

# Package ‘trotter’

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**Type** Package

**Title** Pseudo-Vectors Containing All Permutations, Combinations and Subsets of Objects Taken from a Vector.

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**Description** Class definitions and constructors for pseudo-vectors containing all permutations, combinations and subsets of objects taken from a vector. Simplifies working with structures commonly encountered in combinatorics.

**Depends** methods

**License** GPL-3

**NeedsCompilation** no

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apv

*Amalgams Pseudo-Vector Constructor***Description**

The APV class defines a pseudo-vector containing all the arranged k-amalgams (permutations with replacement) of the objects stored in `items`. The function `apv` is a constructor for this class.

**Usage**

```
apv(k, items)
```

**Arguments**

|                    |  |
|--------------------|--|
| <code>k</code>     | the number of objects taken at a time. |
| <code>items</code> | a vector of objects to be amalgamated. |

**Details**

The amalgams are arranged according to the order in which the objects appear in `items`. The arrangement is very similar to that used by the PPV class (see [ppv](#)) except that objects are replaced during permutation creation.

**Value**

an instance of APV.

**Author(s)**

Richard Ambler

**References**

Steinhaus-Johnson-Trotter algorithm. (2014, April 29). In *Wikipedia, The Free Encyclopedia*. Retrieved 13:24, September 5, 2014

**See Also**

Permutations Pseudo-Vector [ppv](#)  
Combinations Pseudo-Vector [cpv](#)  
Selections Pseudo-Vector [spv](#)  
Subsets Pseudo-Vector [sspv](#)

**Examples**

```
# create a pseudo-vector of 10-amalgams from the first 15 letters
a <- apv(10, letters[1:15])
# generate a description
print(a)
# compatible with length
length(a)
# inspect a few of the combinations "stored" in a
a[1]
a[1000000]
a[576650390625]
```

cpv

*Combinations Pseudo-Vector Constructor***Description**

The CPV class defines a pseudo-vector containing all the arranged k-combinations of the objects stored in `items`. The function `cpv` is a constructor for this class.

**Usage**

```
cpv(k, items)
```

**Arguments**

|                    |  |
|--------------------|--|
| <code>k</code>     | the number of objects taken at a time. |
| <code>items</code> | a vector of objects to be combined.    |

**Details**

The combinations are arranged according to the order in which the objects appear in `items`. Combinations containing the first object in `items` are followed by combinations that contain the second object but not the first, which are followed by combinations that contain the third but neither the first or the second, etc.

**Value**

an instance of CPV.

**Author(s)**

Richard Ambler

**References**

Steinhaus-Johnson-Trotter algorithm. (2014, April 29). In *Wikipedia, The Free Encyclopedia*. Retrieved 13:24, September 5, 2014

**See Also**

Permutations Pseudo-Vector [ppv](#)

Amalgams Pseudo-Vector [apv](#)

Selections Pseudo-Vector [spv](#)

Subsets Pseudo-Vector [ssp](#)

**Examples**

```
# create a pseudo-vector of 10-combinations from the first 15 letters
c <- cpv(10, letters[1:15])
# generate a description
print(c)
# compatible with length
length(c)
# inspect a few of the combinations "stored" in c
c[1]
c[1000]
c[3003]
```

---

|                   |                                      |
|-------------------|--------------------------------------|
| length,APV-method | <i>Amalgams Pseudo-Vector Length</i> |
|-------------------|--------------------------------------|

---

**Description**

Get the length of an APV instance.

**Usage**

```
## S4 method for signature 'APV'
length(x)
```

**Arguments**

x                      an instance of APV

**Details**

Since x contains all the k-amalgams of objects in vector items, length(x) will return length(items)<sup>k</sup>.

**Value**

the number of amalgams (permutations with replacement) in pseudo-vector x

**See Also**

Permutations Pseudo-Vector [ppv](#)  
Combinations Pseudo-Vector [cpv](#)  
Selections Pseudo-Vector [spv](#)  
Subsets Pseudo-Vector [ssp](#)

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|                   |  |
|-------------------|--|
| length,CPV-method | <i>Combinations Pseudo-Vector Length</i> |
|-------------------|--|

---

**Description**

Get the length of a CPV instance.

**Usage**

```
## S4 method for signature 'CPV'  
length(x)
```

**Arguments**

x                      an instance of CPV

**Details**

Since x contains all the k-combinations of objects in vector `items`, `length(x)` will return `choose(length(items), k)`.

**Value**

the number of combinations in pseudo-vector x

**See Also**

Permutations Pseudo-Vector [ppv](#)  
Amalgams Pseudo-Vector [apv](#)  
Selections Pseudo-Vector [spv](#)  
Subsets Pseudo-Vector [ssp](#)

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|                   |  |
|-------------------|--|
| length,PPV-method | <i>Permutations Pseudo-Vector Length</i> |
|-------------------|--|

---

### Description

Get the length of a PPV instance.

### Usage

```
## S4 method for signature 'PPV'
length(x)
```

### Arguments

x                      an instance of PPV

### Details

Since x contains all the k-permutations of objects in vector `items`, `length(x)` will return `choose(length(items), k) * factorial(k)`.

