Package 'spGARCH'

July 23, 2025

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Description

The function extracts the log-likelihood of a spatial ARCH model.

Usage

```
## S3 method for class 'spARCH'
extractAIC(fit, scale, k = 2, ...)
```

Arguments

fit spARCH object (fitted model resulting of qml.spARCH).

scale currently unused for spARCH objects.

k parameter specifying the weight for the penalizing term.

... Other arguments.

Details

Numeric vector of length 2 is returned. The first element specify the edf (equivalent degree of freedom) and the Akaike information criterion is returned as second element.

Author(s)

Philipp Otto <philipp.otto@glasgow.ac.uk>

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fitted.spARCH

Extract model fitted values

Description

The function extracts the fitted values of a spatial ARCH model.

Usage

```
## S3 method for class 'spARCH'
## S3 method for class 'spARCH'
fitted(object, ...)
```

Arguments

```
object spARCH object generated by qml.spARCH or qml.SARspARCH.
... Other arguments.
```

Details

Fitted values extracted from the object.

Author(s)

```
Philipp Otto <philipp.otto@glasgow.ac.uk>
```

See Also

```
residuals.spARCH, logLik.spARCH.
```

logLik.spARCH

Extract logarithmic likelihood

Description

The function extracts the log-likelihood of a spatial ARCH model.

Usage

```
## S3 method for class 'spARCH'
## S3 method for class 'spARCH'
logLik(object, ...)
```

Arguments

```
object spARCH Object of qml.spARCH.
... Other arguments.
```

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Details

logLik object is returned.

Author(s)

Philipp Otto <philipp.otto@glasgow.ac.uk>

See Also

```
residuals.spARCH, fitted.spARCH.
```

plot.spARCH

Descriptive plots for residuals of a fitted spatial ARCH model

Description

The function depicts several descriptive statistics of the residuals of a fitted spatial ARCH model.

Usage

```
## S3 method for class 'spARCH'
## S3 method for class 'spARCH'
plot(x, which = c(1:3), ask, ..., qqline = TRUE)
```

Arguments

Х	spARCH object generated by qml.spARCH or qml.SARspARCH.
which	Index number of plot to be returned.
ask	if TRUE, the user is asked before plotting the next figure.
	Other arguments.
qqline	A line of the normal distribution for comparison is added to the Q-Q plot, if ggline = TRUE.

Details

The function plot.spARCH provides several descriptive plots to analyze the residuals of a fitted spatial ARCH model, namely (1) Moran's plot for residuals, (2) Moran's plot for squared residuals, and (3) Normal Q-Q plot for standardized residuals.

Note

```
For details of moran.plot see: help(moran.plot).
```

Author(s)

```
Philipp Otto <philipp.otto@glasgow.ac.uk>
```

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prostate_cancer

Logarithmic incidence rates of prostate cancer and covariates

Description

The dataset contains logarithmic incidence rates from the National Cancer Institute and Centers for Disease, Control and Prevention (State Cancer Profiles) and factor loadings of a set of covariates. The incidence rates are 5-year averages from 2008 to 2012 in several southeastern states (Arkansas, Louisiana, Mississippi, Tennessee, North and South Carolina, Georgia, Alabama, and Florida). Missing values were imputed by spatial averaging.

Usage

```
data("prostate_cancer")
```

Format

A list with three entries:

data a data frame; see below for details

B a numeric matrix; weighting matrix B to run the example

W a numeric matrix; weighting matrix W to run the example

The data frame contains 755 observations of the following 12 variables.

log_incidence_rates a numeric vector; logarithmic incidence rates of prostate cancer

F₁ a numeric vector; scores of factor 1 (environment: fine atmospheric particles and aerosols)

F_2 a numeric vector; scores of factor 2 (environment: particulate matter)

F_3 a numeric vector; scores of factor 3 (weather: solar radiation and temperature)

F_4 a numeric vector; scores of factor 4 (weather: temperature differences)

F_5 a numeric vector; scores of factor 5 (behavior: smoking)

F_6 a numeric vector; scores of factor 6 (behavior: drinking)

F_7 a numeric vector; scores of factor 7 (behavior: preventive health care)

F_8 a numeric vector; scores of factor 8 (behavior: physical activity)

