# Package 'sensmediation'

July 23, 2025

Title Parametric Estimation and Sensitivity Analysis of Direct and

**Indirect Effects** 

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Description We implement functions to estimate and perform sensitivity analysis to unobserved confounding of direct and indirect effects introduced in Lindmark, de Luna and Eriksson (2018) <doi:10.1002 sim.7620=""> and Lindmark (2022) <doi:10.1007 s10260-021-00611-4="">. The estimation and sensitivity analysis are parametric, based on probit and/or linear regression models. Sensitivity analysis is implemented for unobserved confounding of the exposure-mediator, mediator-outcome and exposure-outcome relationships.</doi:10.1007></doi:10.1002>
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Author Anita Lindmark [aut, cre]
Maintainer Anita Lindmark <anita.lindmark@umu.se></anita.lindmark@umu.se>
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# Description

Function to estimate natural direct and indirect effect estimates and standard errors (using the delta method) based on parametric regression models and perform sensitivity analysis for unobserved confounding. Intended to be called through sensmediation (or more.effects), not on its own.

### Usage

```
calc.effects(
  ML.object,
  type = "my",
  exp.name,
  med.name,
  covariates = NULL,
  alt.decomposition = FALSE,
  exp.value = 1,
  control.value = 0,
  med.model = NULL,
  out.model = NULL
```

# Arguments

ML.object	object from coefs.sensmed
type	the type of confounding for which the sensitivity analysis is to be performed. type = "my", the default, corresponds to unobserved mediator-outcome confounding, type = "zm" to exposure-mediator confounding and type = "zy" to exposure-outcome confounding.
exp.name	A character string indicating the name of the exposure variable used in the models.

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med.name A character string indicating the name of the mediator used in the models.

covariates if conditional effects are to be estimated the list of covariate values. Covariates

not specified are marginalized over. For more information, see sensmediation.

alt.decomposition

logical indicating whether alternative definitions of the direct and indirect effects

should be used (for more information, see sensmediation).

exp. value value of the exposure variable used as the exposure condition, default is 1.

control.value value of the exposure variable used as the control (unexposed) condition, default

is 0.

med.model If type = "zy", fitted glm model object representing the mediator model at the

basis of the estimation.

out.model If type = "zm", fitted glm model object representing the outcome model at the

basis of the estimation.

#### Value

#### A list with elements:

effects A list with elements NIE and NDE, row matrices with the estimated NIE and

NDE (or NIE\* and NDE\* if alt.decomposition = TRUE) for each value of the

sensitivity parameter Rho.

std.errs A list with elements se.nie and se.nde, row matrices with the estimated stan-

dard errors for the natural direct and indirect effects for the different values of

the sensitivity parameter Rho.

betas list of the estimated mediator model parameters over Rho, with

• beta0 Intercept

• beta1 Exposure

• beta2 Covariates

• beta3 Exposure-covariate interactions

Components that are not included in the input mediator model are set to 0.

thetas list of the estimated outcome model parameters over Rho, with

• theta0 Intercept

• theta1 Exposure

• theta2 Mediator

• theta3 Exposure-mediator interaction

• theta4 Covariates

• theta5 Exposure-covariate interactions

• theta6 Mediator-covariate interactions

• theta7 Exposure-mediator-covariate interactions

Components that are not included in the input outcome model are set to 0.

part.deriv List with the partial derivatives of the NDE (Lambda), NIE (Gamma) and TE (Eta) wrt the mediator and outcome model parameters for each value of Rho

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sigma.thetabeta

a list with the joint covariance matrix of the outcome and mediator model parameters for each value of Rho. Note that the covariance matrix is constructed for all estimated parameters listed in betas and thetas but that components not included in the input mediator and outcome models are set to 0.

covariates list of the covariate values that the effects are conditioned on.

#### Author(s)

Anita Lindmark

#### See Also

sensmediation

coefs.sensmed

ML estimation of regression parameters for calculation of direct and indirect effects under unobserved confounding

# Description

This function gives ML estimates of the regression parameters used to calculate mediation effects and perform sensitivity analysis. The optimization is performed using maxLik, see Details for more information. Called by sensmediation.

#### Usage

```
coefs.sensmed(model.expl, model.resp, Rho, progress = TRUE, ...)
```

#### **Arguments**

model.expl	Fitted glm model object. If sensitivity analysis to mediator-outcome confounding the mediator model. Otherwise the exposure model.
model.resp	Fitted glm model object. If sensitivity analysis to exposure-mediator confounding the mediator model. Otherwise the outcome model.
Rho	The sensitivity parameter vector. If type="my" the correlation between the error terms in the mediator and outcome models. If type="zm" the correlation between the error terms in the exposure and mediator models. If type="zy" the correlation between the error terms in the exposure and outcome models.
progress	Logical, indicating whether or not the progress (i.e. the proc.time for each Rho) of the optimization will be output
• • •	Additional arguments to be passed on to the maxLik function. Can be used to set the method and control arguments of the maxLik function.

