to open access pdf](#))

See Also

[robslope TheilSen RepeatedMedian PassingBablok](#)

Examples

```
set.seed(123)
x <- rnorm(20)
y <- rnorm(20)

robslope.out <- robslope.fit(x, y, type = "RepeatedMedian", verbose = TRUE)

coef(robslope.out)
plot(fitted.values(robslope.out))

robslope.out <- robslope.fit(x, y, type = "TheilSen", verbose = TRUE)

plot(residuals(robslope.out))
```

TheilSen

Theil-Sen slope and intercept estimator.

Description

Computes the Theil-Sen median slope estimator by Theil (1950) and Sen (1968). The implemented algorithm was proposed by Dillencourt et. al (1992) and runs in an expected $O(n \log n)$ time while requiring $O(n)$ storage.

Usage

```
TheilSen(x, y, alpha = NULL, verbose = TRUE)
```



```
    TSslope <- sort(as.vector(temp[lower.tri(temp)]))[medind1]
    TSintercept <- sort(y - x * TSslope)[medind2]
    return(list(intercept = TSintercept, slope = TSslope))
}
```

```
n = 100
set.seed(2)
x = rnorm(n)
y = x + rnorm(n)

t0 <- proc.time()
TS.fast <- TheilSen(x, y, NULL, FALSE)
t1 <- proc.time()
t1 - t0

t0 <- proc.time()
TS.naive <- bruteForceTS(x, y)
t1 <- proc.time()
t1 - t0

TS.fast$slope - TS.naive$slope
```

Index

`as.data.frame`, [6](#)

`class`, [6](#)

`formula`, [6](#)

`list`, [8](#)

`na.exclude`, [6](#)

`PassingBablok`, [2](#), [6–9](#)

`RepeatedMedian`, [3](#), [6–9](#)

`robslope`, [5](#), [7](#), [9](#)

`robslope.fit`, [6](#), [7](#), [7](#)

`TheilSen`, [4](#), [6–9](#), [9](#)