## **Package 'truelies'**

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Type Package

**Title** Bayesian Methods to Estimate the Proportion of Liars in Coin Flip Experiments

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**Description** Implements Bayesian methods, described in Hugh-Jones (2019) <doi:10.1007/s40881-019-00069-x>, for estimating the proportion of liars in coin flip-style experiments, where subjects report a random outcome and are paid for reporting a ``good" outcome.

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URL https://github.com/hughjonesd/truelies

BugReports https://github.com/hughjonesd/truelies/issues

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compare\_dists

Calculate probability that one posterior is larger than another

## Description

Given two distributions with density functions  $\phi_1, \phi_2$ , this calculates:

$$\int_0^1 \int_0^{l_1} \phi_1(l_1) \phi_2(l_2) dl_2 dl_1,$$

the probability that the value of the first distribution is greater.

## Usage

compare\_dists(dist1, dist2)

## Arguments

| dist1 | Density of distribution 1, as a one-argument function. |
|-------|--|
| dist2 | Density of distribution 2.                             |

## Value

A probability scalar.

## Examples

d1 <- update\_prior(30, 50, P = 0.5, prior = stats::dunif)
d2 <- update\_prior(25, 40, P = 0.5, prior = stats::dunif)
compare\_dists(d1, d2)</pre>

difference\_dist Find density of the difference of two distributions

#### Description

Given two probability density functions dist1 and dist2, difference\_dist returns the density of "dist1 - dist2'.

#### Usage

```
difference_dist(dist1, dist2)
```

#### Arguments

dist1, dist2 Probability density functions

#### Details

At the moment this only works when dist1 and dist2 are defined on [0, 1].

#### Value

A probability density function defined on [-1, 1].

## Examples

```
d1 <- update_prior(30, 50, P = 0.5, prior = stats::dunif)
d2 <- update_prior(32, 40, P = 0.5, prior = stats::dunif)
dd <- difference_dist(d1, d2)
dist_hdr(dd, 0.95)</pre>
```

dist\_hdr

Compute highest density region for a density function

#### Description

This is a wrapper for hdrcde::hdr. The highest density region is the interval that covers conf\_level of the data and has the highest average density. See:

#### Usage

```
dist_hdr(dist, conf_level, bounds = attr(dist, "limits"))
```

## Arguments

| dist       | A one-argument function                                       |
|------------|---|
| conf_level | A scalar between 0 and 1                                      |
| bounds     | A length 2 vector of the bounds of the distribution's support |

## Details

Rob J Hyndman (1996) "Computing and graphing highest density regions". American Statistician, 50, 120-126.

## Value

A length 2 vector of region endpoints

## Examples

d1 <- update\_prior(33, 50, P = 0.5, prior = stats::dunif)
dist\_hdr(d1, 0.95)</pre>

dist\_mean

Find mean of a probability density function

## Description

Find mean of a probability density function

#### Usage

```
dist_mean(dist, l = attr(dist, "limits")[1], r = attr(dist,
    "limits")[2])
```

#### Arguments

| dist | A one-argument function returned from update_prior() |
|------|--|
| 1    | Lower bound of the density's support                 |
| r    | Upper bound of the density's support                 |

#### Value

A scalar

#### Examples

```
d1 <- update_prior(10, 40, P = 5/6, prior = stats::dunif)
dist_mean(d1)</pre>
```

dist\_quantile

## Description

Find quantiles given a probability density function

#### Usage

dist\_quantile(dist, probs, bounds = attr(dist, "limits"))

## Arguments

| dist   | A one argument function                                       |
|--------|---|
| probs  | A vector of probabilities                                     |
| bounds | A length 2 vector of the bounds of the distribution's support |

## Value

A vector of quantiles

## Examples

d1 <- update\_prior(33, 50, P = 0.5, prior = stats::dunif)
dist\_quantile(d1, c(0.025, 0.975))</pre>

| empirical_bayes | Estimate | proportions | of | liars | in | multiple | samples | using | empirical |
|-----------------|----------|-------------|----|-------|----|----------|---------|-------|-----------|
|                 | Bayes    |             |    |       |    |          |         |       |           |

## Description

This function creates a prior by fitting a Beta distribution to the heads/N vector, using MASS::fitdistr(). The prior is then updated using data from each individual sample to give the posterior distributions.

