Package 'rsvd'

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Type Package

Title Randomized Singular Value Decomposition

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Description Low-rank matrix decompositions are fundamental tools and widely used for data analysis, dimension reduction, and data compression. Classically, highly accurate deterministic matrix algorithms are used for this task. However, the emergence of large-scale data has severely challenged our computational ability to analyze big data. The concept of randomness has been demonstrated as an effective strategy to quickly produce approximate answers to familiar problems such as the singular value decomposition (SVD). The rsvd package provides several randomized matrix algorithms such as the randomized singular value decomposition (rsvd), randomized principal component analysis (rpca), randomized robust principal component analysis (rrpca), randomized interpolative decomposition (rid), and the randomized CUR decomposition (rcur). In addition several plot functions are provided.

Depends R (>= 4.0.0)

Imports Matrix

License GPL (>= 3)

LazyData TRUE

LazyDataCompression xz

URL https://github.com/erichson/rSVD

BugReports https://github.com/erichson/rSVD/issues

Suggests ggplot2, testthat

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`digits` *Digits*

Description

Subsampled MNIST database of handwritten digits. This smaller dataset has 3000 samples for each of the digits corresponding to the class labels 0,1,2,3. Each 28x28 image patch is stored as a flattened row vector.

Usage

```
data('digits')
```

Format

An object of class `rsvd`.

References

Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner. "Gradient-based learning applied to document recognition." Proceedings of the IEEE, 86(11):2278-2324, November 1998.

Examples

```
## Not run:
library('rsvd')
data('digits')

#Display first digit
digit <- matrix(digits[1,], nrow = 28, ncol = 28)
image(digit[,28:1], col = gray(255:0 / 255))
```

```
## End(Not run)
```

---

ggbiplot *Biplot for* rpca *using* ggplot.

Description

Creates a pretty biplot which is showing the individual factor map overlayed by the variables factor map, i.e, plotting both the principal component scores and directions.

Usage

```
ggbiplot(
  rpcaObj,
  pcs = c(1, 2),
  loadings = TRUE,
  groups = NULL,
  alpha = 0.6,
  ellipse = TRUE,
  alpha.ellipse = 0.2,
  var_labels = TRUE,
  var_labels.names = NULL,
  ind_labels = TRUE,
  ind_labels.names = NULL
)
```

Arguments

rpcaObj	Object returned by the rpca function.
pcs	Array_like. An array with two values indicating the two PCs which should be used for plotting. By default the first two PCs are used, e.g., $c(1, 2)$.
loadings	Bool ($TRUE$, $FALSE$), optional. If $TRUE$, the eigenvectors are unit scaled by the square root of the eigenvalues $W = W * diag(sqrt(eigvals))$.
groups	Factor, optional. Factor indicating groups.
alpha	Scalar, optional. Alpha transparency for scatter plot.
ellipse	Bool ($TRUE$, $FALSE$), optional. Draw a 1sd data ellipse for each group, if $TRUE$.
alpha.ellipse	Scalar, optional. Alpha transparency for ellipse.

`var_labels` Bool ($TRUE$, $FALSE$), optional.
Plot variable names, if $TRUE$.

`var_labels.names`
Array_like, optional.
User specific labels for the individuals.

`ind_labels` Bool ($TRUE$, $FALSE$), optional.
Plot data point names, if $TRUE$.

`ind_labels.names`
Array_like, optional.
User specific labels for data points.

Author(s)

N. Benjamin Erichson, <erichson@berkeley.edu>

See Also

rpca, ggplot

Examples

```
#See ?rpca
```

`ggcorplot` *Variables factor map for* rpca *using* ggplot.

Description

Creates a pretty plot which is showing the correlation of the original variable with the principal component (PCs).