#### Details

The maximization of the log-likelihood is performed using maxLik, the default is to use the Newton-Raphson method and an analytic gradient and Hessian.

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# Value

coefs.sensmed returns a list with elements:

call	The matched call
coef	A matrix with the estimated regression parameters for model.resp over the range of Rho. One column per value of Rho.
sigma.res.resp	If $model.resp$ is a linear regression model, the estimated standard deviation of the error term for each Rho.
sigma.res.expl	If $model.expl$ is a linear regression model, the estimated standard deviation of the error term for each Rho.
Rho	The sensitivity parameter vector.
expl.coef	A matrix with the estimated regression parameters for $model.expl$ over the range of Rho. One column per value of Rho.
model.expl	the original fitted glm object of model.expl.
model.resp	the original fitted glm object of model.resp.
X.expl	The model matrix (see model.matrix) of model.expl
X.resp	The model matrix (see model.matrix) of model.resp
outc.resp	The outcome variable of model.resp.
outc.expl	The outcome variable of model.expl.
sigmas	A list with the estimated covariance matrices for the regression parameters of $model.resp$ and $model.expl$ over Rho.
max.info	Information about the maximization (whether or not the convergence was successful, message, method and number of iterations) for each Rho, see maxLik for more information.
value	The values of the loglikelihood function for the best set of regression parameters from the optimization for each Rho, see maxLik.

# Author(s)

Anita Lindmark

# References

Henningsen, A., Toomet, O. (2011). maxLik: A Package for Maximum Likelihood Estimation in R, *Computational Statistics*, **26(3)**, pp. 443–458.

# See Also

sensmediation

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#### **Examples**

```
## Not run:
# Example with data from Riksstroke (the Swedish stroke register)

data(RSdata)

# Probit mediator and outcome models:
m.model <- glm(lowered.consc ~ AF + age.cat + sex, data = RSdata,
    family = binomial(link = 'probit'))
o.model <- glm(cf.3mo ~ AF + lowered.consc + age.cat + sex, data = RSdata,
    family = binomial(link = 'probit'))

# Estimation of regression coefficients under different values of Rho
# Rho = correlation between error terms in mediator and outcome model:
coefs.MY <- coefs.sensmed(model.expl = m.model, model.resp = o.model, Rho = seq(0, 0.5, 0.1))
# Outcome model regression coefficients:
coefs.MY$coef

## End(Not run)</pre>
```

effects

Functions to calculate natural direct and indirect effects.

#### Description

Functions used to calculate natural direct and indirect effects based on the estimated regression parameters. Called by calc.effects. The functions are named according to the convention eff. "mediator model type" "outcome model type" where b stands for binary probit regression and c stands for linear regression.

```
eff.bb(
  Rho,
  betas,
  thetas,
  x.med,
  x.out,
  alt.decomposition,
  exp.value,
  control.value
)

eff.bc(
  Rho,
  betas,
  thetas,
```

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```
x.med,
 x.out,
  alt.decomposition,
 exp.value,
  control.value
)
eff.cb(
 Rho,
 betas,
  thetas,
  sigma.eta,
  x.med,
  x.out,
  alt.decomposition,
  exp.value,
  control.value
)
eff.cc(
 Rho,
 betas,
  thetas,
 x.med,
 x.out,
 alt.decomposition,
 exp.value,
  control.value
)
```

### **Arguments**

Rho The sensitivity parameter vector.

betas List of mediator regression parameters
thetas List of outcome regression parameters

x.med Mediator covariate matrix for which to calculate standard errorsx.out Outcome covariate matrix for which to calculate standard errors

alt.decomposition

logical indicating whether or not alternative definitions of the direct and indirect

effects should be used.

exp. value value of the exposure variable used as the exposure condition.

control.value value of the exposure variable used as the control (unexposed) condition.

sigma.eta For a continuous mediator and binary outcome, matrix with the estimated resid-

ual standard deviation for the mediator model over the range of Rho.

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grr

Analytic gradients of the loglikelihood functions for ML estimation of regression parameters

### **Description**

Implementation of the analytic gradients of the loglikelihood functions for ML estimation of regression parameters for different combinations of exposure, mediator and outcome models. The functions are named according to the convention grr."model.expl type""model.resp type" where b stands for binary probit regression and c stands for linear regression.