F_9 a numeric vector; scores of factor 9 (health: overweight)

F_10 a numeric vector; scores of factor 10 (health: cholesterol and blood pressure)

PSA_test a numeric vector; percentage of positive results for a prostate-specific antigen (PSA) test

Source

https://statecancerprofiles.cancer.gov/index.html

National Cancer Institute, Centers for Disease, Control and Prevention

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References

https://statecancerprofiles.cancer.gov/map/map.withimage.php?99&001&001&00&0&0&0&1&10 Otto, P. (2019). spGARCH: An R-Package for Spatial and Spatiotemporal ARCH and GARCH models To appear: The R Journal URL: https://arxiv.org/abs/1812.01871

Examples

qml.SARspARCH

Maximum-likelihood estimation of a spatial autoregressive model with spatial ARCH residuals

Description

The function fits a spatial autoregressive model with spatial ARCH residuals using the maximum-likelihood approach. All parameters are jointly estimated. In addition, external regressor may be included in the mean equation.

Usage

Arguments

formula	an object of class "formula"): a symbolic description of the model to be fitted.
	The details of model specification are given under "Details." y must be a numeric
	vector of length n (dimension of the weighting matrix)
В	n times n spatial weight matrix for the spatial autoregressive part
W	n times n spatial weight matrix for the spatial ARCH residuals
type	type of spatial ARCH model to be fitted for the error process (see Details)

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data	an optional data frame, list or environment containing the variables in the model. If not found in data, the variables are taken from the working space.
b	parameter b for the E-spARCH model (type = "exp"), must be a (positive) natural number
start	vector of starting values for the numerical optimization of the log-likelihood (optional)
eigen_v	eigen values of B (optional)
control	list of control variables for iterative maximization of the log-likelihood

Details

For type = "spARCH", the functions fits a simple spatial autoregressive model with spatial ARCH residuals, i.e.,

$$Y = \lambda \mathbf{B} Y + \mathbf{X} \boldsymbol{\beta} + \boldsymbol{h}^{1/2} \boldsymbol{\varepsilon}$$

with

$$\boldsymbol{h} = \alpha \mathbf{1}_n + \rho \mathbf{W} \boldsymbol{Y}^{(2)} \,.$$

The distribution of the error term is assumed to be Gaussian.

If type = "log-ARCH", a spatial log-ARCH process is estimated for the error term, i.e.,

$$\ln(\mathbf{h}) = \alpha \mathbf{1}_n + \rho \mathbf{W} g_b(\boldsymbol{\varepsilon}) \,.$$

The function g_b is defined as

$$g_b(\boldsymbol{\varepsilon}) = (\ln |\varepsilon(\boldsymbol{s}_1)|^b, \dots, \ln |\varepsilon(\boldsymbol{s}_n)|^b)'$$

and the error term is also assumed to be Gaussian.

The modelling equation gan be specified as for lm, i.e., as formula object. A typical model has the form response ~ terms where response is the (numeric) response vector and terms is a series of terms which specifies a linear predictor for response. A terms specification of the form first + second indicates all the terms in first together with all the terms in second with duplicates removed. A specification of the form first:second indicates the set of terms obtained by taking the interactions of all terms in first with all terms in second. The specification first*second indicates the cross of first and second. This is the same as first + second + first:second. However, there is no offset permitted for the qml.SARspARCH.

For an intercept-only model, the formula can be specified as response \sim 1. In addition, it is possible to fit an intercept-free model with response \sim 0 or response \sim 0 + terms.

To summarize the results of the model fit, use the generic function summary. For analysis of the residuals, the generic plot. spARCH function provides several descriptive plots. For numerical maximization of the log-likelihood, the function uses the algorithm of solnp from the package Rsolnp.

Value

A spARCH object with the following elements is returned:

coefficients Parameter estimates α and ρ .

residuals Vector of residuals.

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fitted.values Fitted values.

stderr Standard errors of the estimates (Cramer-Rao estimates).

hessian Hessian matrix of the negative Log-Likelihood at the estimated minimum.

LL Value of the Log-Likelihood at the estimated maximum.

h Fitted vector h.

y Vector of observations (input values).

h Chosen type (input).