Usage

```
ggcorplot(
  rpcaObj,
  pcs = c(1, 2),
  loadings = TRUE,
  var_labels = FALSE,
  var_labels.names = NULL,
  alpha = 1,
  top.n = NULL
)
```

Arguments

rpcaObj	Object returned by the rpca function.
pcs	Array_like. An array with two values indicating the two PCs which should be used for plotting. By default the first two PCs are used, e.g., $c(1, 2)$.
loadings	Bool ($TRUE$, $FALSE$), optional. If $TRUE$, the eigenvectors are unit scaled by the square root of the eigenvalues $W = W * diag(sqrt(eigvals))$.
var_labels	Bool ($TRUE$, $FALSE$), optional. Plot variable names, if $TRUE$.
var_labels.names	Array_like, optional. User specific labels for the variables
alpha	Scalar, optional. Alpha transparency of the arrows.
top.n	Scalar, optional. Number of (most influencial) variables to label with small circles.

Author(s)

N. Benjamin Erichson, <erichson@berkeley.edu>

See Also

rpca, ggplot

Examples

```
#
```

---

ggindplot *Individual factor map for* rpca *using* ggplot.

Description

Creates a pretty plot which is showing the individual factor map, i.e, plotting the principal component scores.

Usage

```
ggindplot(
  rpcaObj,
  pcs = c(1, 2),
  groups = NULL,
  alpha = 0.6,
  ellipse = TRUE,
  alpha.ellipse = 0.2,
  ind_labels = TRUE,
  ind_labels.names = NULL
)
```

Arguments

rpcaObj	Object returned by the rpca function.
pcs	Array_like. An array with two values indicating the two PCs which should be used for plotting. By default the first two PCs are used, e.g., $c(1, 2)$.
groups	Factor, optional. Factor indicating groups.
alpha	Scalar, optional. Alpha transparency for scatter plot.
ellipse	Bool ($TRUE$, $FALSE$), optional. Draw a 1sd data ellipse for each group, if $TRUE$.
alpha.ellipse	Scalar, optional. Alpha transparency for ellipse.
ind_labels	Bool ($TRUE$, $FALSE$), optional. Plot names for each individual point, if $TRUE$.
ind_labels.names	Array_like, optional. User specific labels for the individual points.

Author(s)

N. Benjamin Erichson, <erichson@berkeley.edu>

See Also

rpca, ggplot

Examples

```
#See ?rpca
```

ggscreeplot *Pretty Screeplot*

Description

Creates a pretty screeplpot using ggplot. By default the explained variance is plotted againgst the number of the principal component. Alternatively the explained variance ratio, the cumulative explained variance ratio, or the eigenvalues can be plotted.

Usage

```
ggscreeplot(rpcaObj, type = c("var", "ratio", "cum", "eigenvals"))
```

Arguments

rpcaObj	Object returned by the rpca function.
type	String c('var', 'ratio', 'cum', 'eigenvals'), optional.

Author(s)

N. Benjamin Erichson, <erichson@berkeley.edu>

See Also

rpca, ggplot

Examples

```
#
```

plot.rpca *Screeplot*

Description

Creates a screeplot, variables and individual factor maps to summarize the results of the rpca function.

Usage

```
## S3 method for class 'rpca'
plot(x, ...)
```

Arguments

x	Object returned by the rpca function.
...	Additional arguments passed to the individual plot functions (see below).

See Also

ggscreeplot, ggcorplot , ggindplot

Examples

```
#
```

---

rcur *Randomized CUR matrix decomposition.*

Description

Randomized CUR matrix decomposition.

Usage

```
rcur(A, k = NULL, p = 10, q = 0, idx_only = FALSE, rand = TRUE)
```

Arguments

A	array_like; numeric (m, n) input matrix (or data frame). If the data contain NAs na.omit is applied.
k	integer; target rank of the low-rank approximation, i.e., the number of columns/rows to be selected. It is required that k is smaller or equal to $min(m, n)$.
p	integer, optional; oversampling parameter (default $p = 10$).
q	integer, optional; number of additional power iterations (default $q = 0$).
idx_only	bool, optional; if ($TRUE$), only the index set C.idx and R.idx is returned, but not the matrices C and R. This is more memory efficient, when dealing with large-scale data.
rand	bool, optional; if ($TRUE$), a probabilistic strategy is used, otherwise a deterministic algorithm is used.