```
grr.bb(
  par,
  Rho,
 X.expl = X.expl,
 X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)
grr.bc(
  par,
  Rho,
  X.expl = X.expl,
  X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)
grr.cb(
  par,
  Rho,
 X.expl = X.expl,
 X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)
grr.cc(
  par,
  Rho,
  X.expl = X.expl,
  X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
```

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)

# **Arguments**

par Vector of parameter values.

Rho The value of the sensitivity parameter.

X.expl The model matrix (see model.matrix) of model.expl

X.resp The model matrix (see model.matrix) of model.resp

outc.resp The outcome of model.resp, a vector.

outc.expl The outcome of model.expl, a column matrix.

#### See Also

```
coefs.sensmed, maxLik
```

hess

Analytic Hessians of the loglikelihood functions for ML estimation of regression parameters

# **Description**

Implementation of the analytic Hessians of the loglikelihood functions for ML estimation of regression parameters for different combinations of exposure, mediator and outcome models. The functions are named according to the convention hess."model.expl type""model.resp type" where b stands for binary probit regression and c stands for linear regression.

```
hess.bb(
  par,
  Rho,
  X.expl = X.expl,
  X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)

hess.bc(
  par,
  Rho,
  X.expl = X.expl,
  X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)
```

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```
hess.cb(
  par,
  Rho,
  X.expl = X.expl,
  X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)
hess.cc(
  par,
  Rho,
  X.expl = X.expl,
  X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)
```

# Arguments

par	Vector of parameter values.
Rho	The value of the sensitivity parameter.
X.expl	The model matrix (see model.matrix) of model.expl
X.resp	The model matrix (see model.matrix) of model.resp
outc.resp	The outcome of model.resp, a vector.
outc.expl	The outcome of model.expl, a column matrix.

### See Also

```
{\tt coefs.sensmed, maxLik}
```

LogL	$Implementation\ of\ log likelihood\ functions\ for\ ML\ estimation\ of\ regression$
	sion parameters

# Description

Implementation of loglikelihood functions for ML estimation of regression parameters for different combinations of exposure, mediator and outcome models. The functions are named according to the convention LogL."model.expl type""model.resp type" where b stands for binary probit regression and c stands for linear regression.

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# Usage

```
LogL.bb(
  par,
  Rho,
  X.expl = X.expl,
  X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)
LogL.bc(
  par,
  Rho,
  X.expl = X.expl,
  X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)
LogL.cb(
  par,
  Rho,
  X.expl = X.expl,
  X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)
LogL.cc(
  par,
  Rho,
  X.expl = X.expl,
  X.resp = X.resp,
  outc.resp = outc.resp,
  outc.expl = outc.expl
)
```

# Arguments

par	Vector of parameter values.
Rho	The value of the sensitivity parameter.
X.expl	The model matrix (see model.matrix) of model.expl
X.resp	The model matrix (see model.matrix) of model.resp
outc.resp	The outcome of model.resp, a vector.
outc.expl	The outcome of model . expl. a column matrix.

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#### See Also

coefs.sensmed, maxLik

ML Functions for ML estimation of regression parameters for sensitivity analysis

#### **Description**

Functions for ML estimation of regression parameters for sensitivity analysis for different combinations of exposure, mediator and outcome models. The functions are named according to the convention ML."model.expl type""model.resp type" where b stands for binary probit regression and c stands for linear regression. The optimization is performed using maxLik. The functions are intended to be called through coefs.sensmed, not on their own.

#### Usage

```
ML.bb(model.expl, model.resp, Rho, progress = TRUE, ...)
ML.bc(model.expl, model.resp, Rho, progress = TRUE, ...)
ML.cb(model.expl, model.resp, Rho, progress = TRUE, ...)
ML.cc(model.expl, model.resp, Rho, progress = TRUE, ...)
```

### **Arguments**

model.expl	Fitted glm model object (probit or linear). If sensitivity analysis to mediator-outcome confounding the mediator model. Otherwise the exposure model.
model.resp	Fitted glm model object (probit or linear). If sensitivity analysis to exposure-mediator confounding the mediator model. Otherwise the outcome model.
Rho	The sensitivity parameter vector. If type="my" the correlation between the error terms in the mediator and outcome models. If type="zm" the correlation between the error terms in the exposure and mediator models. If type="zy" the correlation between the error terms in the exposure and outcome models.
progress	Logical, indicating whether or not the progress (i.e. the proc.time for each Rho) of the optimization will be output
•••	Additional arguments to be passed on to the maxLik function. Can be used to set the method and control arguments of the maxLik function.

#### Value

#### A list with elements:

coef

A matrix with the estimated regression parameters for model.resp over the range of Rho. One column per value of Rho.