### Value

the number of permutations in pseudo-vector x

### See Also

Combinations Pseudo-Vector [cpv](#)

Amalgams Pseudo-Vector [apv](#)

Selections Pseudo-Vector [spv](#)

Subsets Pseudo-Vector [ssp](#)

---

|                   |  |
|-------------------|--|
| length,SPV-method | <i>Selections Pseudo-Vector Length</i> |
|-------------------|--|

---

### Description

Get the length of an SPV instance.

### Usage

```
## S4 method for signature 'SPV'
length(x)
```

**Arguments**

x                      an instance of SPV

**Details**

Since x contains all the k-selections of objects in vector items, length(x) will return choose(length(items) + k - 1, k).

**Value**

the number of selections (combinations with replacement) in pseudo-vector x

**See Also**

- Permutations Pseudo-Vector [ppv](#)
- Combinations Pseudo-Vector [cpv](#)
- Amalgams Pseudo-Vector [apv](#)
- Subsets Pseudo-Vector [sspv](#)

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|                     |                                     |
|---------------------|-------------------------------------|
| length, SSPV-method | <i>Subsets Pseudo-Vector Length</i> |
|---------------------|-------------------------------------|

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**Description**

Get the length of an SSPV instance.

**Usage**

```
## S4 method for signature 'SSPV'  
length(x)
```

**Arguments**

x                      an instance of SSPV

**Details**

Since x contains all the subsets of objects in vector items, length(x) will return  $2^{\text{length(items)}}$ .

**Value**

the number of subsets in pseudo-vector x

**See Also**

Permutations Pseudo-Vector [ppv](#)  
Combinations Pseudo-Vector [cpv](#)  
Amalgams Pseudo-Vector [apv](#)  
Selections Pseudo-Vector [spv](#)

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ppv

*Permutations Pseudo-Vector Constructor*

---

**Description**

The PPV class defines a pseudo-vector containing all the k-permutations of the objects stored in `items`. The function `ppv` is a constructor for this class.

**Usage**

```
ppv(k, items)
```

**Arguments**

|                    |  |
|--------------------|--|
| <code>k</code>     | the number of objects taken at a time. |
| <code>items</code> | a vector of objects to be permuted.    |

**Details**

The arrangement of permutations is similar, but in many cases not identical, to that obtained from the Steinhaus-Johnson-Trotter algorithm (see references).

**Value**

an instance of PPV.

**Author(s)**

Richard Ambler

**References**

Steinhaus-Johnson-Trotter algorithm. (2014, April 29). In *Wikipedia, The Free Encyclopedia*. Retrieved 13:24, September 5, 2014

**See Also**

Combinations Pseudo-Vector [cpv](#)  
Amalgams Pseudo-Vector [apv](#)  
Selections Pseudo-Vector [spv](#)  
Subsets Pseudo-Vector [sspv](#)



## Examples

```
# create a pseudo-vector of 5-permutations from the first 10 letters
p <- ppv(5, letters[1:10])
# generate a description
print(p)
# comparable with length
length(p)
# inspect a few of the permutations "stored" in p
p[1]
p[1000]
p[30240]
```

---

spv

*Selections Pseudo-Vector Constructor*


---

## Description

The SPV class defines a pseudo-vector containing all the arranged k-selections (combinations with replacement) of the objects stored in `items`. The function `spv` is a constructor for this class.

## Usage

```
spv(k, items)
```

## Arguments

|                    |  |
|--------------------|--|
| <code>k</code>     | the number of objects taken at a time. |
| <code>items</code> | a vector of objects to be selected.    |

## Details

The selections are arranged according to the order in which the objects appear in `items`. The arrangement is very similar to the arrangement of combinations (see [cpv](#)) except that objects may be repeatedly selected.

## Value

an instance of SPV.

## Author(s)

Richard Ambler

## References

Steinhaus-Johnson-Trotter algorithm. (2014, April 29). In *Wikipedia, The Free Encyclopedia*. Retrieved 13:24, September 5, 2014

**See Also**

Permutations Pseudo-Vector [ppv](#)  
Combinations Pseudo-Vector [cpv](#)  
Amalgams Pseudo-Vector [apv](#)  
Subsets Pseudo-Vector [sspv](#)

**Examples**

```
# create a pseudo-vector of 10-selections from the first 15 letters
s <- spv(10, letters[1:15])
# generate a description
print(s)
# computable with length
length(s)
# inspect a few of the combinations "stored" in s
s[1]
s[1000]
s[1961256]
```

---

sspv

*Subsets Pseudo-Vector Constructor*

---

**Description**

The SSPV class defines a pseudo-vector containing all the arranged subsets of the objects stored in `items`. The function `sspv` is a constructor for this class.

**Usage**

```
sspv(items)
```

**Arguments**

`items`                      a vector of objects to be subsetted.

**Details**

The subsets are arranged according to the order in which the objects appear in `items`. The first subset, containing none of the objects, is `NULL`.