Details

Algorithm for computing the CUR matrix decomposition of a rectangular (m, n) matrix A, with target rank $k << min(m, n)$. The input matrix is factored as

$$A = C * U * R$$

using the `rid` decomposition. The factor matrix C is formed using actual columns of A, also called the partial column skeleton. The factor matrix R is formed using actual rows of A, also called the partial row skeleton.

If $rand = TRUE$ a probabilistic strategy is used to compute the decomposition, otherwise a deterministic algorithm is used.

Value

`rcur` returns a list with class id containing the following components:

C array_like;
column subset $C = A[, C.idx]$; (m, k) dimensional array.

R Array_like.
row subset $R = A[R.idx,]$; (k, n) dimensional array.

U array_like;
connector matrix; (k, k) dimensional array.

C.idx array_like;
index set of the k selected columns used to form C.

R.idx array_like;
index set of the k selected rows used to form R.

C.scores array_like;
scores of the selected columns.

R.scores array_like;
scores of the selected rows.

Author(s)

N. Benjamin Erichson, <erichson@berkeley.edu>

References

- [1] N. B. Erichson, S. Voronin, S. L. Brunton and J. N. Kutz. 2019. Randomized Matrix Decompositions Using R. Journal of Statistical Software, 89(11), 1-48. doi: 10.18637/jss.v089.i11.
- [2] N. Halko, P. Martinsson, and J. Tropp. "Finding structure with randomness: probabilistic algorithms for constructing approximate matrix decompositions" (2009). (available at arXiv https://arxiv.org/abs/0909.4061).

See Also

`rid`

Examples

```
## Not run:
# Load test image
data('tiger')

# Compute (column) randomized interpolative decompsition
# Note that the image needs to be transposed for correct plotting
out <- rcur(tiger, k = 150)

# Reconstruct image
tiger.re <- out$C %*% out$U %*% out$R

# Compute relative error
print(norm(tiger-tiger.re, 'F') / norm(tiger, 'F'))

# Plot approximated image
image(tiger.re, col = gray((0:255)/255))

## End(Not run)
```

`rid` *Randomized interpolative decomposition (ID).*

Description

Randomized interpolative decomposition.

Usage

```
rid(A, k = NULL, mode = "column", p = 10, q = 0, idx_only = FALSE, rand = TRUE)
```

Arguments

`A`	array_like; numeric (m, n) input matrix (or data frame). If the data contain NAs na.omit is applied.
`k`	integer, optional; number of rows/columns to be selected. It is required that k is smaller or equal to $min(m, n)$.
`mode`	string c('column', 'row'), optional; columns or rows ID.
`p`	integer, optional; oversampling parameter (default $p = 10$).
`q`	integer, optional. number of additional power iterations (default $q = 0$).

`idx_only` bool, optional;
if ($TRUE$), the index set `idx` is returned, but not the matrix `C` or `R`. This is more memory efficient, when dealing with large-scale data.

`rand` bool, optional;
if ($TRUE$), a probabilistic strategy is used, otherwise a deterministic algorithm is used.

Details

Algorithm for computing the ID of a rectangular (m, n) matrix A, with target rank $k << min(m, n)$. The input matrix is factored as

$$A = C * Z$$

using the column pivoted QR decomposition. The factor matrix C is formed as a subset of columns of A, also called the partial column skeleton. If `mode='row'`, then the input matrix is factored as

$$A = Z * R$$

using the row pivoted QR decomposition. The factor matrix R is now formed as a subset of rows of A, also called the partial row skeleton. The factor matrix Z contains a (k, k) identity matrix as a submatrix, and is well-conditioned.

If $rand =' TRUE'$ a probabilistic strategy is used to compute the decomposition, otherwise a deterministic algorithm is used.