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Rho	The sensitivity parameter vector.
expl.coef	A matrix with the estimated regression parameters for model.expl over the range of Rho. One column per value of Rho.
model.expl	the original fitted glm object of model.expl.
model.resp	the original fitted glm object of model.resp.
X.expl	The model matrix (see model.matrix) of model.expl
X.resp	The model matrix (see model.matrix) of model.resp
outc.resp	The outcome variable of model.resp.
outc.expl	The outcome variable of model.expl.
sigma.res.expl	If model.expl is linear, a column matrix with the estimated residual standard deviation for model.expl over the range of Rho.
sigma.res.resp	If model.resp is linear, a column matrix with the estimated residual standard deviation for model.resp over the range of Rho.
value	The values of the -loglikelihood function for the best set of regression parameters from the optimization for each Rho.
sigmas	A list with the covariance matrices for the model parameters in $model.expl$ and $model.resp$ for each Rho.
max.info	Information about the maximization (whether or not the convergence was successful, message, method and number of iterations) for each Rho, see maxLik for more information.

### Author(s)

Anita Lindmark

#### See Also

coefs.sensmed, maxLik

more.effects	Estimate additional natural direct and indirect effects based on an
	"effectsMed" object

# Description

Takes an "effectsMed" object and estimates additional natural direct and indirect effects, with a sensitivity analysis using the same sensitivity parameter as in the original analysis, without having to redo the optimization to find the estimated regression coefficients. The effects to be estimated are regulated through the arguments covariates, alt.decomposition, exp.value and control.value as described in the documentation for sensmediation. The confidence level used is regulated through the argument conf.level.

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#### Usage

```
more.effects(
   sensmed.object,
   conf.level = 0.95,
   covariates = NULL,
   alt.decomposition = FALSE,
   exp.value = NULL,
   control.value = NULL
)
```

#### Arguments

 $sensmed.object \ \ an \ object \ of \ class \ "effects Med" \ for \ which \ additional \ effects \ are \ to \ be \ calculated.$ 

conf.level the confidence level to be used for confidence intervals and uncertainty intervals.

covariates if conditional effects are to be estimated the list of covariate values (see sensmediation).

Covariates not specified are marginalized over.

alt.decomposition

logical indicating whether alternative definitions of the direct and indirect effects

should be used (see sensmediation).

exp. value value of the exposure variable used as the exposure condition, default is to take

the value stored in sensmed.object.

control.value value of the exposure variable used as the control (unexposed) condition, default

is to take the value stored in sensmed.object.

#### Value

more.effects returns an object of class "effectsMed", see the documentation for sensmediation for information.

## Author(s)

Anita Lindmark

#### See Also

sensmediation

### **Examples**

```
## Not run:
# Example with data from Riksstroke (the Swedish stroke register)
data(RSdata)
# Probit mediator and outcome models:
med.model <- glm(lowered.consc ~ AF + age.cat + sex, data = RSdata,
family = binomial(link = 'probit'))</pre>
```

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```
out.model <- glm(cf.3mo ~ AF + lowered.consc + age.cat + sex, data = RSdata,
 family = binomial(link = 'probit'))
 # First we estimate marginal NIE, NDE with sensitivity analyses to mediator-outcome
 # confounding:
 sensmed <- sensmediation(med.model, out.model, exp.name = "AF1", med.name = "lowered.consc",
 Rho = seq(0, 0.5, 0.1)
 # Then we also estimate NIE, NDE conditional on male sex without reestimating the regression
 # coefficients:
 sensmed.cond <- more.effects(sensmed.object = sensmed, covariates = list(sex = 1))</pre>
 summary(sensmed.cond)
 plot(sensmed.cond)
 ## End(Not run)
partdevs
                          Implementations of the partial derivatives (gradients) of the expres-
                          sions for the direct, indirect and total effects. Used to calculate stan-
                          dard errors (delta method).
```

# Description

Functions implementing the partial derivatives (gradients) of the expressions for the direct, indirect and total effects. These are then used to calculate standard errors of the effects using the delta method. Called by the stderrs functions. The functions are named according to the convention partdevs. "mediator model type" "outcome model type" where bstands for binary probit regression and c stands for linear regression.