B Spatial weight matrix (input).
W Spatial weight matrix (input).

regressors Are regressors included? TRUE/FALSE

AR Is an autoregressive term in the mean equation? TRUE/FALSE

X Matrix of regressors if regressor = TRUE

Control Arguments

see also: solnp

- rho This is used as a penalty weighting scalar for infeasibility in the augmented objective function. The higher its value the more the weighting to bring the solution into the feasible region (default 1). However, very high values might lead to numerical ill conditioning or significantly slow down convergence.
- outer.iter Maximum number of major (outer) iterations (default 400).
- inner.iter Maximum number of minor (inner) iterations (default 800).
- delta Relative step size in forward difference evaluation (default 1.0e-7).
- tol Relative tolerance on feasibility and optimality (default 1e-8).
- trace The value of the objective function and the parameters is printed at every major iteration (default 1).

Author(s)

Philipp Otto <philipp.otto@glasgow.ac.uk>

References

Philipp Otto, Wolfgang Schmid, Robert Garthoff (2018). Generalised Spatial and Spatiotemporal Autoregressive Conditional Heteroscedasticity. Spatial Statistics 26, pp. 125-145. doi:10.1016/j.spasta.2018.07.005, arXiv: doi:10.48550/arXiv.1609.00711

See Also

solnp (package Rsolnp)

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Examples

```
require("spdep")
rho <- 0.5
alpha <- 1
lambda <- 0.5
d <- 5
n <- d^2
nblist <- cell2nb(d, d, type = "queen")</pre>
W <- nb2mat(nblist)</pre>
B <- W
X <- cbind(rep(1, n), rnorm(n))</pre>
beta <- c(5, 2)
y <- solve(diag(n) - lambda * B) %*%
    (sim.spARCH(n = n, rho = rho, alpha = alpha, W = W, type = "log-spARCH") + X %*% beta)
y <- as.vector(y)</pre>
out <- qml.SARspARCH(y ~ X[,2], B = B, W = W, type = "log-spARCH")
summary(out)
```

qml.spARCH

Maximum-likelihood estimation of a spatial ARCH model

Description

The function fits a spatial ARCH model using the maximum-likelihood approach. In addition, external regressor may be included in the mean equation.

Usage

Arguments

formula	an object of class "formula"): a symbolic description of the model to be fitted. The details of model specification are given under "Details."" y must be a numeric vector of length n (dimension of the weighting matrix)
W	n times n spatial weight matrix
type	type of spatial ARCH model to be fitted (see Details)
data	an optional data frame, list or environment containing the variables in the model. If not found in data, the variables are taken from the working space.
b	parameter b for the E-spARCH model (type = "exp"), must be a (positive) natural number
start	vector of starting values for the numerical optimization of the log-likelihood (optional)
control	list of control variables for iterative maximization of the log-likelihood

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Details

For type = "spARCH", the functions fits a simple spatial ARCH model with one spatial lag, i.e.,

$$Y = X\beta + h^{1/2}\varepsilon$$

with

$$\boldsymbol{h} = \alpha \mathbf{1}_n + \rho \mathbf{W} \boldsymbol{Y}^{(2)} \,.$$

The distribution of the error term is assumed to be Gaussian.

If type = "log-spARCH", a spatial log-ARCH process is estimated, i.e.,

$$\ln(\mathbf{h}) = \alpha \mathbf{1}_n + \rho \mathbf{W} q_b(\boldsymbol{\varepsilon}) \,.$$

The function g_b is defined as

$$g_b(\boldsymbol{\varepsilon}) = (\ln |\varepsilon(\boldsymbol{s}_1)|^b, \dots, \ln |\varepsilon(\boldsymbol{s}_n)|^b)'$$

and the error term is also assumed to be Gaussian.

The modelling equation gan be specified as for lm, i.e., as formula object. A typical model has the form response ~ terms where response is the (numeric) response vector and terms is a series of terms which specifies a linear predictor for response. A terms specification of the form first + second indicates all the terms in first together with all the terms in second with duplicates removed. A specification of the form first: second indicates the set of terms obtained by taking the interactions of all terms in first with all terms in second. The specification first*second indicates the cross of first and second. This is the same as first + second + first: second. However, there is no offset permitted for the qml.spARCH.