Value

`rid` returns a list containing the following components:

C array_like;
column subset $C = A[, idx]$, if `mode='column'`; array with dimensions (m, k).

R array_like;
row subset $R = A[idx,]$, if `mode='row'`; array with dimensions (k, n).

Z array_like;
well conditioned matrix; Depending on the selected mode, this is an array with dimensions (k, n) or (m, k).

idx array_like;
index set of the k selected columns or rows used to form C or R.

pivot array_like;
information on the pivoting strategy used during the decomposition.

scores array_like;
scores of the columns or rows of the input matrix A.

scores.idx array_like;
scores of the k selected columns or rows in C or R.

Author(s)

N. Benjamin Erichson, <erichson@uw.edu>

References

- [1] N. Halko, P. Martinsson, and J. Tropp. "Finding structure with randomness: probabilistic algorithms for constructing approximate matrix decompositions" (2009). (available at arXiv https://arxiv.org/abs/0909.4061).
- [2] N. B. Erichson, S. Voronin, S. L. Brunton and J. N. Kutz. 2019. Randomized Matrix Decompositions Using R. Journal of Statistical Software, 89(11), 1-48. doi: 10.18637/jss.v089.i11.

See Also

rcur,

Examples

```
## Not run:
# Load test image
data("tiger")

# Compute (column) randomized interpolative decompsition
# Note that the image needs to be transposed for correct plotting
out <- rid(t(tiger), k = 150)

# Show selected columns
tiger.partial <- matrix(0, 1200, 1600)
tiger.partial[,out$idx] <- t(tiger)[,out$idx]
image(t(tiger.partial), col = gray((0:255)/255), useRaster = TRUE)

# Reconstruct image
tiger.re <- t(out$C %*% out$Z)

# Compute relative error
print(norm(tiger-tiger.re, 'F') / norm(tiger, 'F'))

# Plot approximated image
image(tiger.re, col = gray((0:255)/255))

## End(Not run)
```

---

rpca *Randomized principal component analysis (rpca).*

Description

Fast computation of the principal components analysis using the randomized singular value decomposition.

Usage

```
rpca(
  A,
  k = NULL,
  center = TRUE,
  scale = TRUE,
  retx = TRUE,
  p = 10,
  q = 2,
  rand = TRUE
)
```

Arguments

A	array_like; a numeric (m, n) input matrix (or data frame) to be analyzed. If the data contain NAs na.omit is applied.
k	integer; number of dominant principle components to be computed. It is required that k is smaller or equal to $min(m, n)$, but it is recommended that $k << min(m, n)$.
center	bool, optional; logical value which indicates whether the variables should be shifted to be zero centered ($TRUE$ by default).
scale	bool, optional; logical value which indicates whether the variables should be scaled to have unit variance ($TRUE$ by default).
retx	bool, optional; logical value indicating whether the rotated variables / scores should be returned ($TRUE$ by default).
p	integer, optional; oversampling parameter for $rsvd$ (default $p = 10$), see rsvd.
q	integer, optional; number of additional power iterations for $rsvd$ (default $q = 1$), see rsvd.
rand	bool, optional; if ($TRUE$), the $rsvd$ routine is used, otherwise svd is used.

Details

Principal component analysis is an important linear dimension reduction technique.

Randomized PCA is computed via the randomized SVD algorithm (rsvd). The computational gain is substantial, if the desired number of principal components is relatively small, i.e. $k << min(m, n)$.

The print and summary method can be used to present the results in a nice format. A scree plot can be produced with ggscreeplot. The individuals factor map can be produced with ggindplot, and a correlation plot with ggcorplot.

The predict function can be used to compute the scores of new observations. The data will automatically be centered (and scaled if requested). This is not fully supported for complex input matrices.