```
partdevs.bb(
  beta0,
  beta1,
  beta2,
  beta3,
  theta0,
  theta1,
  theta2,
  theta3,
  theta4,
  theta5,
  theta6,
  theta7,
  x.med,
  x.out,
  t.de,
```

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```
t.ie,
  exp.value,
  control.value
)
partdevs.bc(
 beta0,
 beta1,
  beta2,
 beta3,
  theta2,
  theta3,
  theta6,
  theta7,
  x.med,
  x.out,
  t.de,
  t.ie,
  exp.value,
  control.value
)
partdevs.cb(
  beta0,
 beta1,
 beta2,
 beta3,
  theta0,
  theta1,
  theta2,
  theta3,
  theta4,
  theta5,
  theta6,
  theta7,
  sigma.eta,
  x.med,
  x.out,
  t.de,
  t.ie,
  exp.value,
  control.value
)
partdevs.cc(
  beta0,
  beta1,
```

beta2,

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```
beta3,
theta2,
theta3,
theta6,
theta7,
exp.value,
control.value,
x.med,
x.out,
t.de,
t.ie
)
```

# Arguments

beta0, beta1	Vectors of mediator regression parameters (intercept and exposure) over Rho
beta2, beta3	Matrices of mediator regression parameters (covariate main effects and exposure-covariate interactions) over Rho
theta0, theta1,	theta2, theta3
	Vectors of outcome regression parameters (intercept, exposure, mediator, exposure-mediator interaction) over Rho
theta4, theta5,	theta6, theta7
	Matrices of outcome regression parameters (covariate main effects, exposure-covariate, mediator-covariate and exposure-mediator-covariate interactions) over Rho
x.med	Mediator covariate matrix for which to calculate standard errors
x.out	Outcome covariate matrix for which to calculate standard errors
t.de, t.ie	exposure values used to calculate the direct and indirect effects depending on the desired decomposition (see the Details section of sensmediation for more information). If alt.decomposition = TRUE then t.de = exp.value and t.ie = control.value, otherwise t.de = control.value and t.ie = exp.value.
exp.value	value of the exposure variable used as the exposure condition.
control.value	value of the exposure variable used as the control (unexposed) condition.
sigma.eta	For a continuous mediator and binary outcome, matrix with the estimated residual standard deviation for the mediator model over the range of Rho.

plot.effectsMed
-----------------

Plot function for objects of class "effectsMed"

# Description

Plots the estimated natural indirect or direct effects with confidence intervals over the range of the sensitivity parameter Rho.

RSdata RSdata

### Usage

```
## S3 method for class 'effectsMed'
plot(
    x,
    effect = "indirect",
    xlab = NULL,
    ylab = NULL,
    xlim = NULL,
    ylim = NULL,
    main = NULL,
    lwd = graphics::par("lwd"),
    ...
)
```

### **Arguments**

X	object of class "effectsMed"
effect	which effect to plot results for ("indirect" or "direct")
xlab	a title for the x axis, see title. Default is expression(rho).
ylab	a title for the y axis, see title. Default is NIE (NIE* if alt.decomposition = TRUE) or NDE (NDE*)
xlim	the x limits $(x1, x2)$ of the plot, see plot. default. Default is $c(min(x\$Rho), max(x\$Rho))$
ylim	the y limits of the plot. Default is c(min(x\$CI\$CI.nie[,1]),max(x\$CI\$CI.nie[,2]))
main	a main title for the plot, see title
lwd	line widths for the lines of the plot, see par
	additional graphical parameters to be passed to plotting functions, see par

RSdata	Example data for the functions in sensmediation

# Description

The data are a subsample of 1000 observations from Riksstroke, the Swedish Stroke Register. The original data consisted of over 50 000 patients with first time ischemic stroke during the years 2009-2012. The data are limited to patients over the age of 44 and its purpose is to illustrate the functioning of the functions in the package.

```
data(RSdata)
```

#### **Format**

A data frame with 1000 observations on the following 5 variables.

```
cf. 3mo Outcome: case fatality within 3 months after stroke, 1 = deceased, 0 = not deceased.
```

lowered.consc Mediator: level of consciousness upon arrival to hospital. 1 = lowered consciousness, 0 = fully alert.

AF Exposure: atrial fibrillation. Factor with levels, "1" = atrial fibrillation, "0" = no atrial fibrillation.

```
age.cat Age at time of stroke. Factor with levels, "45-69", "70-79", "80-89" and "90-". sex Factor with levels, "1" = male, "0" = female
```

# **Examples**

```
data(RSdata)
```

sensmediation

Estimate natural direct and indirect effects based on parametric regression models and perform sensitivity analysis

#### **Description**

Function to estimate the natural direct and indirect effects based on parametric regression models. Standard errors for the effects are calculated using the delta method. The function also gives sensitivity analysis results for unobserved confounding. Implements methods introduced in Lindmark, de Luna and Eriksson (2018).