**Value**

an instance of SSPV.

**Author(s)**

Richard Ambler

**See Also**

Permutations Pseudo-Vector [ppv](#)  
 Combinations Pseudo-Vector [cpv](#)  
 Amalgams Pseudo-Vector [apv](#)  
 Selections Pseudo-Vector [spv](#)

**Examples**

```
# create a pseudo-vector of subsets from the first 15 letters
ss <- sspv(letters[1:15])
# generate a description
print(ss)
# compatable with length
length(ss)
# inspect a few of the combinations "stored" in ss
ss[1]
ss[1000]
ss[32768]
```

[,APV-method

*Retrieve an Amalgam by Index***Description**

Access an amalgam (permutation with replacement) stored in an APV instance by index.

**Usage**

```
## S4 method for signature 'APV'
x[i, j, drop]
```

**Arguments**

|      |  |
|------|--|
| x    | an instance of APV.                                    |
| i    | an index specifying the position of the sought amalgam |
| j    | not used.  |
| drop | not used.  |

**Details**

The amalgam at index *i* of pseudo-vector *x* is not actually stored in memory but calculated as needed. The extract method is used solely for interpretation.

**Value**

the amalgam located at position *i* in pseudo-vector *x*

**See Also**

Permutations Pseudo-Vector [ppv](#)  
 Combinations Pseudo-Vector [cpv](#)  
 Selections Pseudo-Vector [spv](#)  
 Subsets Pseudo-Vector [ssp](#)

[,CPV-method

*Retrieve a Combination by Index***Description**

Access a combination stored in a CPV instance by index.

**Usage**

```
## S4 method for signature 'CPV'
x[i, j, drop]
```

**Arguments**

|      |   |
|------|---|
| x    | an instance of CPV.   |
| i    | an index specifying the position of the sought combination. |
| j    | not used.   |
| drop | not used.   |

**Details**

The combination at index *i* of pseudo-vector *x* is not actually stored in memory but calculated as needed. The extract method is used solely for interpretation.

**Value**

the combination located at position *i* in pseudo-vector *x*

**See Also**

Permutations Pseudo-Vector [ppv](#)  
 Amalgams Pseudo-Vector [apv](#)  
 Selections Pseudo-Vector [spv](#)  
 Subsets Pseudo-Vector [ssp](#)

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|              |  |
|--------------|--|
| [,PPV-method | <i>Retrieve a Permutation by Index</i> |
|--------------|--|

---

## Description

Access a permutation stored in a PPV instance by index.

## Usage

```
## S4 method for signature 'PPV'  
x[i, j, drop]
```

## Arguments

|      |   |
|------|---|
| x    | an instance of PPV.   |
| i    | an index specifying the position of the sought permutation. |
| j    | not used.   |
| drop | not used.   |

## Details

The permutation at index *i* of pseudo-vector *x* is not actually stored in memory but calculated as needed. The `extract` method is used solely for interpretation.

## Value

the permutation located at position *i* in pseudo-vector *x*

## See Also

Combinations Pseudo-Vector [cpv](#)

Amalgams Pseudo-Vector [apv](#)

Selections Pseudo-Vector [spv](#)

Subsets Pseudo-Vector [sspv](#)

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|              |                                      |
|--------------|--------------------------------------|
| [,SPV-method | <i>Retrieve a Selection by Index</i> |
|--------------|--------------------------------------|

---

### Description

Access a selection (combination with replacement) stored in an SPV instance by index.

### Usage

```
## S4 method for signature 'SPV'  
x[i, j, drop]
```

### Arguments

|      |   |
|------|---|
| x    | an instance of SPV.                                       |
| i    | an index specifying the position of the sought selection. |
| j    | not used.   |
| drop | not used.   |

### Details

The selection at index *i* of pseudo-vector *x* is not actually stored in memory but calculated as needed. The `extract` method is used solely for interpretation.

### Value

the selection located at position *i* in pseudo-vector *x*

### See Also

Permutations Pseudo-Vector [ppv](#)  
Combinations Pseudo-Vector [cpv](#)  
Amalgams Pseudo-Vector [apv](#)  
Subsets Pseudo-Vector [sspv](#)

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|                |                                   |
|----------------|-----------------------------------|
| [, SSPV-method | <i>Retrieve a Subset by Index</i> |
|----------------|-----------------------------------|

---

**Description**

Access asubset stored in an SSPV instance by index.

**Usage**

```
## S4 method for signature 'SSPV'  
x[i, j, drop]
```

**Arguments**

- x                    an instance of SSPV.
- i                    an index specifying the position of the sought amalgam
- j                    not used.
- drop                not used.

**Details**

The subset at index i of pseudo-vector x is not actually stored in memory but calculated as needed.  
The extract method is used solely for interpretation.

**Value**

the subset located at position i in pseudo-vector x

**See Also**

- Permutations Pseudo-Vector [ppv](#)
- Combinations Pseudo-Vector [cpv](#)
- Amalgams Pseudo-Vector [apv](#)
- Selections Pseudo-Vector [spv](#)

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