Value

rpca returns a list with class $rpca$ containing the following components:

rotation array_like;
the rotation (eigenvectors); (n, k) dimensional array.

eigvals array_like;
eigenvalues; k dimensional vector.

sdev array_like;
standard deviations of the principal components; k dimensional vector.

x array_like;
the scores / rotated data; (m, k) dimensional array.

center, scale array_like;
the centering and scaling used.

Note

The principal components are not unique and only defined up to sign (a constant of modulus one in the complex case) and so may differ between different PCA implementations.

Similar to prcomp the variances are computed with the usual divisor N - 1.

Author(s)

N. Benjamin Erichson, <erichson@berkeley.edu>

References

- [1] N. B. Erichson, S. Voronin, S. L. Brunton and J. N. Kutz. 2019. Randomized Matrix Decompositions Using R. Journal of Statistical Software, 89(11), 1-48. doi: 10.18637/jss.v089.i11.
- [2] N. Halko, P. Martinsson, and J. Tropp. "Finding structure with randomness: probabilistic algorithms for constructing approximate matrix decompositions" (2009). (available at arXiv https://arxiv.org/abs/0909.4061).

See Also

ggscreeplot, ggindplot, ggcorplot, plot.rpca, predict, rsvd

Examples

```
library('rsvd')
#
# Load Edgar Anderson's Iris Data
#
data('iris')
```

```
#
# log transform
#
log.iris <- log( iris[ , 1:4] )
iris.species <- iris[ , 5]

#
# Perform rPCA and compute only the first two PCs
#
iris.rpca <- rpca(log.iris, k=2)
summary(iris.rpca) # Summary
print(iris.rpca) # Prints the rotations

#
# Use rPCA to compute all PCs, similar to \code{\link{prcomp}}
#
iris.rpca <- rpca(log.iris)
summary(iris.rpca) # Summary
print(iris.rpca) # Prints the rotations
plot(iris.rpca) # Produce screeplot, variable and individuls factor maps.
```

---

rqb *Randomized QB Decomposition (rqb).*

Description

Compute the near-optimal QB decomposition of a rectangular matrix.

Usage

```
rqb(A, k = NULL, p = 10, q = 2, sdist = "normal", rand = TRUE)
```

Arguments

A	array_like; real/complex (m, n) input matrix (or data frame).
k	integer, optional; target rank of the low-rank decomposition. It should satisfy $k << min(m, n)$.
p	integer, optional; oversampling parameter (default $p = 10$).
q	integer, optional; number of power iterations (default $q = 2$).
sdist	string $c('unif','normal','rademacher')$, optional; specifies the sampling distribution: $'unif'$: Uniform '[-1,1]'. $'normal'$' (default) : Normal '~N(0,1)'.

$'rademacher'$: Rademacher random variates.

`rand` bool, optional;
If ($TRUE$), a probabilistic strategy is used, otherwise a deterministic algorithm is used.

Details

The randomized QB decomposition factors a rectangular (m, n) matrix A as $A = Q * B$. Q is an (m, k) matrix with orthogonal columns, and B a (k, n) matrix. The target rank is assumed to be $k << min(m, n)$.

p is an oversampling parameter to improve the approximation. A value between 5 and 10 is recommended, and $p = 10$ is set by default.

The parameter q specifies the number of power (subspace) iterations to reduce the approximation error. This is recommended if the the singular values decay slowly. In practice 1 or 2 iterations achieve good results, however, computing power iterations increases the computational time. The number of power iterations is set to $q = 2$ by default.

Value

`rqb` returns a list containing the following components:

Q array_like;
matrix with orthogonal columns; (m, k) dimensional array.

B array_like;
smaller matrix; (k, n) dimensional array.

Author(s)

N. Benjamin Erichson, <erichson@berkeley.edu>

References

- [1] N. B. Erichson, S. Voronin, S. L. Brunton and J. N. Kutz. 2019. Randomized Matrix Decompositions Using R. Journal of Statistical Software, 89(11), 1-48. doi: 10.18637/jss.v089.i11.
- [2] N. Halko, P. Martinsson, and J. Tropp. "Finding structure with randomness: probabilistic algorithms for constructing approximate matrix decompositions" (2009). (available at arXiv https://arxiv.org/abs/0909.4061).