```
sensmediation(
 med.model,
 out.model,
  exp.model = NULL,
  exp.name = NULL,
 med.name = NULL,
  type = "my",
 Rho = 0,
  progress = TRUE,
  conf.level = 0.95,
  covariates = NULL,
  alt.decomposition = FALSE,
  control.value = 0,
  exp.value = 1,
  covariance = NULL,
 med.full = NULL,
 out.full = NULL,
  all.interactions = NULL,
)
```

# Arguments

med.model	Fitted glm model object representing the mediator model at the basis of the estimation (see Details for more information).
out.model	Fitted glm model object representing the outcome model at the basis of the estimation (see Details for more information).
exp.model	Fitted glm model object representing the exposure model. Should be provided if type="zm" or type="zy".
exp.name	A character string indicating the name of the exposure variable used in the models. Needs to match the name of the exposure found in the output from the fitted glm-models (this is especially important to check for exposures of class factor).
med.name	A character string indicating the name of the mediator used in the models. Needs to match the name of the mediator found in the output from the outcome glm-model (this is especially important to check for mediators of class factor).
type	the type of confounding for which the sensitivity analysis is to be performed. type="my", the default, corresponds to unobserved mediator-outcome confounding, type="zm" to exposure-mediator confounding and type="zy" to exposure-outcome confounding.
Rho	The sensitivity parameter vector. If type="my" the correlation between the error terms in the mediator and outcome models. If type="zm" the correlation between the error terms in the exposure and mediator models. If type="zy" the correlation between the error terms in the exposure and outcome models.
progress	Logical, indicating whether or not the progress (i.e. the proc.time for each Rho) of the optimization will be output
conf.level	the confidence level to be used for confidence intervals and uncertainty intervals.
covariates	if conditional effects are to be estimated the named list of covariate values (see Details). Covariates not specified are marginalized over.
alt.decomposit	ion
	logical indicating whether or not alternative definitions of the direct and indirect effects should be used (see Details).
control.value	value of the exposure variable used as the control (unexposed) condition, default is 0.
exp.value	value of the exposure variable used as the exposure condition, default is 1.
covariance, med	. full, out.full, all.interactions arguments used in previous versions of the package that are now deprecated.
	Additional arguments to be passed on to the maxLik function. Can be used to set the method and control arguments of the maxLik function (see coefs.sensmed).

# **Details**

To obtain the ML estimates of the regression parameters used to calculate mediation effects and perform sensitivity analysis sensmediation calls coefs.sensmed. The maximization of the log-likelihood is performed using maxLik, the default is to use the Newton-Raphson method and an analytic gradient and Hessian.

The mediator and outcome models (and exposure model for type = "zm" or "zy") should be fitted using glm and can be of two types, probit models (family = binomial(link = 'probit')) for binary mediators or outcomes (exposures) and linear regression models (family = gaussian) for continuous mediators or outcomes (exposures). Note that the exposure can either be binary or continuous, categorical exposures with more than two levels are not currently supported. The outcome model may contain exposure-mediator, exposure-covariate, mediator-covariate and exposure-mediator-covariate interactions. The mediator model may contain exposure-covariate interactions. All models may also contain interactions between covariates. Note, however that interactions may not be included in a model without also including the main effects of the interacting variables. That is, interactions should be specified either as X1\*X2 or X1 + X2 + X1:X2, not as X1:X2 alone.

To obtain results conditional on specific covariate values, these values should be provided through the covariates argument as a named list (see Examples). The effects will be averaged over covariates not specified in the list.

The total effect can be decomposed into a direct and indirect effect in different ways. Let z be the exposure value and  $z^*$  the control (unexposed) value. The default is to give the decomposition into the "pure direct effect"  $E(Y(z,M(z^*)))-E(Y(z^*,M(z^*)))$  (here denoted NDE) and the "total indirect effect"  $E(Y(z,M(z)))-E(Y(z,M(z^*)))$  (denoted NIE). Setting alt. decomposition=TRUE instead gives the decomposition into the "total direct effect"  $E(Y(z,M(z)))-E(Y(z^*,M(z)))$  (here denoted NDE\*) and "pure indirect effect"  $E(Y(z^*,M(z)))-E(Y(z^*,M(z^*)))$  (denoted NIE\*).

Standard errors for the effects are calculated using the delta method. Confidence intervals (CI) for (and p-values for tests of) the natural direct and indirect effects for each value of the sensitivity parameter are constructed based on a normal approximation. Uncertainty intervals (UI) are constructed as the union of all CIs over the sensitivity parameter vector.

#### Value

call

UI

sensmediation returns an object of class "effectsMed".

The matched call

The function summary (summary.effectsMed) gives a summary of the results in the form of a table with the estimated effects and results of the sensitivity analysis. The function plot (plot.effectsMed) plots the estimated natural indirect or direct effects with confidence intervals over the range of the sensitivity parameter.

Rho	The sensitivity parameter vector.
type	character, the type of confounding the sensitivity analysis is performed for.
coefs.sensmed	a list with the output from coefs.sensmed
NIE	matrix with the estimated NIEs (or NIE*s if alt.decomposition=TRUE) over the range of the sensitivity parameter Rho.
NDE	matrix with the estimated NDEs (or NDE*s if alt.decomposition=TRUE) over the range of the sensitivity parameter Rho.
std.errs	list with the standard errors of the NIE (NIE*), NDE (NDE*) and total effect over the range of the sensitivity parameter Rho.
CI	a list with the confidence intervals of the NIE (NIE*), NDE (NDE*) and total effect over the range of the sensitivity parameter Rho.

matrix with the uncertainty intervals for the NIE (NIE\*) and NDE (NDE\*) over

the range of the sensitivity parameter Rho.

conf.level numeric, the confidence level used for confidence intervals and uncertainty in-

tervals.

covariates list of the covariate values that the effects are conditioned on.

exp. name character vector containing the name of the exposure variable.

med.name character vector containing the name of the mediator variable.

exp.value value of the exposure variable used as the exposure condition.

control.value value of the exposure variable used as the control (unexposed) condition.

alt.decomposition

logical, indicating whether the alternative definitions of the direct and indirect

effects have been used

med.model the mediator model input.

out.model the outcome model input.

betas list of the estimated mediator model parameters over Rho, with

• beta0 Intercept

• beta1 Exposure

• beta2 Covariates

• beta3 Exposure-covariate interactions

Components that are not included in the input mediator model are set to 0.

thetas list of the estimated outcome model parameters over Rho, with

• theta0 Intercept

• theta1 Exposure

• theta2 Mediator

• theta3 Exposure-mediator interaction

• theta4 Covariates

• theta5 Exposure-covariate interactions

• theta6 Mediator-covariate interactions

• theta7 Exposure-mediator-covariate interactions

Components that are not included in the input outcome model are set to 0.

part.deriv List with the partial derivatives of the NDE (Lambda), NIE (Gamma) and TE

(Eta) wrt the mediator and outcome model parameters for each value of Rho.

See partdevs.

sigma.thetabeta

a list with the joint covariance matrix of the outcome and mediator model parameters for each value of Rho. Note that the covariance matrix is constructed for all estimated parameters listed in betas and thetas but that components not included in the input mediator and outcome models are set to 0.

#### Author(s)

Anita Lindmark

#### References

Lindmark, A., de Luna, X., Eriksson, M. (2018) Sensitivity Analysis for Unobserved Confounding of Direct and Indirect Effects Using Uncertainty Intervals, *Statistics in Medicine*, **37(10)**, pp 1744–1762, doi:10.1002/sim.7620.

Lindmark A (2022). Sensitivity analysis for unobserved confounding in causal mediation analysis allowing for effect modification, censoring and truncation. *Statistical Methods & Applications*, **31**, pp 785–814, doi:10.1007/s10260-021-00611-4.

#### See Also

more.effects which can be used to calculate additional direct and indirect effects with sensitivity analysis using the same sensitivity parameter without running the optimization again.

### **Examples**