For an intercept-only model, the formula can be specified as response ~ 1. In addition, it is possible to fit an intercept-free model with response ~ 0 or response ~ 0 + terms.

To summarize the results of the model fit, use the generic function summary. For analysis of the residuals, the generic plot provides several descriptive plots. For numerical maximization of the log-likelihood, the function uses the algorithm of solnp from the package Rsolnp.

Value

A spARCH object with the following elements is returned:

coefficients Parameter estimates α and ρ .

residuals Vector of residuals. fitted.values Fitted values.

stderr Standard errors of the estimates (Cramer-Rao estimates).

hessian Hessian matrix of the negative Log-Likelihood at the estimated minimum.

Value of the Log-Likelihood at the estimated maximum.

h Fitted vector h.

y Vector of observations (input values).

h Chosen type (input).

W Spatial weight matrix (input).

regressors included? TRUE/FALSE

AR Is an autoregressive term in the mean equation? TRUE/FALSE

X Matrix of regressors if regressor = TRUE

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Control Arguments

```
see also: solnp
```

 rho - This is used as a penalty weighting scalar for infeasibility in the augmented objective function. The higher its value the more the weighting to bring the solution into the feasible region (default 1). However, very high values might lead to numerical ill conditioning or significantly slow down convergence.

- outer.iter Maximum number of major (outer) iterations (default 400).
- inner.iter Maximum number of minor (inner) iterations (default 800).
- delta Relative step size in forward difference evaluation (default 1.0e-7).
- tol Relative tolerance on feasibility and optimality (default 1e-8).
- trace The value of the objective function and the parameters is printed at every major iteration (default 1).

Author(s)

```
Philipp Otto <philipp.otto@glasgow.ac.uk>
```

References

Philipp Otto, Wolfgang Schmid, Robert Garthoff (2018). Generalised Spatial and Spatiotemporal Autoregressive Conditional Heteroscedasticity. Spatial Statistics 26, pp. 125-145. doi:10.1016/j.spasta.2018.07.005, arXiv: doi:10.48550/arXiv.1609.00711

See Also

```
solnp (package Rsolnp)
```

Examples

```
require("spdep")

# directional spatial ARCH process (W is triangular, 1:1 origin)

rho <- 0.5
alpha <- 1
d <- 5
n <- d^2
nblist <- cell2nb(d, d, type = "queen")
W <- nb2mat(nblist)
W[lower.tri(W)] <- 0
y <- sim.spARCH(n = n, rho = rho, alpha = alpha, W = W, type = "spARCH")

out <- qml.spARCH(y ~ 0, W = W, type = "spARCH")

summary(out)</pre>
```

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residuals.spARCH

Extract model residuals

Description

The function extracts the residuals of a fitted spatial ARCH model.

Usage

```
## S3 method for class 'spARCH'
## S3 method for class 'spARCH'
residuals(object, ...)
```

Arguments

object spARCH object generated by qml.spARCH or qml.SARspARCH.
... Other arguments.

Details

The function extracts the residuals of a fitted spatial ARCH model.

Author(s)

```
Philipp Otto <philipp.otto@glasgow.ac.uk>
```

See Also

```
residuals.spARCH, fitted.spARCH.
```

sim.spARCH

Simulation of spatial ARCH models

Description

The function generates n random numbers of a spatial ARCH process for given parameters and weighting schemes.

Usage

```
sim.spARCH(n = dim(W)[1], rho, alpha, W, b = 2, type = "spARCH", control = list())
```

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Arguments

n	number of observations. If length(n) > 1, the length is taken to be the number required. Default $dim(W)[1]$
rho	spatial dependence parameter rho
alpha	unconditional variance level alpha
W	n times n spatial weight matrix
b	parameter b for logarithmic spatial ARCH (only needed if type = "log-spARCH"). Default 2.
type	type of simulated spARCH process (see details)
control	list of control arguments (see below)

Details

The function simulates n observations $Y = (Y_1, ..., Y_n)'$ of a spatial ARCH process, i.e.,

$$Y = diag(h)^{1/2} \varepsilon$$
,

where ε is a spatial White Noise process. The definition of h depends on the chosen type. The following types are available.