See Also

svd

`rrpca` *Randomized robust principal component analysis (rrpca).*

Description

Robust principal components analysis separates a matrix into a low-rank plus sparse component.

Usage

```
rrpca(
  A,
  lambda = NULL,
  maxiter = 50,
  tol = 1e-05,
  p = 10,
  q = 2,
  trace = FALSE,
  rand = TRUE
)
```

Arguments

`A`	array_like; a real (m, n) input matrix (or data frame) to be decomposed. na.omit is applied, if the data contain NAs.
`lambda`	scalar, optional; tuning parameter (default $lambda = max(m, n)^-0.5$).
`maxiter`	integer, optional; maximum number of iterations (default $maxiter = 50$).
`tol`	scalar, optional; precision parameter (default $tol = 1.0e - 5$).
`p`	integer, optional; oversampling parameter for $rsvd$ (default $p = 10$), see `rsvd`.
`q`	integer, optional; number of additional power iterations for $rsvd$ (default $q = 2$), see `rsvd`.
`trace`	bool, optional; print progress.
`rand`	bool, optional; if ($TRUE$), the $rsvd$ routine is used, otherwise svd is used.

Details

Robust principal component analysis (RPCA) is a method for the robust seperation of a a rectangular (m, n) matrix A into a low-rank component L and a sparse comonent S:

$$A = L + S$$

To decompose the matrix, we use the inexact augmented Lagrange multiplier method (IALM). The algorithm can be used in combination with either the randomized or deterministic SVD.

Value

`rrpca` returns a list containing the following components:

L array_like;
low-rank component; (m, n) dimensional array.

S array_like
sparse component; (m, n) dimensional array.

Author(s)

N. Benjamin Erichson, <erichson@berkeley.edu>

References

- [1] N. B. Erichson, S. Voronin, S. L. Brunton and J. N. Kutz. 2019. Randomized Matrix Decompositions Using R. Journal of Statistical Software, 89(11), 1-48. doi: 10.18637/jss.v089.i11.
- [2] Lin, Zhouchen, Minming Chen, and Yi Ma. "The augmented lagrange multiplier method for exact recovery of corrupted low-rank matrices." (2010). (available at arXiv https://arxiv.org/abs/1009.5055).

Examples

```
library('rsvd')

# Create toy video
# background frame
xy <- seq(-50, 50, length.out=100)
mgrid <- list( x=outer(xy*0,xy,FUN="+"), y=outer(xy,xy*0,FUN="+") )
bg <- 0.1*exp(sin(-mgrid$x**2-mgrid$y**2))
toyVideo <- matrix(rep(c(bg), 100), 100*100, 100)

# add moving object
for(i in 1:90) {
  mobject <- matrix(0, 100, 100)
  mobject[i:(10+i), 45:55] <- 0.2
  toyVideo[,i] =  toyVideo[,i] + c( mobject )
}

# Foreground/Background separation
out <- rrpca(toyVideo, trace=TRUE)

# Display results of the seperation for the 10th frame
par(mfrow=c(1,4))
```

```
image(matrix(bg, ncol=100, nrow=100)) #true background
image(matrix(toyVideo[,10], ncol=100, nrow=100)) # frame
image(matrix(out$L[,10], ncol=100, nrow=100)) # seperated background
image(matrix(out$S[,10], ncol=100, nrow=100)) #seperated foreground
```

`rsvd` *Randomized Singular Value Decomposition (rsvd).*

Description

The randomized SVD computes the near-optimal low-rank approximation of a rectangular matrix using a fast probablistic algorithm.