```
# Example with data from Riksstroke (the Swedish stroke register)
data(RSdata)
# Probit mediator and outcome models:
m.model <- glm(lowered.consc ~ AF + age.cat + sex, data = RSdata,</pre>
   family = binomial(link = 'probit'))
o.model <- glm(cf.3mo ~ AF + lowered.consc + age.cat + sex, data = RSdata,
   family = binomial(link = 'probit'))
# Estimation of NIE, NDE and sensitivity analyses to mediator-outcome confounding:
# (note that the name of the exposure is "AF1" to match the name in coef(out.model))
sensmed <- sensmediation(m.model, o.model, exp.name = "AF1", med.name = "lowered.consc",</pre>
   Rho = c(0, 0.1)
summary(sensmed)
plot(sensmed)
plot(sensmed, effect = "direct")
## Not run:
# Conditional effects and sensitivity analysis to mediator-outcome confounding using
# more.effects():
sensmed.cond <- more.effects(sensmed.object = sensmed,</pre>
   covariates = list(sex = 1, age.cat = "70-79"))
summary(sensmed.cond)
## End(Not run)
## Not run:
## Sensitivity analysis to exposure-mediator confounding:
  e.model <- glm(AF ~ age.cat + sex, data = RSdata,
     family = binomial(link = 'probit'))
  sensmed.zm <- sensmediation(med.model = m.model, out.model = o.model,</pre>
     exp.model = e.model, type = "zm", Rho = seq(0, 0.5, 0.1), exp.name = "AF1",
     med.name = "lowered.consc")
```

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```
summary(sensmed.zm)
## End(Not run)
## Not run:
# Additional effects using more.effects:
# Results with conf.level = 0.99:
sensmed.zm.99 <- more.effects(sensmed.object = sensmed.zm, conf.level = 0.99)</pre>
summary(sensmed.zm.99)
## End(Not run)
## Not run:
# Examples with simulated data, continuous exposure:
require(mvtnorm)
n <- 1000
set.seed(102677)
x <- rnorm(n)</pre>
z < -0.5 + 0.1*x + rnorm(n)
R <- 0.5
Sigma <- cbind(c(1,R), c(R,1))
epsilon <- rmvnorm(n, sigma = Sigma)</pre>
m < -1.2 + 0.8*z + 0.13*x + epsilon[,1]
y < -1 + 0.05*z + 3*m + 0.5*x + epsilon[,2]
# Models:
z.model \leftarrow glm(z \sim x)
m.model2 \leftarrow glm(m \sim z + x)
y.model \leftarrow glm(y \sim z + m + x)
## Estimation of NIE, NDE. Note that the exposure condition is 2
## so effects are calculated for a 2 unit increase of the exposure:
eff.contz <- sensmediation(med.model = m.model2, out.model = y.model,</pre>
            exp.name = "z", med.name = "m", control.value = 0, exp.value = 2)
summary(eff.contz)
## End(Not run)
```