• type = "spARCH" - simulates ε from a truncated normal distribution on the interval [-a,a], such that h>0 with

$$h = \alpha + \rho W Y^{(2)}$$
 and $a = 1/||\rho^2 W^2||_1^{1/4}$.

Note that the normal distribution is not trunctated $(a = \infty)$, if **W** is a strictly triangular matrix, as it is ensured that h > 0. Generally, it is sufficient that if there exists a permutation such that **W** is strictly triangular. In this case, the process is called oriented spARCH process.

• type = "log-spARCH" - simulates a logarithmic spARCH process (log-spARCH), i.e.,

$$\ln \mathbf{h} = \alpha + \rho \mathbf{W} g(\boldsymbol{\varepsilon}).$$

For the log-spARCH process, the errors follow a standard normal distribution. The function g_b is given by

$$g_b(\boldsymbol{\varepsilon}) = (\ln |\varepsilon(\boldsymbol{s}_1)|^b, \dots, \ln |\varepsilon(\boldsymbol{s}_n)|^b)'.$$

• type = "complex-spARCH" - allows for complex solutions of $m{h}^{1/2}$ with

$$\boldsymbol{h} = \alpha + \rho \mathbf{W} \boldsymbol{Y}^{(2)} \,.$$

The errors follow a standard normal distribution.

Value

The functions returns a vector y.

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Control Arguments

- seed positive integer to initialize the random number generator (RNG), default value is a random integer in $[1,10^6]$
- silent if FALSE, current random seed is reported
- ullet triangular if TRUE, old W is a triangular matrix and there are no checks to verify this assumption (default FALSE)

Author(s)

```
Philipp Otto <philipp.otto@glasgow.ac.uk>
```

References

Philipp Otto, Wolfgang Schmid, Robert Garthoff (2018). Generalised Spatial and Spatiotemporal Autoregressive Conditional Heteroscedasticity. Spatial Statistics 26, pp. 125-145. doi:10.1016/j.spasta.2018.07.005, arXiv: doi:10.48550/arXiv.1609.00711

Examples

```
require("spdep")
# 1st example
###############
# parameters
rho <- 0.5
alpha <- 1
d <- 2
nblist <- cell2nb(d, d, type = "queen")</pre>
W <- nb2mat(nblist)</pre>
# simulation
Y <- sim.spARCH(rho = rho, alpha = alpha, W = W, type = "log-spARCH")
# visualization
image(1:d, 1:d, array(Y, dim = c(d,d)), xlab = expression(s[1]), ylab = expression(s[2]))
# 2nd example
###############
# two spatial weighting matrices W_1 and W_2
# h = alpha + rho_1 W_1 Y^2 + rho_2 W_2 Y^2
W_{1} < - W
nblist <- cell2nb(d, d, type = "rook")</pre>
W_2 <- nb2mat(nblist)</pre>
```

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```
rho_1 <- 0.3
rho_2 <- 0.7