#### Usage

```
empirical_bayes(heads, ...)
## Default S3 method:
empirical_bayes(heads, N, P, ...)
## S3 method for class 'formula'
empirical_bayes(formula, data, P, subset, ...)
```

#### Arguments

| heads   | A vector of numbers of the good outcome reported  |
|---------|---|
|         | Ignored   |
| Ν       | A vector of sample sizes  |
| Р       | Probability of <i>bad</i> outcome   |
| formula | A two-sided formula of the form heads ~ group. heads is a logical vector spec-<br>ifying whether the "good" outcome was reported. group specifies the sample. |
| data    | A data frame or matrix. Each row represents one individual.   |
| subset  | A logical or numeric vector specifying the subset of data to use  |

#### Details

The formula interface allows calling the function directly on experimental data.

#### Value

A list with two components:

- prior, the calculated empirical prior (of class densityFunction).
- posterior, a list of posterior distributions (objects of class densityFunction). If heads was named, the list will have the same names.

#### Examples

)

empirical\_bayes(I(report == "heads") ~ group, data = raw\_data, P = 0.5)

group = rep(LETTERS[1:10], each = 30)

power\_calc

## Description

This uses simulations to estimate the power to detect a given level of lying in a sample of size N by this package's methods.

#### Usage

```
power_calc(N, P, lambda, alpha = 0.05, prior = stats::dunif,
    nsims = 200)
```

#### Arguments

| Ν      | Total number in sample  |
|--------|---|
| Р      | Probability of bad outcome  |
| lambda | Probability of a subject lying  |
| alpha  | Significance level to use for the null hypothesis   |
| prior  | Prior over lambda. A function which takes a vector of values between 0 and 1, and returns the probability density. The default is the uniform distribution. |
| nsims  | Number of simulations to run  |

## Value

Estimated power, a scalar between 0 and 1.

#### Examples

 $power_calc(N = 50, P = 0.5, lambda = 0.2)$ 

power\_calc\_difference Estimate power to detect differences in lying between two samples

## Description

Using simulations, estimate power to detect differences in lying using compare\_dists(), given values for  $\lambda$ , the probability of lying, in each sample.

#### Usage

```
power_calc_difference(N1, N2 = N1, P, lambda1, lambda2, alpha = 0.05,
    alternative = c("two.sided", "greater", "less"),
    prior = stats::dunif, nsims = 200)
```

## Arguments

| N1          | N of sample 1   |
|-------------|---|
| N2          | N of sample 2   |
| Р           | Probability of <i>bad</i> outcome   |
| lambda1     | Probability of lying in sample 1  |
| lambda2     | Probability of lying in sample 2  |
| alpha       | Significance level  |
| alternative | "two.sided", "greater" (sample 1 is greater), or "less". Can be abbreviated   |
| prior       | Prior over lambda. A function which takes a vector of values between 0 and 1, and returns the probability density. The default is the uniform distribution. |
| nsims       | Number of simulations to run  |

## Value

Estimated power, a scalar between 0 and 1.

## Examples

power\_calc\_difference(N1 = 100, P = 0.5, lambda = 0, lambda2 = 0.25)

print.densityFunction *Print/plot an object of class* densityFunction.

## Description

Print/plot an object of class densityFunction.

## Usage

```
## S3 method for class 'densityFunction'
print(x, ...)
```

## S3 method for class 'densityFunction'
plot(x, ...)

## Arguments

| х | The object |
|---|------------|
|   | Unused     |

## update\_prior

#### Examples

```
d1 <- update_prior(33, 50, P = 0.5, prior = stats::dunif)
d1
plot(d1)
# show the actual R code (techies only)
unclass(d1)</pre>
```

update\_prior Calculate posterior distribution of the proportion of liars

#### Description

update\_prior uses the equation for the posterior:

$$\phi(\lambda|R;N,P) = \Pr(R|\lambda;N,P)\phi(\lambda) / \int \Pr(R|\lambda';N,P)\phi(\lambda')d\lambda'$$

where  $\phi$  is the prior and  $Pr(R|\lambda; N, P)$  is the probability of R reports of heads given that people lie with probability  $\lambda$ :

$$Pr(R|\lambda; N, P) = binom(N, (1 - P) + \lambda P)$$

#### Usage

update\_prior(heads, N, P, prior = stats::dunif, npoints = 1000)

#### Arguments

| heads   | Number of good outcomes reported  |
|---------|---|
| Ν       | Total number in sample  |
| Р       | Probability of <i>bad</i> outcome   |
| prior   | Prior over lambda. A function which takes a vector of values between 0 and 1, and returns the probability density. The default is the uniform distribution. |
| npoints | How many points to integrate on?  |

#### Value

The probability density of the posterior distribution, as a one-argument function.

#### Examples

```
posterior <- update_prior(heads = 30, N = 50, P = 0.5, prior = stats::dunif)
plot(posterior)</pre>
```

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