stderrs

Functions to calculate standard errors of the direct, indirect and total effects using the delta method.

#### **Description**

Functions used to calculate standard errors of the direct, indirect and total effects using the delta method. Called by calc.effects. The functions are named according to the convention stderr."mediator

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model type" "outcome model type" where b stands for binary probit regression and c stands for linear regression.

```
stderr.bb(
 Rho,
 betas,
  thetas,
  sigma.pars,
 x.med,
 x.out,
 alt.decomposition,
  exp.value,
 control.value
)
stderr.bc(
 Rho,
 betas,
  thetas,
  sigma.pars,
  x.med,
  x.out,
  alt.decomposition,
 exp.value,
  control.value
)
stderr.cb(
 Rho,
 betas,
  thetas,
  sigma.eta,
  sigma.pars,
  x.med,
 x.out,
 alt.decomposition,
 exp.value,
  control.value
)
stderr.cc(
 Rho,
 betas,
  thetas,
  sigma.pars,
  x.med,
  x.out,
```

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```
alt.decomposition,
  exp.value,
  control.value
)
```

# Arguments

Rho The sensitivity parameter vector.

betas List of mediator regression parameters
thetas List of outcome regression parameters

sigma.pars List of covariance matrices for the mediator and outcome regression parameters

x.med Mediator covariate matrix for which to calculate standard errorsx.out Outcome covariate matrix for which to calculate standard errors

alt.decomposition

logical indicating whether or not alternative definitions of the direct and indirect

effects should be used.

exp. value value of the exposure variable used as the exposure condition.

control.value value of the exposure variable used as the control (unexposed) condition.

sigma.eta For a continuous mediator and binary outcome, matrix with the estimated resid-

ual standard deviation for the mediator model over the range of Rho.

summary.effectsMed

Summary function for objects of class "effectsMed"

#### **Description**

Summary function for objects of class "effectsMed"

#### Usage

```
## S3 method for class 'effectsMed'
summary(object, non.sign = FALSE, ...)
## S3 method for class 'summaryeffectsMed'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

# **Arguments**

object of class "effectsMed"

non.sign logical indicating whether sensitivity analysis results should be printed for non-

significant effects.

... additional arguments

x object of class "summaryeffectsMed"

digits number of digits to be printed.

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#### Value

#### A list with values:

call The matched call

Rho The sensitivity parameter vector.

type character, the type of confounding the sensitivity analysis is performed for.

conf.level numeric, the confidence level used for confidence intervals and uncertainty in-

tervals.

UI matrix with the uncertainty intervals for the NIE (NIE\*) and NDE (NDE\*) over

the range of the sensitivity parameter Rho.

covariates list of the covariate values that the effects are conditioned on.

exp.name character vector containing the name of the exposure.

med.name character vector containing the name of the mediator.

alt.decomposition

logical, indicating whether the alternative definitions of the direct and indirect

effects have been used

non.sign logical indicating whether sensitivity analysis results are printed for non-significant

effects.

effects Results of the mediation analysis. Estimated NIE and NDE with confidence

intervals and p-values for Rho = 0

ns.nie values of Rho with estimated NIEs and confidence intervals where the NIE is not

significant.

ns.nde values of Rho with estimated NDEs and confidence intervals where the NDE is

not significant.

rev.nie values of Rho with estimated NIEs and confidence intervals where the NIE is

reversed.

rev.nde values of Rho with estimated NDEs and confidence intervals where the NDE is

reversed.

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