W <- rho_1 * W_1 + rho_2 * W_2
rho <- 1

Y <- sim.spARCH(n = d^2, rho = rho, alpha = alpha, W = W, type = "log-spARCH")
image(1:d, 1:d, array(Y, dim = c(d,d)), xlab = expression(s[1]), ylab = expression(s[2]))</pre>
```

sim.spGARCH

Simulation of spatial ARCH models

Description

The function generates n random numbers of a spatial GARCH process for given parameters and weighting schemes.

Usage

Arguments

n	number of observations. If $length(n) > 1$, the length is taken to be the number required. Default $dim(W1)[1]$
rho	spatial dependence parameter rho
lambda	spatial dependence parameter lambda
alpha	unconditional variance level alpha
W1	n times n spatial weight matrix (ARCH component, parameter rho)
W2	n times n spatial weight matrix (GARCH component, parameter lambda)
b	parameter b for logarithmic spatial GARCH (only needed if type = "log-spGARCH"). Default 2.
zeta	parameter zeta for exponential spatial GARCH (only needed if type = "e-spGARCH"). Default 0.5.
theta	parameter theta for exponential spatial GARCH (only needed if type = "e-spGARCH"). Default 0.5 .
type	type of simulated spGARCH process (see details)
control	list of control arguments (see below)

sim.spGARCH

Details

The function simulates n observations $Y = (Y_1, ..., Y_n)'$ of a spatial GARCH process, i.e.,

$$Y = diag(h)^{1/2} \varepsilon$$
,

where ε is a spatial White Noise process. The definition of h depends on the chosen type. The following types are available.

• type = "spGARCH" - simulates ε from a truncated normal distribution on the interval [-a,a], such that h>0 with

$$h = \alpha + \rho \mathbf{W}_1 \mathbf{Y}^{(2)} + \lambda \mathbf{W}_2 h$$
 and $a = 1/||\rho^2 \mathbf{W}_1^2||_1^{1/4}$.

Note that the normal distribution is not trunctated $(a = \infty)$, if \mathbf{W}_1 is a strictly triangular matrix, as it is ensured that h > 0. Generally, it is sufficient that if there exists a permutation such that \mathbf{W}_1 is strictly triangular. In this case, the process is called oriented spGARCH process.

• type = "e-spGARCH" - simulates an exponential spARCH process (e-spGARCH), i.e.,

$$\ln \mathbf{h} = \alpha + \rho \mathbf{W}_1 g(\boldsymbol{\varepsilon}) + \lambda \mathbf{W}_2 log(\mathbf{h}).$$

For the e-spGARCH process, the errors follow a standard normal distribution. The function g is given by

$$g(\varepsilon) = \Theta\varepsilon + \zeta(|\varepsilon| - E(|\varepsilon|)).$$

• type = "log-spGARCH" - simulates a logarithmic spARCH process (log-spGARCH), i.e.,

$$\ln \mathbf{h} = \alpha + \rho \mathbf{W}_1 g(\boldsymbol{\varepsilon}) + \lambda \mathbf{W}_2 log(\mathbf{h}).$$

For the log-spGARCH process, the errors follow a standard normal distribution. The function g is given by

$$g(\boldsymbol{\varepsilon}) = (\ln |\varepsilon(\boldsymbol{s}_1)|^b, \dots, \ln |\varepsilon(\boldsymbol{s}_n)|^b)'.$$

• type = "complex-spGARCH" - allows for complex solutions of $m{h}^{1/2}$ with

$$\boldsymbol{h} = \alpha + \rho \mathbf{W}_1 \boldsymbol{Y}^{(2)} + \lambda \mathbf{W}_2 \boldsymbol{h}.$$

The errors follow a standard normal distribution.

Value

The functions returns a vector y.

Control Arguments

- seed positive integer to initialize the random number generator (RNG), default value is a random integer in $[1,10^6]$
- silent if FALSE, current random seed is reported
- ullet triangular if TRUE, f W is a triangular matrix and there are no checks to verify this assumption (default FALSE)

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Author(s)

Philipp Otto <philipp.otto@glasgow.ac.uk>

References

Philipp Otto, Wolfgang Schmid (2019). Spatial GARCH Models - A Unified Approach. arXiv: doi:10.48550/arXiv.1908.08320

Examples

```
require("spdep")
# 1st example (spatial GARCH)
##############
# parameters
rho <- 0.5
lambda <- 0.3
alpha <- 1
      <- 5
nblist <- cell2nb(d, d, type = "rook") # lattice process with Rook's contiguity matrix</pre>
W_1 <- nb2mat(nblist)</pre>
W_2
      <- W_1
# simulation
       <- sim.spGARCH(rho = rho, lambda = lambda, alpha = alpha,
                      W1 = W_1, W2 = W_2, type = "spGARCH")
# visualization
image(1:d, 1:d, array(Y, dim = c(d,d)), xlab = expression(s[1]), ylab = expression(s[2]))
# 2nd example (exponential spatial GARCH)
###############
# parameters
    <- 0.5
lambda <- 0.3
alpha <- 1
zeta <- 0.5
theta <- 0.5
      <- 5
nblist <- cell2nb(d, d, type = "rook") # lattice process with Rook's contiguity matrix</pre>
W_1
      <- nb2mat(nblist)
W_2
       <- W_1
# simulation
```

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```
Y <- sim.spGARCH(rho = rho, lambda = lambda, alpha = alpha,
	W1 = W_1, W2 = W_2, zeta = zeta, theta = 0.5, type = "e-spGARCH")
# visualization
image(1:d, 1:d, array(Y, dim = c(d,d)), xlab = expression(s[1]), ylab = expression(s[2]))
```

spARCH

Output of Quasi-Maximum-Likelihood Estimation

Description

The spARCH class is a class generated by the estimation functions qml.spARCH or qml.SARspARCH comprising the results of the quasi-maximum-likelihood estimation.