Usage

```
rsvd(A, k = NULL, nu = NULL, nv = NULL, p = 10, q = 2, sdist = "normal")
```

Arguments

`A`	array_like; a real/complex (m, n) input matrix (or data frame) to be decomposed.
`k`	integer; specifies the target rank of the low-rank decomposition. k should satisfy $k << min(m, n)$.
`nu`	integer, optional; number of left singular vectors to be returned. nu must be between 0 and k.
`nv`	integer, optional; number of right singular vectors to be returned. nv must be between 0 and k.
`p`	integer, optional; oversampling parameter (by default $p = 10$).
`q`	integer, optional; number of additional power iterations (by default $q = 2$).
`sdist`	string $c('unif','normal','rademacher')$, optional; specifies the sampling distribution of the random test matrix: $'unif'$: Uniform '[-1,1]'. $'normal'$' (default) : Normal '~N(0,1)'. $'rademacher'$: Rademacher random variates.

Details

The singular value decomposition (SVD) plays an important role in data analysis, and scientific computing. Given a rectangular (m, n) matrix A, and a target rank $k << min(m, n)$, the SVD factors the input matrix A as

$$A = U_k diag(d_k) V_k^\top$$

The k left singular vectors are the columns of the real or complex unitary matrix U. The k right singular vectors are the columns of the real or complex unitary matrix V. The k dominant singular values are the entries of d, and non-negative and real numbers.

p is an oversampling parameter to improve the approximation. A value of at least 10 is recommended, and $p = 10$ is set by default.

The parameter q specifies the number of power (subspace) iterations to reduce the approximation error. The power scheme is recommended, if the singular values decay slowly. In practice, 2 or 3 iterations achieve good results, however, computing power iterations increases the computational costs. The power scheme is set to $q = 2$ by default.

If $k > (min(n, m)/4)$, a deterministic partial or truncated svd algorithm might be faster.

Value

rsvd returns a list containing the following three components:

d array_like;
singular values; vector of length (k).

u array_like;
left singular vectors; (m, k) or (m, nu) dimensional array.

v array_like;
right singular vectors; (n, k) or (n, nv) dimensional array.

Note

The singular vectors are not unique and only defined up to sign (a constant of modulus one in the complex case). If a left singular vector has its sign changed, changing the sign of the corresponding right vector gives an equivalent decomposition.

Author(s)

N. Benjamin Erichson, <erichson@berkeley.edu>

References

- [1] N. B. Erichson, S. Voronin, S. L. Brunton and J. N. Kutz. 2019. Randomized Matrix Decompositions Using R. Journal of Statistical Software, 89(11), 1-48. doi: 10.18637/jss.v089.i11.
- [2] N. Halko, P. Martinsson, and J. Tropp. "Finding structure with randomness: probabilistic algorithms for constructing approximate matrix decompositions" (2009). (available at arXiv https://arxiv.org/abs/0909.4061).

See Also

svd, rpca

Examples

```
library('rsvd')

# Create a n x n Hilbert matrix of order n,
# with entries H[i,j] = 1 / (i + j + 1).
hilbert <- function(n) { i <- 1:n; 1 / outer(i - 1, i, "+") }
H <- hilbert(n=50)

# Low-rank (k=10) matrix approximation using rsvd
k=10
s <- rsvd(H, k=k)
Hre <- s$u %*% diag(s$d) %*% t(s$v) # matrix approximation
print(100 * norm( H - Hre, 'F') / norm( H,'F')) # percentage error
# Compare to truncated base svd
s <- svd(H)
Hre <- s$u[,1:k] %*% diag(s$d[1:k]) %*% t(s$v[,1:k]) # matrix approximation
print(100 * norm( H - Hre, 'F') / norm( H,'F')) # percentage error
```

`tiger` *Tiger*

Description

1600x1200 grayscaled (8 bit [0-255]/255) image.

Usage

```
data('tiger')
```

Format

An object of class `rsvd`.

Source

Wikimedia

References

S. Taheri (2006). "Panthera tigris altaica", (Online image)

Examples

```
## Not run:
library('rsvd')
data('tiger')

#Display image
```

```
image(tiger, col = gray((0:255)/255))

## End(Not run)
```

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