Methods

Several generic methods for summarizing the results are available:

```
plot.spARCH - Descriptive plots for residuals of a fitted spatial ARCH model
```

plot(spARCH_object) summary.spARCH-The function returns a summary of the model fit of a spatial ARCH model

fitted(spARCH_object) fitted.spARCH - The function extracts the fitted values of a spatial ARCH model.

spGARCH

spGARCH - Package to fit spatial ARCH models

Description

A collection of functions for simulating and fitting spatial autoregressive conditional heteroscedasticity (spARCH) processes are provided.

The functions sim.spARCH and sim.spGARCH are the main function for simulating spARCH and spGARCH processes, respectively. Via the argument type several types of spatial ARCH and GARCH can be simulated, e.g., exponential spARCH models, spARCH for oriented processes, or spARCH processes with truncated error support. For details, refer the paper Otto, Schmid, and Garthoff (2018), see doi:10.1016/j.spasta.2018.07.005. Moreover, the package provides function for fitting spARCH models. Basically, there are two functions to fit these kind of model: qml.spARCH and qml.spARCH. SARSpARCH. First, spARCH models can be fitted by qml.spARCH.

Author(s)

Philipp Otto <philipp.otto@glasgow.ac.uk>

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References

Philipp Otto, Wolfgang Schmid, Robert Garthoff (2018). Generalised Spatial and Spatiotemporal Autoregressive Conditional Heteroscedasticity. Spatial Statistics 26, pp. 125-145. doi:10.1016/j.spasta.2018.07.005, arXiv: doi:10.48550/arXiv.1609.00711

summary.spARCH Summary for spARCH object

Description

The function returns a summary of the model fit of a spatial ARCH model (qml.spARCH or qml.SARspARCH).

Usage

```
## S3 method for class 'spARCH'
summary(object, ...)
## S3 method for class 'summary.spARCH'
print(x, digits = max(5, .Options$digits - 3),
signif.stars = TRUE, ...)
## S3 method for class 'spARCH'
print(x, ...)
```

Arguments

```
object spARCH object generated by qml.spARCH or qml.SARspARCH.

digits The number of significant digits to be printed.

signif.stars Logical variable. If TRUE, significance stars are printed for each coefficient.

x spARCH object of qml.spARCH.

further arguments passed to or from other methods
```

Details

The function summary.spARCH returns an spARCH object with all results (coefficients, residuals, diagnostic checks etc.). If the returned object is printed, a detailed summary of the model fit is returned.

Value

The function returns the input spARCH object, plus

I, moran.test).

Coef a matrix with columns for the estimated coefficients, their standard error, tstatistics and corresponding (two-sided, asymptotic) p-values.

AIC Akaike information criterion

BIC Bayesian Schwarz information criterion

moran_res Test on spatial spatial autocorrelation of the residuals (based on Morans I, moran_test).

Test on spatial spatial autocorrelation of the squared residuals (based on Morans

20 summary.spARCH

Note

For further details about the Moran's I test see moran. test.

Author(s)

```
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```

See Also

The model fitting functions qml.spARCH and qml.SARspARCH. Function coef will extract the matrix of coefficients with standard errors, t-statistics and p-values.

Examples

```
require("spdep")
# directional spatial ARCH process (W is triangular, 1:1 origin)

rho <- 0.5
alpha <- 1
d <- 5
n <- d^2
nblist <- cell2nb(d, d, type = "queen")
W <- nb2mat(nblist)
W[lower.tri(W)] <- 0
y <- sim.spARCH(n = n, rho = rho, alpha = alpha, W = W, type = "spARCH")

out <- qml.spARCH(y ~ 0, W = W, type = "spARCH")

summary(out)</pre>
```

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